# **Decentralized adaptive force/position control of reconfigurable manipulator based on soft sensors**

**Yanli Du<sup>1</sup> and Quanmin Zhu<sup>2</sup>**

#### **Abstract**

Two soft sensor control methods are proposed to deal with force/position control of reconfigurable manipulators without using wrist force sensors. Firstly, modeling uncertainties and coupling interconnection terms between the subsystems are approximated by using adaptive RBF neural network, and the soft sensor model of the contact force is established by means of adaptive RBF neural network to design hybrid force/position controller. Then, a decentralized impedance inner/force outer loop controller is designed. The reference trajectory of impedance inner controller is provided by force outer loop controller based on the fuzzy prediction, and the soft sensor model of the contact force is established by the fuzzy system. The proposed soft sensor model does not request the exact mathematical relationship between the end contact force and auxiliary variables, and provides a feasible method to replace the wrist force sensors which are expensive and easily noised by the external factors. Compared with the observer method, the proposed methods provide better position and force tracking precision.

#### **Keywords**

Reconfigurable manipulator, soft sensor, decentralized hybrid force/position control, impedance inner control, adaptive RBF neural network, fuzzy approximation

#### 1 Introduction

Reconfigurable manipulators can form the various configurations of different degrees of freedom (DOF) to carry out tasks and are widely applied in the field of dangerous work environment, space exploration, and military, industrial, medical, entertainment etc. There are many tasks like polishing, grabbing and operation that require interaction between reconfigurable manipulator and the environment. This fact requires that the position and the contact force with the environment for reconfigurable manipulator should be controlled at the same time. So, many researchers have done lots of researches on the force and position control of the manipulator in recent years [1-10].

The force control methods of the manipulator include force/position control [1-4] and impedance control [5-10], but these methods require a wrist force sensor to be installed at the manipulator end. In the applications of industrial manipulators, high accurate and reliable force sensors are very expensive, and the use of force sensors will increase the complexity of the manipulator in electrical, mechanical and software parts. There are various uncertainties and environmental factors in the industrial field, which may have influence to the precision of the sensor and operational reliability. In recent years, to improve the reliability of the manipulator control system, external force estimation method of reconfigurable manipulator is proposed. Colomé [11] proposes a robust observer to estimate contact forces between the manipulator and the environment. The force sensor is not used in this method. In order to estimate the position and force of the manipulator during FSW processes, Qin [12] proposes a non-linear observer to estimate not only the state (position and velocity) of links, but also the external forces exerted by the robot during Friction Stir Welding (FSW) processes. In order to ensure a

Email: [quan.zhu@uwe.ac.uk](mailto:quan.zhu@uwe.ac.uk)

 $\overline{a}$ 

<sup>&</sup>lt;sup>1</sup> College of Electrical Information Engineering, Beihua University, Jilin, China

<sup>&</sup>lt;sup>2</sup>Department of Engineering Design and Mathematics, University of the West of England, Bristol BS161QY, UK

**Corresponding author:** Quanmin Zhu ,Department of Engineering Design and Mathematics, University of the West of England, Bristol, UK.

better tracking performance, the data such as real positions, velocities of links and external forces are required. Wang [13] designs an observer to approximate force, and in order to overcome the uncertainty of the environment, the adaptive law of stiffness is derived. Chan [14] proposed a force estimation method based on the active observer in the presence of the noise for the robot. It can not only estimate contact force, but also observe the state of the system. Du [15] proposes a decentralized adaptive force control method based on nonlinear joint torque observer for reconfigurable manipulator. The nonlinear observer is designed to observe the torque of each joint, and finally get the contact force by Jacobian matrix transformation.

The above methods are to estimate the contact force by the observer, which is difficult to prove the convergence of the observation error and is easily affected by the observed noise. So, in recent years, many scholars have invested in the research of force control methods based on soft sensor technology. Ren [16] and Cho [17] present a soft sensor method to solve the problem that stress signal is difficult to obtain in the health monitoring of multibody manipulator. In the method, stress signal is considered as dominant variable and angle signal is regarded as auxiliary variable. By establishing the mathematical relationship between them, a soft sensor model is proposed. Hammond [18] proposes a soft sensor method for the submillimeter contact localization and force measurement in micromanipulation. Tactile sensing experiments verify the effectiveness of the method. Yang [19] has designed a novel pneumatic soft sensor (PSS). According to the inner pressure of sensing body, PSS can measure contact force and curvature by building relation models of contact force and curvature, and its measurement accuracy is tested by a large of experiments.

The above force estimation methods based on soft sensor need to know the mathematical relationship between contact force and auxiliary variables. For reconfigurable manipulator system, it is difficult to determine the mathematical relationship between end contact force and other auxiliary variables. To solve the problem and avoid the difficulty in observer design and convergence analysis, this study presents two

kinds of decentralized adaptive force control methods based on soft sensor. One is the hybrid force/position control method based on adaptive RBF neural network estimation. The contact force is estimated by RBF neural network, and the adaptive laws of its center and width are deduced. The other is the impedance inner/ force outer loop control method based on the Fuzzy prediction reference trajectory. The end contact force is approximated by the fuzzy systems. The proposed two methods derive adaptive laws of all parameters, and are compared with the force estimation method based on the observer.

This article is organized as follows. Problem formulation, the necessity and importance for study of position and force control based on soft sensor is described in section "Introduction". In section "Reconfigurable manipulator dynamic model", the dynamic model of reconfigurable manipulator and the subsystem dynamic model at each direction are given. In section "The decentralized force controller design based on soft sensor", design and simulation of two force/position controllers based on soft sensor are proposed. The last section is the conclusion.

### 2 Reconfigurable manipulator dynamic

#### model

When reconfigurable manipulator is in contact with the environment, its dynamic model with the external disturbance in the joint space is

 $M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) + \tau_f(q, \dot{q}, t) = \tau - \tau_c$  (1) where  $q \in R^n$  denotes the joint position;  $\dot{q}$ ,  $\ddot{q}$  are the speed and acceleration of the joint, respectively;  $M(q) \in R^{n \times n}$  is the inertia matrix;  $C(q, \dot{q})\dot{q} \in R^n$  donates the Centripetal and Coriolis torques;  $G(q) \in \mathbb{R}^n$  is the gravitational torque vector;  $\tau \in R^n$  is the control torque;  $\tau_c \in R^n$  is the torque vector exerted by the manipulator on the environment;  $\tau_{f}(q, \dot{q}, t) \in R^{n}$  is the external disturbance.

Consider the following equations[20]

$$
\begin{cases}\n\dot{X} = J\dot{q} \\
\ddot{X} = \dot{J}\dot{q} + J\ddot{q} \\
\tau = J^T F\n\end{cases}
$$

where  $J$  is the Jacobian matrix;  $F$  and  $X$  are the contact force and position of the task space, respectively.

With the workspace position  $X$  as the variable, the equation (1) is written as

$$
M_{x}\ddot{X} + C_{x}\dot{X} + G_{x} + F_{f} = F - F_{C}
$$
 (2)

where

$$
M_x = J^{-T} M(q) J^{-1}
$$
  
\n
$$
C_x = J^{-T} [C(q, \dot{q}) - M(q) J^{-1} \dot{J}] J^{-1}
$$
  
\n
$$
G_x = J^{-T} G(q)
$$
  
\n
$$
F_f = J^{-T} \tau_f(q, \dot{q}, t)
$$
  
\n
$$
F_c = J^{-T} \tau_c
$$

The model of reconfigurable manipulator is decomposed at each direction, and the dynamic model of the subsystem *j* is as follows

$$
M_j(x_j)\ddot{x}_j + C_j(x_j, \dot{x}_j)\dot{x}_j + G_j(x_j) + F_j(x_j, \dot{x}_j, t) + Z_j(X, \dot{X}, \ddot{X}) = F_j - F_{cj}
$$
 (3)

where  $x_j$  is the jth element of the vector X and

$$
Z_j(X, \dot{X}, \ddot{X}) = \left\{ \sum_{m=1, m \neq j}^n M_{jm}(X)\ddot{x}_m + [M_{jj}(X) - M_j(x_j)\ddot{x}_j] \right\} + \left\{ \sum_{m=1, m \neq j}^n C_{jm}(X, \dot{X})\dot{x}_m + [C_{jj}(X, \dot{X}) - C_j(x_j, \dot{x}_j)\dot{x}_j] \right\} + [\overline{G}_j(x_j) - G_j(x_j)]
$$

is coupled interconnection between the subsystems.

In the premise of without wrist force sensor, the next task is to design the controller based on soft sensor for the subsystem equation (3) so as to realize the position and force control of reconfigurable manipulator in the constrained space.



**Figure1.** Control block diagram of decentralized hybrid force/position controller

## 3 The decentralized force controller design

## based on soft sensor

**3.1 The design of decentralized hybrid force/position controller based on adaptive RBFNN soft sensor model**

#### **3.1.1 Controller design**

The advantage of the hybrid force/position controller is able to directly control contact force. In this part, PI control algorithm based on the force error is adopted to control force and PID control algorithm based on the position error is used in the position control. In the absence of wrist force sensor, the soft sensor model of

the contact force is established based on adaptive RBFNN, and subsystem uncertainty and coupling interconnection are also estimated by using RBFNN. The control block diagram of decentralized hybrid force/position controller is shown in Figure1.

The force error and position error of the subsystems are defined as follows:

$$
e_{jj} = \hat{F}_{cj} - F_{dj}, e_{pj} = x_j - x_{dj}
$$

where  $\hat{F}_{c_j}$  is the estimate value of  $F_{c_j}$ ,  $x_{d_j}$  and  $F_{d_j}$ are respectively the desired position and contact force.

Letting

$$
x_{jr} = \dot{x}_{dj} - k_{pj}e_{pj} - \lambda_j \int_0^t e_{pj} d\tau - k_{jj}e_{jj}
$$

$$
- \gamma_j \int_0^t e_{jj} d\tau
$$

 $s_j = \dot{x}_j - x_j$ 

We have

$$
s_j = \dot{x}_j - x_{jr}
$$
  
=  $\dot{e}_{pj} + k_{pj}e_{pj} + \lambda_j \int_0^t e_{pj} d\tau + k_{jj}e_{jj}$   
+  $\gamma_j \int_0^t e_{jj} d\tau$ 

So

$$
\dot{s}_j = \ddot{x}_j - \dot{x}_{jr} = \ddot{e}_{pj} + k_{pj} \dot{e}_{pj} + \lambda_j e_{pj} + k_{jj} \dot{e}_{jj} + \gamma_j e_{jj}
$$
\n(4)

Bringing  $\dot{x}_j = s_j + x_{jr}$  and  $\ddot{x}_j = \dot{s}_j + \dot{x}_{jr}$ 

into equation (3), then equation (3) will be

$$
M_j(x_j) (s_j + \dot{x}_{jr}) + C_j(x_j, \dot{x}_j) (s_j + x_{jr})
$$
  
+  $G_j(x_j) + F_j(x_j, \dot{x}_j, t) + Z_j(X, \dot{X}, \ddot{X}) = F_j - F_{cj}$ 

The above equation is written as

$$
M_j(x_j)\dot{s}_j + C_j(x_j, \dot{x}_j)s_j + h_j(s_j) = F_j - F_{cj}(x_j, \dot{x}_j)
$$

where

$$
h_j = M_j(x_j)\dot{x}_{jr} + C_j(x_j, \dot{x}_j)x_{jr} + G_j(x_j) + F_j(x_j, \dot{x}_j, t) + Z_j(X, \dot{X}, \ddot{X})
$$

We introduce a decentralized control law that is described by

$$
F_j = \hat{F}_{cj}(x_j, \dot{x}_j, |s_j|) + \hat{h}_j(|x_j|, s_j) - m_j s_j
$$
  
+  $u_{jc} + u_{jr}$  (5-a)

$$
u_{jc} = -(E_{1f} + E_{1h})sign(s_j^T)
$$
 (5-b)

$$
u_{j\tau} = -k_{j\tau} \Big| F_j - F_{uj} \Big| sign(s_j^T) \tag{5-c}
$$

where  $u_{jc}$  is the approximation error compensation;  $u_{j\tau}$  is the joint torque compensation;  $E_{1f}$  and  $E_{1h}$ are the error upper bounds of the contact force  $F_{cj}(x_j, \dot{x}_j)$  and  $h_j(s_j)$  ,respectively;  $k_{j\tau}$  and  $m_j$  are the positive constants;  $F_{ij}$  is the output mapping of the joint torque sensor;  $\hat{F}_{cj}(x_j, \dot{x}_j, |s_j|)$ and  $\hat{h}_j(|x_j|, s_j)$  are respectively the estimate values of  $F_{cj}(x_j, \dot{x}_j)$  and  $h_j(s_j)$  that can be expressed by using adaptive RBFNN

$$
\hat{F}_{cj}(x_j, \dot{x}_j, |s_j|) = \hat{W}_{j\ell}^T \xi_{j\ell} (x_j, \dot{x}_j, |s_j|)
$$

$$
\hat{h}_j(|x_j|, s_j) = \hat{W}_{j\ell}^T \xi_{j\ell}(|x_j|, s_j)
$$

where  $\hat{W}_{jfc}$ ,  $\hat{W}_{jh}$  are the weight vectors;  $\xi_{jh}(|x_j|, s_j)$ and  $\zeta_{jfc}(x_j, \dot{x}_j, |s_j|)$  are the radial basis functions (Internal structure of RBFNN for estimating contact

## force refers to **Appendix I**).

The following adaptive laws of the parameters are obtained

$$
\dot{\hat{W}}_{jfc} = \eta_{j1} s_j^T \hat{\xi}_{jfc}(x_j, \dot{x}_j, |s_j|)
$$
 (6-a)

$$
\dot{\hat{W}}_{jh} = \eta_{j2} s_j^T \hat{\xi}_{jh} (x_j, s_j) \tag{6-b}
$$

$$
\dot{\hat{c}}_{jfc} = \eta_{j3} s_j^T \frac{\partial \xi_{jfc}}{\partial \hat{c}_{jfc}} \hat{W}_{jfc}(x_j, \dot{x}_j, |s_j|)
$$
(6-c)

$$
\dot{\hat{b}}_{jfc} = \eta_{j4} s_j^T \frac{\partial \xi_{jfc}}{\partial \hat{b}_{jfc}} \hat{W}_{jfc}(x_j, \dot{x}_j, |s_j|)
$$
(6-d)

$$
\dot{\hat{c}}_{jh} = \eta_{j5} S_j^T \frac{\partial \xi_{jh}}{\partial \hat{c}_{jh}} \hat{W}_{jh} (x_j | s_j)
$$
 (6-e)

$$
\dot{\hat{b}}_{jh} = \eta_{j6} s_j^T \frac{\partial \xi_{jh}}{\partial \hat{b}_{jh}} \hat{W}_{jh} (x_j | s_j)
$$
 (6-f)

where  $\hat{c}_{jfc}$ ,  $\hat{c}_{jh}$  and  $\hat{b}_{jfc}$ ,  $\hat{b}_{jh}$  are centers and widths of the radial basis function  $\hat{\xi}_{j\ell c}(x_j, \dot{x}_j, |s_j|)$  and  $\hat{\xi}_{jk}(|x_j|, s_j)$ , respectively;  $\eta_{j1}, \eta_{j2}, \eta_{j3}, \eta_{j4}, \eta_{j5}, \eta_{j6}$ are the positive constants.

Property 1. For the scalar function  $M_j(q_j)$  and  $C_j(q_j, \dot{q}_j)$ , there is the following equation [21]:  $s_j^T[\dot{M}_j(q_j) - 2C_j(q_j, \dot{q}_j)]s_j = 0 \quad \forall s_j \in R$ 

Assumption 1. Approximation errors of RBFNN are assumed to be bounded by  $\left| \varepsilon_{1j} \right| \leq E_{1f}$ ,  $\left| \varepsilon_{1jh} \right| \leq E_{1h}$ , where  $\varepsilon_{1j}$  and  $\varepsilon_{1jh}$  are the approximation errors of  $F_{cj}(x_j, \dot{x}_j)$  and  $h_j(s_j)$ , respectively.

Theorem 1. For the subsystem dynamic model described by equation (3), if the decentralized control laws such as equation (5) and adaptive laws of the parameters such as equation (6) are applied, the position error and force error of reconfigurable manipulator system will [asymptotically](http://dict.cnki.net/dict_result.aspx?searchword=%e6%b8%90%e8%bf%91&tjType=sentence&style=&t=asymptotically) [converge](javascript:showjdsw() to [zero](javascript:showjdsw() in the constrained space.

**Proof.** The Lyapunov function is defined by

$$
V = \sum_{j=1}^{n} V_j
$$

where

$$
\begin{aligned} V_j&=\frac{1}{2}\,s_j^T M_{j}s_j\,+\frac{1}{2\eta_{j1}}\,\widetilde{W}_{j\ell^c}^T\widetilde{W}_{j\ell^c}+\frac{1}{2\eta_{j2}}\,\widetilde{W}_{j\hbar}^T\widetilde{W}_{j\hbar}\\ &+\frac{1}{2\eta_{j3}}\,\widetilde{c}_{j\ell^c}^T\widetilde{c}_{j\ell^c}+\frac{1}{2\eta_{j4}}\,\widetilde{b}_{j\ell^c}^T\widetilde{b}_{j\ell^c}+\frac{1}{2\eta_{j5}}\,\widetilde{c}_{j\hbar}^T\widetilde{c}_{j\hbar}+\frac{1}{2\eta_{j6}}\,\widetilde{b}_{j\hbar}^T\widetilde{b}_{j\hbar} \end{aligned}
$$

where  $\hat{W}_{\text{ifc}} = W_{\text{ifc}} \cdot \hat{W}_{\text{ifc}}$ , and the other error variables are like this.

The time derivative of Lyapunov function  $V_j$  is

$$
\dot{V}_{j} = \frac{1}{2} s_{j}^{T} \dot{M}_{j} s_{j} + s_{j}^{T} M_{j} \dot{s}_{j} - \frac{1}{\eta_{j1}} \tilde{W}_{j\bar{k}}^{\bar{T}} \dot{\hat{W}}_{j\bar{k}} - \frac{1}{\eta_{j2}} \tilde{W}_{j\bar{k}}^{\bar{T}} \dot{\hat{W}}_{j\bar{k}} \n- \frac{1}{\eta_{j3}} \tilde{c}_{j\bar{k}}^{\bar{T}} \dot{\hat{c}}_{j\bar{k}} - \frac{1}{\eta_{j4}} \tilde{b}_{j\bar{k}}^{\bar{T}} \dot{\hat{b}}_{j\bar{k}} - \frac{1}{\eta_{j5}} \tilde{c}_{j\bar{k}}^{\bar{T}} \dot{\hat{b}}_{j\bar{k}} - \frac{1}{\eta_{j6}} \tilde{b}_{j\bar{k}}^{\bar{T}} \dot{\hat{b}}_{j\bar{k}} \n= \frac{1}{2} s_{j}^{\bar{T}} \dot{M}_{j} s_{j} + s_{j}^{\bar{T}} (F_{j} - F_{\epsilon_{j}} - C_{j} s_{j} - h_{j}) - \frac{1}{\eta_{j1}} \tilde{W}_{j\bar{k}}^{\bar{T}} \dot{\hat{W}}_{j\bar{k}} \n- \frac{1}{\eta_{j2}} \tilde{W}_{j\bar{k}}^{\bar{T}} \dot{\hat{W}}_{j\bar{k}} - \frac{1}{\eta_{j3}} \tilde{c}_{j\bar{k}}^{\bar{T}} \dot{\hat{c}}_{j\bar{k}} - \frac{1}{\eta_{j4}} \tilde{b}_{j\bar{k}}^{\bar{T}} \dot{\hat{b}}_{j\bar{k}} - \frac{1}{\eta_{j5}} \tilde{c}_{j\bar{k}}^{\bar{T}} \dot{\hat{C}}_{j\bar{k}} \n- \frac{1}{\eta_{j5}} \tilde{b}_{j\bar{k}}^{\bar{T}} \dot{\hat{b}}_{j\bar{k}} \n= \frac{1}{2} s_{j}^{\bar{T}} (\dot{M}_{j} - 2C_{j}) s_{j} + s_{j}^{\bar{T}} (F_{j} - F_{\epsilon_{j}} - h_{j}) \n- \frac{1}{\eta_{j1}} \tilde{W}_{j\bar{k}}^{\bar{T}} \dot{\hat{W}}_{j\bar{k}} - \frac{1}{\eta_{j2}} \tilde{W}_{j\bar{k}}^
$$

Using property 1 and control law equation (5), it is easy to show that

$$
\dot{V}_{j} = s_{j}^{T}[\hat{F}_{cj} + \hat{h}_{j} - m_{j}s_{j} + u_{jc} + u_{jr} - F_{cj} - h_{j}] \n- \frac{1}{\eta_{j1}} \tilde{W}_{jfe}^{\tau} \dot{\hat{W}}_{jfe} - \frac{1}{\eta_{j2}} \tilde{W}_{jh}^{\tau} \dot{\hat{W}}_{jh} - \frac{1}{\eta_{j3}} \tilde{c}_{jfe}^{\tau} \dot{\hat{c}}_{jfe} \n- \frac{1}{\eta_{j4}} \tilde{b}_{jfe}^{\tau} \dot{\hat{b}}_{jfe} - \frac{1}{\eta_{j5}} \tilde{c}_{jh}^{\tau} \dot{\hat{c}}_{jh} - \frac{1}{\eta_{j6}} \tilde{b}_{jh}^{\tau} \dot{\hat{b}}_{jh} \n= -m_{j}s_{j}^{T}s_{j} + s_{j}^{T}u_{jc} + s_{j}^{T}u_{jr} + -s_{j}^{T} \tilde{F}_{cj} - s_{j}^{T} \tilde{h}_{j} \n- \frac{1}{\eta_{j1}} \tilde{W}_{jfe}^{\tau} \dot{\hat{W}}_{jfe} - \frac{1}{\eta_{j2}} \tilde{W}_{jh}^{\tau} \dot{\hat{W}}_{jh} - \frac{1}{\eta_{j3}} \tilde{c}_{jfe}^{\tau} \dot{\hat{c}}_{jfe} \n- \frac{1}{\eta_{j4}} \tilde{b}_{jfe}^{\tau} \dot{\hat{b}}_{jfe} - \frac{1}{\eta_{j5}} \tilde{c}_{jh}^{\tau} \dot{\hat{c}}_{jh} - \frac{1}{\eta_{j6}} \tilde{b}_{jh}^{\tau} \dot{\hat{b}}_{jh}
$$

For an arbitrary function  $f_j = W_k^T \xi_k + \varepsilon_j$  $f_j = W_k^T \xi_k + \varepsilon_j$ , its estimate value is  $\hat{f}_j = \sum_{k=1}^N \hat{W}_{jk} \hat{\xi}_{jk} = \hat{W}_k^T \hat{\xi}_k$  $\hat{f}_j$  =  $\sum_{k=1}^{\infty} \hat{W}_{jk} \hat{\xi}_{jk}$  = $\hat{W}_k^T \hat{\xi}_k$  $= \sum_{i=1}^{5} \hat{W}_{ik} \hat{\xi}_{ik} =$ 1 ,where  $\varepsilon_j$  is the estimate error and  $\hat{f}_j$  is the adaptive RBFNN estimate value of  $f_j$ , then

$$
\tilde{f}_j = f_j - \hat{f}_j
$$
\n
$$
= W_k^T \xi_k + \varepsilon_j - \hat{W}_k^T \hat{\xi}_k
$$
\n
$$
= (\hat{W}_k + \hat{W}_k)^T (\hat{\xi}_k + \tilde{\xi}_k) + \varepsilon_j - \hat{W}_k^T \hat{\xi}_k \tag{7}
$$
\n
$$
= \hat{W}_k^T \tilde{\xi}_k + \tilde{W}_k^T \hat{\xi}_k + \hat{W}_k^T \tilde{\xi}_k + \varepsilon_j
$$
\n
$$
= \hat{W}_k^T \tilde{\xi}_k + \tilde{W}_k^T \hat{\xi}_k + \varepsilon_{1j}
$$

where  $\varepsilon_{1i} = \widetilde{W}_k^T \widetilde{\xi}_k + \varepsilon_i + \widetilde{W}_k^T o(h)$  $k$   $\top$   $\boldsymbol{\epsilon}_j$   $\top$   $\boldsymbol{w}_k$  $\mathcal{E}_{1j} = \widetilde{W}_k^T \widetilde{\xi}_k + \mathcal{E}_j + \widehat{W}_k^T o(h).$ 

According to Taylor series expansion, we can

obtain

$$
\widetilde{\xi}_{k} = \frac{\partial \xi_{k}}{\partial \hat{c}_{k}} \cdot \widetilde{c}_{k} + \frac{\partial \xi_{k}}{\partial \hat{b}_{k}} \cdot \widetilde{b}_{k}
$$
\n(8)

By analogy with equation (7) and equation (8), we get

$$
\begin{split} \dot{V}_j &= -m_j s_j^T s_j + s_j^T u_{jc} + s_j^T u_{jr} - s_j^T [\tilde{W}_{jjc}^T \hat{\xi}_{jjc} + \varepsilon_{1jf} + \\ &\quad \hat{W}_{jjc}^T (\frac{\partial \xi_{jfc}}{\partial \hat{c}_{jjc}} \cdot \tilde{c}_{jtc} + \frac{\partial \xi_{jfc}}{\partial \hat{b}_{jtc}} \cdot \tilde{b}_{jtc}) \big] - s_j^T [\tilde{W}_{jh}^T \hat{\xi}_{jh} + \\ &\varepsilon_{1jh} + \hat{W}_{jh}^T (\frac{\partial \xi_{jh}}{\partial \hat{c}_{jh}} \cdot \tilde{c}_{jh} + \frac{\partial \xi_{jh}}{\partial \hat{b}_{jh}} \cdot \tilde{b}_{jh}) \big] - \frac{1}{\eta_{ji}} \tilde{W}_{jjc}^T \dot{\hat{W}}_{jtc} \\ &- \frac{1}{\eta_{j2}} \tilde{W}_{jh}^T \dot{\hat{W}}_{jh} - \frac{1}{\eta_{js}} \tilde{c}_{jjc}^T \dot{\hat{c}}_{jtc} - \frac{1}{\eta_{js}} \tilde{b}_{jjc}^T \dot{\hat{b}}_{jtc} - \frac{1}{\eta_{js}} \tilde{c}_{jh}^T \dot{\hat{c}}_{jh} \\ &- \frac{1}{\eta_{js}} \tilde{b}_{jh}^T \dot{\hat{b}}_{jh} \end{split}
$$

Since 
$$
\hat{W}_{jfc}^T \frac{\partial \xi_{jfc}}{\partial \hat{c}_{jfc}} \cdot \tilde{c}_{jfc} = \tilde{c}_{jfc}^T \frac{\partial \xi_{jfc}}{\partial \hat{c}_{jfc}} \hat{W}_{jfc}
$$
 and

adaptive laws of the parameters in the equation (6) are introduced into above equation, we get

$$
\dot{V}_j = -m_j s_j^T s_j + s_j^T u_{jc} + s_j^T u_{jt} - s_j^T \varepsilon_{1jf} - s_i^T \varepsilon_{1jh} \n\le -m_j s_j^T s_j + s_j^T u_{jc} + s_j^T u_{jt} + |s_j^T| E_{1f} + |s_j^T| E_{1h}
$$

 According to the equation (5-c), the above inequality can be written

$$
\dot{V}_j \le -m_j s_j^T s_j + s_j^T u_{jc} + \left| s_j^T \right| E_{1f} + \left| s_j^T \right| E_{1h}
$$

Applying equation (5-b), it is easy to obtain

$$
\dot{V}_j \le -m_j s_j^2
$$
, namely  $\dot{V} = \sum_{j=1}^n \dot{V}_j \le \sum_{j=1}^n -m_j s_j^2$ .

Because  $\int_0^\infty \sum_{j=1}^n m_j s_j^2 \leq -\int_0^\infty \dot{V} dt = V(0) - V(\infty) < \infty$  $0 \t 1 \t 0$   $J_0$  $\sum_{i=1}^{n} m_i s_i^2 \leq -\int_{-\infty}^{\infty} V dt = V(0) - V(\infty)$  $\sum_{j=1}^{K} m_j s_j^2 \leq -\int_0^{\infty} \dot{V} dt = V(0) - V(\infty) < \infty$ , it

is obvious that  $s_j \in L_2$ . By equation (4) can be

known  $\dot{s}_j \in L_\infty$ . According to Babalat lemma [22],

 $\lim_{t\to\infty} s_j(t) = 0$ , and this means that the theorem is proved.

#### **3.1.2 Simulation results**

The designed controller is applied to 2-DOF planar reconfigurable manipulator in the Figure 2(a).



(a) 2-DOF planar manipulator (b) 3-DOF reconfigurable manipulator **Figure 2.** Reconfigurable manipulator configurations

The desired position trajectory is defined as  $y_d = 0.5 \sin t$  in the Y direction, and the desired force is  $f_d = (1 + \sin t)N$  in the X direction.

To show the efficiency of the proposed method in improving the tracking accuracy, the observer in reference [15] is also employed in the simulation for comparison. The simulation results under the proposed soft sensor and the observer are depicted in Figures 3.



**Figure 3.** Force and position tracking of 2-DOF planar manipulator

The 3-DOF reconfigurable manipulator is shown in Figure 2(b). The contact force is controlled in Z direction of the constrained surface, and the position trajectories are controlled in Y and X directions. Given the desired force  $f_d = (1 + \sin t)N$ , and desired

trajectories are set to be  $x_d = \sin(t)$ ,  $y_d = \cos(t)$ . The simulation results are shown in Figure 4.





It is observed from Figures 3 and 4 that in the initial stage of the observer, the observer lacks the knowledge of the subsystem dynamics model, so its tracking error is relatively large during the first 0.5 s. In the following tracking process, the observer is easily affected by the Jacobi matrix transformation and the parameters of the proposed soft sensor method are adjusted in real time according to the force error and the position error, so the simulation accuracy of the proposed soft sensor method is better than the observer method.

It is worth noting that this method can cause certain impact force when the manipulator moves from free space to constrained space, so it is only suitable for position and force control in constrained space.

## **3.2 The design of impedance inner/ force outer loop controller based on adaptive fuzzy soft sensor model**

The impedance control method can realize indirectly force control by adjusting the reference position. The soft sensor model of the contact force is established based on adaptive fuzzy system in the proposed method, and corrected value of the reference trajectory for the impedance inner controller is provided by output of the force outer loop controller based on the fuzzy prediction.

## **3.2.1 The reference trajectory algorithm based on the fuzzy prediction**

The algorithm consists of the following parts:

1) The reference trajectory that makes the current output value gradually transit to the setting value. The equation is written as

$$
F_{dj}(k + i) = \alpha^i \times \hat{F}_{cj} + (1 - \alpha^i) \times F_{dj}
$$

where  $\alpha$  is the softness coefficient,  $k$  is the sampling time,  $i$  is the predictive step.

2) The prediction model is chosen as

$$
B_d\dot{X} + K_d(X - X_r) = F_d - F_c
$$

where  $B_d$  and  $K_d$  are the desired damping and position stiffness matrices, respectively. They are replaced by the  $b_d$  and  $k_d$  in the subsystem; X is the position of the manipulator;  $X_r$  is the reference trajectory of the impedance inner controller. The selected model is equivalent to

$$
F_{cj}(k + i) = F_{dj}(k + i) - b_d \dot{x}_j(k) - k_d [x_j(k) - x_{rj}(k)]
$$

 3) The prediction output (equivalent to the feedback correction) is

$$
F_{pj}(k + i) = F_{cj}(k + i) + \beta_i [\hat{F}_{cj} - F_{cj}(k)]
$$

where  $\beta_i$  is the correction coefficient.

#### **3.2.2 Controller design and prove**

The block diagram of impedance control system is shown in Figure 5.

The force error and position error are defined as

$$
e_{fj} = \hat{F}_{cj} - F_{dj}
$$

$$
e_{pj} = x_j - x_{dj}
$$

They are introduced into the first order filter

$$
\dot{\mu}_j + k_j \mu_j = \eta_j e_{jj}
$$
  

$$
\dot{p}_j + k_j p_j = \lambda_j e_{pj}
$$

$$
\sigma_j
$$
 is defined by  $\sigma_j = \dot{e}_{pj} + p_j + \mu_j$ ,

namely  $p_j = \sigma_j - \dot{e}_{pj} - \mu_j$ . The time derivative of  $\sigma_j$  is given by

where  $k_j$ ,  $\eta_j$  and  $\lambda_j$  are the positive constants,  $\mu_j$  and  $p_j$  are the filter outputs.



Figure 5. Block diagram of impedance control system

$$
\dot{\sigma}_j = \ddot{e}_{ij} + \dot{p}_j + \dot{\mu}_j
$$
  
\n
$$
= \ddot{e}_{ij} + \lambda_j e_{ij} - k_j p_j + \eta_j e_{jj} - k_j \mu_j
$$
  
\n
$$
= \ddot{e}_{ij} + \lambda_j e_{ij} - k_j (\sigma_j - \dot{e}_{ij} - \mu_j) + \eta_j e_{jj} - k_j \mu_j
$$
  
\n
$$
= \ddot{e}_{ij} + \lambda_j e_{ij} + k_j \dot{e}_{ij} - k_j \sigma_j + \eta_j e_{jj}
$$

The above equation is rewritten as

$$
\ddot{e}_{pj} + k_j \dot{e}_{pj} + \lambda_j e_{pj} = \dot{\sigma}_j + k_j \sigma_j - \eta_j e_{jj} \qquad (9)
$$

By choosing  $\left(\eta_{j} = m_d^{-1}\right)$  $\overline{\phantom{a}}$  $\vert$ ∤  $\int$  $=$  $=$  $\overline{a}$  $\overline{a}$ 1 1  $\eta_j = m_d^$  $j$  *d*  $\mu_d$   $\mu_d$  $j$  *d*  $\theta_d$  $m_d^{-1}k$  $k_i = m_d^{-1}b_j$  $\lambda_i = m_d^{-1} k_d$ ,  $\dot{\sigma}_i = 0$  and  $\sigma_i = 0$ ,

equation (9) is identical to the target impedance as follows equation (10).

$$
m_d \ddot{e}_{pj} + b_d \dot{e}_{pj} + k_d e_{pj} = -e_{jj}
$$
 (10)

where  $m_d$  is the desired inertia.

Differentiating 
$$
\sigma_j
$$
 with respect to time, we have  
\n
$$
\dot{\sigma}_j = \ddot{e}_{ni} + \dot{p}_j + \dot{\mu}_j
$$
\n
$$
= M_j^{-1} [F_j - F_{ij} - C_j(x_j, \dot{x}_j)\dot{x}_j - G_j(x_j)
$$
\n
$$
- F_j(x_j, \dot{x}_j, t) - Z_j(X, \dot{X}, \ddot{X})] - \ddot{x}_{ij}
$$
\n
$$
+ \dot{p}_j + \dot{\mu}_j
$$
\n(11)

The control law is obtained as:

$$
F_{j} = \hat{F}_{g}(x_{j}, \dot{x}_{j}, |\sigma_{j}|) + \hat{C}_{j}(x_{j}, \dot{x}_{j})\dot{x}_{j} + \hat{G}_{j}(x_{j}) +
$$
\n
$$
\hat{F}_{g}(x_{j}, \dot{x}_{j}, t) + \hat{Z}_{j}(X, \dot{X}, \ddot{X}) +
$$
\n
$$
\hat{M}_{j}(\ddot{x}_{d_{j}} - \dot{p}_{j} - \dot{\mu}_{j}) - m_{j}\sigma_{j} + u_{j} + u_{j} \qquad (12-a)
$$
\n
$$
= \hat{M}_{j}\ddot{x}_{j\alpha_{q}} + \hat{C}_{j}\dot{x}_{j\alpha_{q}} + \hat{G}_{j}(x_{j}) + \hat{F}_{g}(x_{j}, \dot{x}_{j}, t) +
$$
\n
$$
\hat{Z}_{j}(X, \dot{X}, \ddot{X}) + \hat{F}_{g} - m_{j}\sigma_{j} + u_{j} + u_{j} \qquad
$$
\n
$$
u_{j} = -(d_{j m}|\ddot{x}_{j\alpha_{q}}| + d_{j\alpha}|\dot{x}_{j\alpha_{q}}| + d_{j\alpha} +
$$
\n
$$
d_{j} + d_{jz} + d_{j\beta})sign(\sigma_{j}^{T}) \qquad (12-b)
$$

$$
u_{ja} = -k_{ja} \Big| F_j - F_{uj} \Big| sign(\sigma_j^T) \tag{12-c}
$$

where

$$
\sigma_j = 0 \Rightarrow \dot{x}_{jeq} = \dot{x}_{dj} - p_j - \mu_j
$$

$$
\dot{\sigma}_j = 0 \Rightarrow \ddot{x}_{jeq} = \ddot{x}_{dj} - \dot{p}_j - \dot{\mu}_j
$$

 $d_{jm}$ ,  $d_{jc}$ ,  $d_{js}$ ,  $d_{jf}$ ,  $d_{jz}$ ,  $d_{jfc}$  are error upper bounds of of  $M_j(x_j), C_j(x_j, \dot{x}_j)$ ,  $G_j(x_j), F_j(x_j, \dot{x}_j, t)$ ,  $Z_j(X, \dot{X}, \ddot{X})$  and  $F_{cj}$ , respectively;  $\hat{F}_{cj}(x_j, \dot{x}_j, |\sigma_j|)$ ,  $\hat{M}_j(x_j), \hat{C}_j(x_j, \dot{x}_j), \hat{G}_j(x_j), \hat{F}_j(x_j, \dot{x}_j, t), \hat{Z}_j(X, \dot{X}, \ddot{X})$ are the estimates of  $F_{cj}$ ,  $M_j(x_j)$ ,  $C_j(x_j, \dot{x}_j)$ ,  $G_j(x_j)$ ,  $F_{jj}(x_j, \dot{x}_j, t)$  and  $Z_j(X, \dot{X}, \ddot{X})$ , respectively;  $F_{uj}$  is the output mapping of the joint torque sensor;  $u_{jc}$  is

the compensation of the estimation error ;  $u_{ja}$  is the compensation of the joint torque measured value;  $k_{ja}$ is the positive constant.

The fuzzy system representations are described by

$$
\hat{F}_{cj}(x_j, \dot{x}_j, |\sigma_j|) = \hat{\theta}_{j\ell}^T \xi_{j\ell}(x_j, \dot{x}_j, |\sigma_j|)
$$
\n
$$
\hat{M}_j(x_j) = \hat{\theta}_{jm}^T \xi_{jm}(x_j)
$$
\n
$$
\hat{C}_j(x_j, \dot{x}_j) = \hat{\theta}_{jc}^T \xi_{jc}(x_j, \dot{x}_j)
$$
\n
$$
\hat{G}_j(x_j) = \hat{\theta}_{js}^T \xi_{js}(x_j)
$$
\n
$$
\hat{F}_{jj}(x_j, \dot{x}_j, t) = \hat{\theta}_{jj}^T \xi_{jj}(x_j, \dot{x}_j, t_j)
$$
\n
$$
\hat{Z}_j(X, \dot{X}, \ddot{X}) = \hat{\theta}_{jc}^T \xi_{jc}(X, \dot{X}, \ddot{X})
$$
\nwhere  $\hat{\theta}_{j\ell}, \hat{\theta}_{jm}, \hat{\theta}_{jc}, \hat{\theta}_{js}, \hat{\theta}_{jj}$  and  $\hat{\theta}_{jz}$  are the adjustable parameter vectors, respectively;  $\xi_{j\ell}(x_j, \dot{x}_j, |\sigma_j|)$ ,  $\xi_{jm}(x_j)$ ,  $\xi_{jc}(x_j, \dot{x}_j)$ ,  $\xi_{js}(x_j)$ ,  $\xi_{j\ell}(x_j, \dot{x}_j, t_j)$  and  $\xi_{jz}(X, \dot{X}, \ddot{X})$  are the fuzzy basis function vectors, respectively;

function of fuzzy system for estimating contact force

#### refers to **Appendix II**).

The adaptive laws of the parameters are

$$
\dot{\hat{\theta}}_{jm} = \eta_{j1} \sigma_j^T \xi_{jm} \ddot{x}_{jeq} \tag{13-a}
$$

$$
\dot{\hat{\theta}}_{jc} = \eta_{j2} \sigma_j^T \xi_{jc} \dot{x}_{jeq}
$$
 (13-b)

$$
\dot{\hat{\theta}}_{jg} = \eta_{j3} \sigma_j^T \xi_{jg} \tag{13-c}
$$

$$
\dot{\hat{\theta}}_{jz} = \eta_{j4} \sigma_j^T \xi_{jz}
$$
 (13-d)

$$
\dot{\hat{\theta}}_{jfc} = \eta_{js}\sigma_j^T \xi_{jfc}
$$
\n
$$
\dot{\hat{\theta}}_{fj} = \eta_{js}\sigma_j^T \xi_{fj}
$$
\n(13-f)

where  $\eta_{j1}$ ,  $\eta_{j2}$ ,  $\eta_{j3}$ ,  $\eta_{j4}$ ,  $\eta_{j5}$ ,  $\eta_{j6}$  are the positive constants.

*fj*

Assumption 2. Approximation errors of the fuzzy system are assumed to be bounded by  $|\varepsilon_{jm}| \leq d_{jm}$ ,  $\left| \varepsilon_{i_{c}} \right| \leq d_{i_{c}}, \left| \varepsilon_{i_{g}} \right| \leq d_{i_{g}}, \left| \varepsilon_{j_{j}} \right| \leq d_{j_{j}}, \left| \varepsilon_{i_{z}} \right| \leq d_{i_{z}},$ 

 $\mathcal{E}_{\textit{ifc}} \leq d_{\textit{ifc}}$ , where  $\mathcal{E}_{\textit{jm}}$ ,  $\mathcal{E}_{\textit{jc}}$ ,  $\mathcal{E}_{\textit{jg}}$ ,  $\mathcal{E}_{\textit{fj}}$ ,  $\mathcal{E}_{\textit{jz}}$  and  $\mathcal{E}_{\textit{ifc}}$ are approximation errors of  $M_j(x_j)$ ,  $C_j(x_j, \dot{x}_j)$ ,  $G_j(x_j)$ ,  $F_{jj}(x_j, x_j, t)$ ,  $Z_j(X, \dot{X}, \ddot{X})$  and  $F_{cj}$ , respectively.

**Theorem 2.** For the subsystem dynamic model described by equation (3), reconfigurable manipulator system achieves the target impedance equation (10) with the decentralized control law equation (12) and the adaptive laws of the parameters equation (13).

**Proof.** Lyapunov function is chosen as

$$
V\,=\,\sum_{\scriptscriptstyle j=1}^{\scriptscriptstyle n}V_{\scriptscriptstyle j}
$$

where

$$
\begin{split} V_j\;&=\;\frac{1}{2}\,M_j\sigma_j^2\,+\,\frac{1}{2\eta_{j1}}\,\widetilde{\theta}_{jm}^T\widetilde{\theta}_{jm}\,+\,\frac{1}{2\eta_{j2}}\,\widetilde{\theta}_{jc}^T\widetilde{\theta}_{jc}\,+\,\frac{1}{2\eta_{j3}}\,\widetilde{\theta}_{js}^T\widetilde{\theta}_{js}\\ &+\,\frac{1}{2\eta_{j4}}\,\widetilde{\theta}_{jc}^T\widetilde{\theta}_{jc}\,+\,\frac{1}{2\eta_{j5}}\,\widetilde{\theta}_{jfc}^T\widetilde{\theta}_{jc}\,+\,+\,\frac{1}{2\eta_{j6}}\,\widetilde{\theta}_{jj}^T\widetilde{\theta}_{jj} \end{split}
$$

Differentiating  $V_j$  with respect to time, then

$$
\dot{V}_{j} = \frac{1}{2} \sigma_{j}^{T} \dot{M}_{j} \sigma_{j} + \sigma_{j}^{T} M_{j} \dot{\sigma}_{j} - \frac{1}{\eta_{j1}} \tilde{\theta}_{jm}^{T} \dot{\tilde{\theta}}_{jm} - \frac{1}{\eta_{j2}} \tilde{\theta}_{jc}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{j3}} \tilde{\theta}_{jc}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{j4}} \tilde{\theta}_{jc}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{js}} \tilde{\theta}_{jfc}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{js}} \tilde{\theta}_{jb}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{js}} \tilde{\theta}_{jb}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\eta_{js}} \tilde{\theta}_{jc}^{T} \dot{\tilde{\theta}}_{jc} - \frac{1}{\
$$

Using equation (12-a), we get

$$
\vec{V}_{j} = \sigma_{j}^{T}[\hat{M}_{j}\ddot{x}_{jeq} + \hat{C}_{j}\dot{x}_{jeq} + \hat{G}_{j}(x_{j}) + \hat{F}_{jj}(x_{j}, \dot{x}_{j}, t) \n+ \hat{Z}_{j}(X, \dot{X}, \ddot{X}) + \hat{F}_{cj} - m_{j}\sigma_{j} + u_{jc} + u_{ja} -\nF_{cj} - G_{j}(x_{j}) - F_{jj}(x_{j}, \dot{x}_{j}, t) - Z_{j}(X, \dot{X}, \ddot{X}) -\nM_{j}\ddot{x}_{jeq} - C_{j}\dot{x}_{jeq}] - \frac{1}{\eta_{ji}} \hat{\theta}_{jm}^{T}\dot{\hat{\theta}}_{jm} - \frac{1}{\eta_{j2}} \hat{\theta}_{jc}^{T}\dot{\hat{\theta}}_{jc} -\n\frac{1}{\eta_{j3}} \hat{\theta}_{js}^{T}\dot{\hat{\theta}}_{js} - \frac{1}{\eta_{ja}} \hat{\theta}_{jc}^{T}\dot{\hat{\theta}}_{jc} - \frac{1}{\eta_{js}} \hat{\theta}_{jic}^{T}\dot{\hat{\theta}}_{jc} - \frac{1}{\eta_{js}} \hat{\theta}_{jj}^{T}\dot{\hat{\theta}}_{jb} \n= -m_{j}\sigma_{j}^{2} + \sigma_{j}^{T}u_{k} + \sigma_{j}^{T}u_{ja} + \sigma_{j}^{T}(\tilde{M}_{j}\ddot{x}_{jaq} + \tilde{C}_{j}\dot{x}_{jaq}) +\tilde{G}_{j}(x_{j}) + \tilde{Z}_{j}(X, \dot{X}, \ddot{X}) + \tilde{F}_{q} + \tilde{F}_{j}(x_{j}, \dot{x}_{j}, t)) \n+ \sigma_{j}^{T}(-\varepsilon_{ja}\ddot{x}_{jaq} - \varepsilon_{ja}\ddot{x}_{jaq} - \varepsilon_{ja} - \varepsilon_{ja} - \varepsilon_{ja} - \varepsilon_{jb} - \frac{1}{\eta_{ja}} \tilde{\theta}_{ja}^{T}\dot{\hat{\theta}}_{ja} \n- \frac{1}{\eta_{ja}} \tilde{\theta}_{jb}^{T}\dot{\hat{\theta}}_{k} - \frac{1}{\eta_{ja}} \tilde{\theta}_{jb}^{T}\dot{\hat{\theta}}_{k} - \frac{1}{\eta_{ja}} \tilde{\theta}_{jb}^{T}\dot{\hat{\theta}}_{k} - \frac{1}{\eta_{ja}} \tilde{\
$$

*f j*

Applying equation (13) and assumption 2,  
\n
$$
\dot{V}_j = -m_j \sigma_j^2 + \sigma_j^T u_{j_c} + \sigma_j^T u_{j_a} + \sigma_j^T (-\varepsilon_{j_m} \ddot{x}_{j_{eq}} - \varepsilon_{j_c} \dot{x}_{j_{eq}} - \varepsilon_{j_s} - \varepsilon_{j_s} - \varepsilon_{j_c} - \varepsilon_{j_b} - \varepsilon_{j}
$$
\n
$$
\leq -m_j \sigma_j^2 + \sigma_j^T u_{j_c} + \sigma_j^T u_{j_a} + |\sigma_j^T| (\varepsilon_{j_m} || \ddot{x}_{j_{eq}}| + |\varepsilon_{j_c} || \dot{x}_{j_{eq}}| + |\varepsilon_{j_s}| + |\varepsilon_{j_s}| + |\varepsilon_{j_{fc}}| + |\varepsilon_{j_0}|)
$$
\n
$$
\leq -m_j \sigma_j^2 + \sigma_j^T u_{j_c} + |\sigma_j^T| (d_{j_m} || \ddot{x}_{j_{eq}}| + d_{j_c} || \dot{x}_{j_{eq}}| + d_{j_s} + d_{j_s} + d_{j_t} - d_{j_t})
$$

Substituting equation (12-b) into inequation, it is easy to obtain  $\dot{V}_j \leq -m_j \sigma_j^2$ ,  $\dot{V} = \sum_{j=1}^n \dot{V}_j \leq \sum_{j=1}^n -m_j \sigma_j^2$ Ξ  $=\sum_{i=1}^{n}V_i \leq \sum_{i=1}^{n}$  $\sum_{j=1}^{j} - m_j \sigma_j^2$ *n j*  $\hat{V} = \sum \hat{V}$ 1 2 1  $\dot{V} = \sum_{i=1}^{n} \dot{V}_{i} \leq \sum_{i=1}^{n} -m_{i} \sigma_{i}^{2}$ . Because  $\int_0^{\infty} \sum_{j=1}^{n} m_j \sigma_j^2 \leq -\int_0^{\infty} V dt = V(0) - V(\infty) < \infty$  $0 \t 1 \t 0$  $\sum_{i=1}^{n} m_i \sigma_i^2 \leq -\int_{0}^{\infty} \dot{V} dt = V(0) - V(\infty)$  $\sum_{j=1}^{\infty} m_j \sigma_j^2 \leq -\int_0^{\infty} \dot{V} dt = V(0) - V(\infty) < \infty$ 

so  $\sigma_j \in L_2$ . By equation (11) may be known  $\dot{\sigma}_j \in L_{\infty}$  . According to Babalat lemma [22] ,

 $\lim_{t\to\infty}\sigma_i(t) = 0$ , so theorem is proved.

#### **3.2.3 Simulation results**

The designed impedance controller is applied to 2-DOF

reconfigurable manipulator in the Figure 2(a). The desired force is  $f_d = (1 + \sin t)N$ , the desired trajectory is  $y_a = 0.5 \sin t$ . The simulation results under the proposed soft sensor and the observer are depicted in Figures 6.



**Figure 6.** Force and position tracking of the impedance controller for 2-DOF planar manipulator

For the 3-DOF reconfigurable manipulator in the Figure 2 (b), the desired trajectories are  $x_d = \sin(t)$ and  $y_d = \cos(t)$ , the contact force is defined by  $f_d = (1 + \sin t)N$ . The simulation results are shown in Figure 7.



(b) Z direction force tracking **Figure 7.** Force and position tracking of the impedance controller for 3-DOF manipulator

Time(sec

 $10$ 

 $\overline{0}$ 

Together with the tracking responses of Figures 6 and 7, it is observed that because proposed impedance inner loop control method is adaptive to adjust the parameters in equation (13), so the simulation accuracy of the proposed soft sensor method is better than the observer method. The fuzzy adjusting scaling factor and the predicting reference trajectory are suitable for the situations where the contact stiffness is unknown, and the smooth transition from free space to constrained space can also be realized.

## **3.3 Comparison between soft sensor method and observer force estimation method**

Under the condition of that the wrist force sensor is not installed in the end of the manipulator, hybrid force/position controller based on RBFNN and impedance inner/force outer loop controller based on the fuzzy system can estimate the end contact force of reconfigurable manipulator. The two proposed methods are compared with the force estimation method based on the observer in the reference [15]( Some briefed details in reference  $[15]$  refers to Appendix III), the error comparison of the 2-DOF planar reconfigurable manipulator under the two methods is shown in Table 1, and the error comparison of the 3-DOF reconfigurable manipulator under the two methods is shown in Table 2.

**Table 1.** Error comparison of 2-DOF planar reconfigurable manipulator

error	Method 1	Method 2	Reference [15]
Position error	0.8932	0.6271	1.5214
force error	1.5543	0.3946	5.5298

**Table 2.** Error comparison of 3-DOF planar reconfigurable manipulator



From the comparison of the above two tables, we can see that because of the lack of knowledge about the subsystem dynamics model in the initial stage of the observer, and the parameters of the soft sensor model are adjusted in real time according to the force error and the position error, so the position error and force error of the soft sensor force estimation method are better than the observer force estimation method.

## 4 Conclusions

In this paper, under the condition of reconfigurable manipulator is not installed with the wrist force sensor, two soft sensor models are established in this paper to estimate the contact force, and do not need to know the exact relationship between the contact force and the auxiliary variable. The adaptive laws of all parameters are presented. In the control process, each parameter can be adjusted timely according to the position error and force error, so as to achieve better position and force tracking performance compared with the observer. In practical application, the soft sensor method can effectively solve the problems that wrist force sensor of reconfigurable manipulator is expensive and easy to damage.

Further research works include the following aspects.

The first one is that the proposed soft sensor method will be extended to the underlying systems with the actuator faults. The key factors affecting the actuator fault are found, and the soft sensor method is used to estimate the actuator fault in real time. Second, the distributed force/position control of reconfigurable manipulator will be studied and compared with the existing decentralized control results. Sliding mode technique has a strong robustness for external disturbances of the systems, so using sliding mode technology to improve the force/position control robustness for reconfigurable manipulator could be three interesting issue. In practical applications, if the actuator is saturated, the position error and force error will be inaccurate, which will directly lead to the deviation of position and force estimation results. Therefore, the actuator saturation problem for reconfigurable manipulator will be also the key research problem in the future.

### Declaration of conflicting interests

The author(s) declared no potential conflicts of interest with respect to the research, authorship and/or publication of this article.

## Funding

This work was supported by the National Natural Science Foundation of China (61300098).

### References

- 1. Neranon P, Bicker R. Force/Position control of robot manipulator for human-robot interaction. Thermal Science 2016; 20:537-548.
- 2. Zhou D S, Ji L, Zhang Q, et al. Practical analytical inverse kinematic approach for 7-DOF space manipulators with joint and attitude limits. Intelligent Service Robotics 2015;8(4): 215-224.
- 3. Naveen K, Vikas P. Neural network based hybrid force/position control for robot manipulators. International Journal of Precision Engineering and Manufacturing 2011; 12(3): 419-426.
- 4. Y Wang , H Shen , HR Karimi , et al. dissipativity-based fuzzy integral sliding mode

control of continuous-time t-s fuzzy systems. IEEE Transactions on Fuzzy Systems ,2017, PP (99) :1-12.

- 5. Kumar S,Rastogi V and Gupta P. A hybrid impedance control scheme for underwater welding robots with a passive foundation in the controller domain. Simulation 2017;93(7):619-630.
- 6. Boaventura T, Buchli J, Semini C,et al. Model-Based Hydraulic Impedance Control for Dynamic Robots. IEEE Transactions on Robotics 2015; 31 (6):1324-1336.
- 7. Zhang T, Jiang L,Fan S,et al. Development and experimental evaluation of multi-fingered robot hand with adaptive impedance control for unknown environment grasping. Robotica 2016; 34(5):1168-1185.
- 8. Isela B, Fernando R, Marco M, et al. A Dynamic-compensation Approach to Impedance Control of Robot Manipulators. J Intell Robot Syst 2011;63(1):51-73.
- 9. Parra-Vega V, Arteaga MA . Observer-based sliding mode impedance control of bilateral teleoperation under constant unknown time delay. Robotics and Autonomous Systems 2007;55 (8):  $609 - 617.$
- 10. Jhan ZY , CH Lee. Adaptive Impedance Force Controller Design for Robot Manipulator including Actuator Dynamics. International Journal of Fuzzy Systems 2017 ;3:1-11.
- 11. Colome A, Pardo D, Alenya G,et al. External force estimation during compliant robot manipulation.Robotics and Automation. IEEE Computer Press 2013; 3535-3540.
- 12. Qin J, Leonard F, Abba G.Experimental external force estimation using a non-linear observer for 6 axes flexible joint industrial manipulators. In: Control Conference (ASCC), 2013 9th Asian, Istanbul, Turkey, 23-26 June 2013, pp. 1-6.
- 13. Wang LJ, Meng B. Distributed Force/Position Consensus Tracking of Networked Robotic Manipulators.IEEE/CAA Journal of Automatica Sinica 2014;2:180-186.
- 14. Chan LP, Fazel Naghdy, David Stirling. Extended active observer for force estimation and disturbance rejection of robotic manipulators. Robotics and Autonomous Systems

2013;61(12):1277-1287.

- 15. Du YL. Research on Decentralized Control and Active Fault Tolerant Control for Reconfigurable Manipulator. PhD Thesis, Jilin University, China,2014.
- 16. Wu R, Wu YX, Zhang ZW, et al. A Large-Scale Multibody Manipulator Soft Sensor Model and Experiment Validation. Journal of Robotics 2014:1-8.
- 17. Cho H, Lee H, Kim Y, et al. Design of an optical soft sensor for measuring fingertip force and contact recognition. International Journal of Control Automation & Systems 2017;15(1):1-9.
- 18. Hammond FL , Kramer RK , Qian W , et al. Soft Tactile Sensor Arrays for Force Feedback in Micromanipulation. IEEE Sensors Journal 2014; 14(5):1443-1452.
- 19. Yang H, Chen Y, Sun Y, et al. A novel pneumatic soft sensor for measuring contact force and curvature of a soft gripper. Automatica 2017;12(1):851-862.
- 20. Chen HP, Liu Y.Robotic assembly automation using robust compliant control.Robotics and Computer-Integrated Manufacturing 2013;29 (2):293–300.
- 21. Li YM, Tong SC, Li TS. Adaptive fuzzy output feedback control for a single-link flexible robot manipulator driven DC motor via backstepping. Nonlinear Analysis: Real World Applications 2013; 14 (1): 483-494.
- 22. Kassem AM. Robust voltage control of a standalone wind energy conversion system based on functional model predictive approach. Electrical Power and Energy Systems 2012;41(1): 124-132.
- 23. J Qiu , Y Wei , HR Karimi , et al.Reliable Control of Discrete-Time Piecewise-Affine Time-Delay Systems via Output Feedback. IEEE Transactions on Reliability , 2017 , PP (99) :1-13.
- 24. Y Wei , J Qiu , HR Karimi.Reliable Output Feedback Control of Discrete-Time Fuzzy Affine Systems With Actuator Faults. IEEE Transactions on Circuits & Systems I Regular Papers, 2017 , 64 (1) :170-181.

**Appendix I.** Internal structure of RBF neural network for

estimating contact force

The network is composed of the input layer, the hidden layer and the output layer. It contains 3 input nodes, 5 hidden layer nodes, and 1 output nodes.

The first layer: The input layer. The number of input nodes is the number of input variables.

$$
f_1(i) = X = [x, \dot{x}, |s|]^T
$$

In the formula,  $i=3$  is the number of input variables, and  $x$  is the position component, which is the absolute value of the difference between the position component and its desired value.

Second layer: Hidden layer. The radial basis vector of

RBF is 
$$
\xi_{fc}(j) = [h_1, h_2, h_3, h_4, h_5]^T
$$
,

 $h_j$  ( $j = 1,2 \cdots 5$ ) is a Gauss basis function.

$$
\xi_{fc}(j) = exp(-\frac{(X - c_j)^2}{(b_j)^2})
$$

In the formula,  $C_j$  is the central vector of the *j* node in the

hidden layer,  $c_j = [c_{j1}, c_{j2}, c_{j3}]^T$ ;  $b_j$  is the width vector of the *j* node of the hidden layer, and the two can all be adjusted according to the adaptive law.

The third layer: The output layer.

$$
\hat{F}_c = \hat{W}_{fc}^T \xi_{fc}(j)
$$

where  $\hat{W}_{fc}$  is the weight vector from the hidden layer to the output layer, which can be adjusted according to the adaptive law.

**Appendix II.** Membership function of fuzzy system for estimating contact force

According to each input of the contact force soft sensor model, the membership function is selected as follows:

$$
\mu_{F_1} = \exp(\frac{-(x+2)^{x_1}}{0.2831}), \mu_{F_2} = \exp(\frac{-(x+1.3333)^{x_2}}{0.2831})
$$
\n
$$
\mu_{F_3} = \exp(\frac{-(x+0.6667)^{x_2}}{0.2831}), \quad \mu_{F_4} = \exp(\frac{-x^{x_2}}{0.2831})
$$
\n
$$
\mu_{F_5} = \exp(\frac{-(x-0.6667)^{x_2}}{0.2831}), \quad \mu_{F_6} = \exp(\frac{-(x-1.3333)^{x_2}}{0.2831})
$$
\n
$$
\mu_{F_7} = \exp(\frac{-(x-2)^{x_2}}{0.2831})
$$

The central averaging method is adopted for the defuzzification method.

#### **Appendix III.** Some briefed details in reference [15]

In contact with the environment, the dynamic model of the reconfigurable manipulator is as is like equation (1).

The overall block diagram of the control system is as follows:



#### **Figure 8.** The overall block diagram of the control system

 Each joint is regarded as a subsystem, and the dynamic model of each joint subsystem is

$$
M_i(q_i)\ddot{q}_i + C_i(q_i, \dot{q}_i)\dot{q}_i + G_i(q_i) +
$$
  
\n
$$
Z_i(q, \dot{q}, \ddot{q}) + \tau_{ji} + \tau_{ei} = \tau_i
$$
 (14)

where

$$
Z_i(q,\dot{q},\ddot{q}) = \left\{ \sum_{j=1,\,j\neq i}^n M_{ij}(q)\ddot{q}_j + [M_{ii}(q) - M_i(q_i)]\ddot{q}_i \right\}
$$
  
+ 
$$
\left\{ \sum_{j=1,\,j\neq i}^n C_{ij}(q,\dot{q})\dot{q}_j + [C_{ii}(q,\dot{q}) - C_i(q_i,\dot{q}_i)]\dot{q}_i \right\}
$$
  
+ 
$$
[ \overline{G}_i(q) - G_i(q_i)]
$$

 As the subsystem has unmodeled dynamics, the equation (14) is rewritten as

$$
(M_{i0} + \Delta M_{i0})\ddot{q}_i + (C_{i0} + \Delta C_{i0})\dot{q}_i + G_{i0} + \Delta G_{i0} + Z_i + \tau_{i0} + \tau_{ci} = \tau_i
$$
\n(15)

where  $M_{i0}$ ,  $C_{i0}$ ,  $G_{i0}$ are the nominal parts, and

 $\Delta M_{i0}, \Delta C_{i0}, \Delta G_{i0}$  are the uncertain parts.

The equation (15) is

$$
M_{i0}\ddot{q}_i + C_{i0}\dot{q}_i + G_{i0} + h_i(q, \dot{q}, \ddot{q}) + \tau_{ci} = \tau_i \tag{16}
$$

where

$$
h_i(q, \dot{q}, \ddot{q}) = \Delta M_{i0} \ddot{q}_i + \Delta C_{i0} \dot{q}_i + \Delta G_{i0} + Z_i + \tau_{fi}
$$

A nonlinear joint torque observer is designed for equation (16).

$$
\dot{\hat{\tau}}_i = -l_i \hat{\tau}_i + l_i (M_{i0} \ddot{q}_i + C_{i0} \dot{q}_i + G_{i0} + \hat{h}_i (q, \dot{q}, \ddot{q}) + \tau_{ci})
$$
 (17)

where  $l_i$  is the undetermined coefficient,  $\hat{h}_i(q, \dot{q}, \ddot{q})$  is

the estimated value of  $h_i(q, \dot{q}, \ddot{q})$ .

As the acceleration term appears in the torque observer, it is generally unknown, so an auxiliary variable is introduced to improve the observer.

The auxiliary variable is defined as follows:

$$
d_i = \hat{\tau}_i - b_i \tag{18}
$$

where  $l_i = a_i^{-1} M_{i0}^{-1}$ 0  $-1$   $\mathbf{M}$  –  $l_i = a_i^{-1} M_{i0}^{-1}$ ,  $b_i = l_i M_{i0}(q_i) \dot{q}_i = a_i^{-1} \dot{q}_i$  $\mathbf 0$  $=$   $l_i M_{i0}(q_i) \dot{q}_i = a_i^{-1} \dot{q}_i$ ,

 $a_i$  is a constant.

Differentiating  $\sigma_j$  with respect to time, we have

$$
\dot{d}_{i} = \dot{\hat{\tau}}_{i} - \dot{b}_{i} = \dot{\hat{\tau}}_{i} - l_{i} M_{i0}(q_{i}) \ddot{q}_{i}
$$
\n
$$
= -l_{i} \hat{\tau}_{i} + l_{i} (C_{i0} \dot{q}_{i} + G_{i0} + \hat{h}_{i} (q, \dot{q}, \ddot{q}) + \tau_{ci})
$$
\n
$$
= -l_{i} (d_{i} + b_{i}) + l_{i} (C_{i0} \dot{q}_{i} + G_{i0} + \hat{h}_{i} (q, \dot{q}, \ddot{q}) + \tau_{ci})
$$
\n
$$
= -l_{i} d_{i} + l_{i} (C_{i0} \dot{q}_{i} + G_{i0} + \hat{h}_{i} (q, \dot{q}, \ddot{q}) + \tau_{ci} - b_{i})
$$

Improved torque observer is

$$
\begin{cases}\n\dot{d}_i = -l_i d_i + l_i (C_{i0} \dot{q}_i + G_{i0} + \hat{h}_i (q, \dot{q}, \ddot{q}) + \tau_{ci} - b_i) \\
\hat{\tau}_i = d_i + b_i \\
b_i = l_i M_{i0} (q_i) \dot{q}_i\n\end{cases}
$$
\n(19)

Under the premise of the observation error is uniformly ultimately bounded in the equation (19), the Jacobian matrix can realize the conversion between the force and torque, and finally get the end contact force of the reconfigurable manipulator.