

Supplemental Data

Title: A two-state model for the kinetics of competitive radioligand binding

Running title: a two-state model for kinetic investigation

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1. Enter equations for unlabeled ligands into Graphpad Prism 6.

Enter the data as below. The title for each group is the concentration of the competitor in the unit of M. For this example, Y values have already been corrected to baseline and normalized to the maximal binding of radioligand at 180 min. Values at each data point represent the mean of five individual experiments each performed in duplicate.

X	Group A					Group B					Group C					Group D				
time (min)	0					1e-8					3e-8					1e-7				
X	A:Y1	A:Y2	A:Y3	A:Y4	A:Y5	B:Y1	B:Y2	B:Y3	B:Y4	B:Y5	C:Y1	C:Y2	C:Y3	C:Y4	C:Y5	D:Y1	D:Y2	D:Y3	D:Y4	D:Y5
0	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
1	9.894714	18.87389	19.31058	17.069890	21.093460	10.10956	14.82283	13.28848	9.921174	26.09900	11.02278	11.77820	13.70482	10.80457	11.10085	8.456811	8.598828	8.383534	5.986296	10.088490
3	32.939410	37.50308	37.44980	32.346750	37.439970	27.78256	31.49275	29.23380	20.250070	38.55032	19.72497	28.20327	26.87338	19.92389	18.54869	12.591320	12.338140	10.90380	10.179400	13.151090
7	49.482830	53.87701	58.82661	52.718130	48.280480	39.07391	44.28282	49.21362	33.283500	48.04211	30.35024	32.07918	32.81469	28.78171	24.82900	18.946000	18.388840	14.072980	13.548680	16.868830
14	69.582290	65.28219	64.97697	60.750200	59.468980	52.58984	54.49548	53.29852	39.725470	54.83813	32.14439	38.49265	37.88514	30.52480	31.41054	17.851400	20.230740	18.00990	16.188480	19.889980
22	71.153850	71.91547	67.80455	66.553410	67.738190	56.15899	58.38795	54.78950	46.392770	49.56871	38.07478	42.29172	40.89812	33.36146	41.52196	19.907610	21.915470	18.708170	16.528230	24.529000
30	73.205840	73.18593	74.39759	72.546890	65.773520	55.43618	61.20205	63.21954	46.412070	55.43037	35.05587	44.00195	45.86384	34.78488	44.08940	18.872110	22.843880	18.473900	17.205700	25.378650
40	80.092390	80.18588	82.29585	75.129110	72.201700	61.84590	66.88487	66.08099	54.294640	61.74732	40.81435	46.10310	45.49898	39.31775	41.44810	19.348950	21.648710	18.992840	19.271540	25.360180
60	84.581870	83.58173	85.24097	82.440880	76.209620	68.85082	67.40777	60.74297	63.583470	61.71038	37.96734	48.02101	50.51874	42.59510	55.20613	19.338200	23.137080	19.986850	19.976250	27.151830
90	89.589600	88.14708	86.19478	82.298810	81.283390	71.29351	71.85439	65.88019	68.143620	79.73772	44.90761	53.85268	49.73228	43.53085	55.08095	23.238080	24.138770	19.811780	22.328940	30.070190
120	101.101700	96.55509	96.19748	90.323480	92.371630	77.18092	74.87028	72.35009	82.388620	78.42830	42.81283	52.77303	49.59639	44.90351	60.04802	19.123330	23.808840	21.201470	21.377910	29.700780
180	100.000000	100.000000	100.000000	100.000000	100.000000	85.58230	78.10898	78.24832	77.800470	75.45253	48.29179	55.47278	48.81191	44.00852	63.48509	28.418130	29.198190	26.288490	25.004780	28.483240

With this, click on the **Analyze** button. From **XY analyses** choose **Nonlinear regression (curve fit)** and click **User-defined equations**. Click **New** and choose **Create new equation**. Enter the following equations under the tag **Equation** in **Definition** as illustrated below:

$$kA_R1 = k1*A+k2$$

$$kA_R2 = k3*A+k4$$

$$kB_R1 = k5*B+k6$$

$$kB_R2 = k7*B+k8$$

$$AR1_ss = k1*A*Bmax*Span*k6/(kA_R1*kB_R1-k1*k5*A*B)$$

$$AR2_ss = k3*A*Bmax*(1-Span)*k8/(kA_R2*kB_R2-k3*k7*A*B)$$

$$S_R1 = \text{SQRT}((kA_R1-kB_R1)^2 + 4*k1*k5*A*B)$$

$$S_R2 = \text{SQRT}((kA_R2-kB_R2)^2 + 4*k3*k7*A*B)$$

$$KF_R1 = 0.5*(kA_R1 + kB_R1 + S_R1)$$

$$KS_R1 = 0.5*(kA_R1 + kB_R1 - S_R1)$$

$$KF_R2 = 0.5*(kA_R2 + kB_R2 + S_R2)$$

$$KS_R2 = 0.5*(kA_R2 + kB_R2 - S_R2)$$

$$P1 = (k1*A*Bmax*Span - KS_R1*AR1_ss)/(KF_R1 - KS_R1)$$

$$P2 = (k3*A*Bmax*(1-Span) - KS_R2*AR2_ss)/(KF_R2 - KS_R2)$$

$$Q1 = (KF_R1*AR1_ss - k1*A*Bmax*Span)/(KF_R1 - KS_R1)$$

$$Q2 = (KF_R2*AR2_ss - k3*A*Bmax*(1-Span))/(KF_R2 - KS_R2)$$

$$Y = AR1_ss - P1*\exp(-KF_R1*x) - Q1*\exp(-KS_R1*x) + AR2_ss - P2*\exp(-KF_R2*x) - Q2*\exp(-KS_R2*x)$$

User-defined Equation



Equation Rules for Initial Values Default Constraints Transforms to Report

Equation type
Explicit Equation: Y = a function of X and parameters.

Name
two-state competition association assay

Definition Available functions

```
kA_R1 = k1*A+k2  
kA_R2 = k3*A+k4  
kB_R1 = k5*B+k6  
kB_R2 = k7*B+k8  
AR1_ss = k1*A*Bmax*Span*k6 / (kA_R1*kB_R1-k1*k5*A*B)  
AR2_ss = k3*A* Bmax*(1-Span)*k6 / (kA_R2*kB_R2-k3*k7*A*B)
```

Tip

Description

Help Cancel OK

Click OK and choose the tag “Rule for Initial Values”. Enter parameters as illustrated below

User-defined Equation



Equation Rules for Initial Values Default Constrains Transforms to Report

Define a set of rules to compute initial values to use as a default every time you curve fit with this equation.

Initial Values

Parameter Name	Initial Value	Rule
k1	1.000000e+007	(Initial value, to be fit)
A	2.000000e-008	(Initial value, to be fit)
k2	0.05	(Initial value, to be fit)
k3	1000000.0	(Initial value, to be fit)
k4	0.005	(Initial value, to be fit)
k5	1.000000e+007	(Initial value, to be fit)
B	0.0	(Initial value, to be fit)
k6	0.01	(Initial value, to be fit)
k7	1000000.0	(Initial value, to be fit)
k8	0.005	(Initial value, to be fit)
Bmax	100.0	(Initial value, to be fit)
Span	0.5	(Initial value, to be fit)

Default range

Start graphing the curve at: The smallest X value X = 0

Clone this equation Edit equation Help Close

Click OK and choose the tag “Default Constrains”. Set parameters as illustrated below

Equation Rules for Initial Values **Default Constraints** Transforms to Report

Define a set of constraints to use as the default every time you curve fit with this equation

Fix, constrain or share a parameter

Parameter Name	Constraint Type	Value
k1	Constant equal to	
A	Constant equal to	
k2	Constant equal to	
k3	Constant equal to	
k4	Constant equal to	
k5	Shared, and must be greater than	0.0
B	Data set constant (=column title)	
k6	Shared, and must be greater than	0.0
k7	Shared, and must be greater than	0.0
k8	Shared, and must be greater than	0.0
Bmax	Shared, and must be greater than	0.0

Constrain one parameter relative to another

must be greater than times

must be greater than times

Help Cancel **OK**

And click OK.

Enter k1, k2, k3 and k4 predetermined by kinetic radioligand binding experiments and the concentration of the radioligand (A) as below. Note: the units for A and B are in M.

Parameters: Nonlinear Regression X

Fit Compare **Constrain** Weights Initial values Range Output Diagnostics

Parameter Name	Constraint Type	Value	Hook
k1	Constant equal to	1.474000e+007	
A	Constant equal to	1.900000e-008	
k2	Constant equal to	0.04642	
k3	Constant equal to	432800.0	
k4	Constant equal to	0.007616	
k5	Shared, and must be greater than	0.0	
B	Data set constant (=column title)		
k6	Shared, and must be greater than	0.0	
k7	Shared, and must be greater than	0.0	
k8	Shared, and must be greater than	0.0	
Bmax	Shared, and must be greater than	0.0	
Span	Shared, and must be between zero and	1.0	

Constrain one parameter relative to another

 must be greater than 1.0 times

 must be greater than 1.0 times

Learn Cancel **OK**

Click OK and analyze the result.