ON POLYMORPHIC LOGICAL GATES IN SUB-EXCITABLE CHEMICAL MEDIUM

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In a sub-excitable light-sensitive Belousov-Zhabotinsky (BZ) chemical medium an asymmetric disturbance causes the formation of localized traveling wave-fragments. Under the right conditions these wave-fragment can conserve their shape and velocity vectors for extended time periods. The size and life span of a fragment depend on the illumination level of the medium. When two or more wave-fragments collide they annihilate or merge into a new wave-fragment. In computer simulations based on the Oregonator model we demonstrate that the outcomes of inter-fragment collisions can be controlled by varying the illumination level applied to the medium. We interpret these wave-fragments as values of Boolean variables and design collision-based polymorphic logical gates. The gate implements operation XNOR for low illumination, and it acts as NOR gate for high illumination. As a NOR gate is a universal gate then we are able to demonstrate that a simulated light sensitive BZ medium exhibits computational universality.

Keywords: Belousov-Zhabotinsky, logical gates, polymorphic gates

1. Introduction

Designing of logical gates in chemical systems can be traced back to early 1990s. Hjemfelft and colleagues suggested a theoretical coupled mass flow system for implementing logic gates and finite-state machines[Hjelmfelt et al, 1991], [Hjelmfelt et al, 1992], [Hjelmfelt & Ross, 1993], [Hjelmfelt et al, 1993], [Hjelmfelt & Ross, 1995] and Lebender and Schneider described approaches towards building logical gates using a series of flow rate coupled continuous stirred tank reactors and a bistable chemical reaction[Lebender & Schneider, 1994]. No experimental prototypes were implemented at that time.

In 1994 Tóth, Showalter and Steinbock presented the first ever experimental implementation of logical gates in the Belousov-Zhabotinsky system[Tóth et al, 1994], [Tóth & Showalter, 1995]. Their constructs of logical gates were based on the configuration of excitation wave propagation channels and the ratio between channel diameter and the critical nucleation radii of the excitable media. Their findings aroused great interest and resulted in several innovative designs of computational devices, including logical gates for Boolean and multiple-valued logic[Sielewiesiuk & Górecki, 2001], [Motoike & Yoshikawa, 2003], [Górecki et al, 2009], [Yamaguchi et al, 2009], many-input logical gates[Górecki & Górecka, 2006], [Górecki & Górecki, 2006], counters[Górecki et al, 2003], coincidence detector[Górecka & Górecki, 2003], detectors of direction and distance[Górecki et al, 2005], [Yoshikawa et al, 2009] and inductive memory[Motoike & Yoshikawa, 2003]. All these chemical computing devices were realised in geometrically-constrained media, where excitation waves propagated along defined channels loaded with catalyst or tubes filled with BZ reagents. The waves perform computation by interacting at the junctions between the channels/tubes. Such an approach is noble, however, it essentially just imitates conventional computing architectures (wires and valves) but using novel materials (excitable chemical systems). Computing in unconstrained media would be a step

forward towards the implementation of massively-parallel chemical processors.

To appreciate the massive-parallelism of a thin-layer chemical media we can adopt the paradigm of collision-based computing [Adamatzky, 2003]. This paradigm originates from the computational universality of the Game of Life [Berlekam et al, 1992], conservative logic and the billiard-ball model [Fredkin & Toffoli, 1982] and their cellular-automaton implementations [Margolus, 1984]. A collision-based computer employs mobile self-localized excitation to represent quanta of information in active non-linear media. Information values, e.g. truth values of logical variables, are given by either the absence or presence of the localizations or by other parameters such as direction or velocity. The localizations travel in space and collide with each other. The results of the collisions are interpreted as computation. There are no predetermined stationary wires, a trajectory of the travelling localization is a momentary wire. Almost any part of the reactor space can be used as a wire. Localizations can collide anywhere within this space. The localizations undergo transformations, form bound states, annihilate or fuse when they interact. Information values of localizations are transformed as a result of these collisions[Adamatzky, 2003].

To implement a collision-based scheme in a spatially-extended chemical medium we must employ travelling localisations. The self-localized excitation wave-fragments, traveling in a light-sensitive BZ medium when it is in a sub-excitable state [Sendiña-Nadal et al, 2001] are ideal candidates. These excitation wave-fragments behave like quasi-particles. They exhibit rich dynamics of collisions, including quasi-reflection, fission, fusion, and annihilation[Adamatzky & De Lacy Costello, 2007], [Toth et al, 2009]. Using the wave-fragments we have implemented collision-based computing schemes [Adamatzky, 2004]. We have produced a range of basic collision-based computing schemes in computer simulations and chemical laboratory experiments including logical gates[Adamatzky, 2004], [Adamatzky & De Lacy Costello, 2007], [Toth et al, 2009], [De Lacy Costello et al, 2009], evolvable chemical logical circuits[Toth et al, 2009], and elements of a one-bit adder[Adamatzky, 2010], [Adamatzky et al, 2010].

All these excitable chemical computing devices are light-sensitive, the wave-fragments grow in size with a decrease in illumination, and the wave-fragments collapse with an increase in illumination. In a very narrow illumination the wave-fragments remain localized and conserve their shape and velocity vectors for a (relatively) significant amount of time. Thus the wave-fragments can be used to represent quanta of information. What happens if the level of illumination is altered between the lower and upper limits of the wave-fragments-stability range? In the present paper we demonstrate that a design can be implemented where the outcomes of collisions between wave-fragments sensitively depend on the level of illumination. A logical function is realised by the collision of wave fragments. By changing the illumination level we are able to change the logical function. Thus we implement BZ collision-based polymorphic logical gates[Stoika et al, 2002], i.e. gates which change their function depending on control signals.

The paper is structured as follows. In Sect. 2 we show how we simulate the light-sensitive Belousov-Zhabotinsky system. Collisions between wave-fragments are studied in Sect. 3. We describe our implementation of collision-based polymorphic logical gates in Sect. 4.

2. Methods

We use the two-variable Oregonator equation [Field & Noyes, 1974] adapted to a light-sensitive Belousov-Zhabotinsky (BZ) reaction with applied illumination [Beato & Engel, 2003]:

$$\frac{\partial u}{\partial t} = \frac{1}{\epsilon} (u - u^2 - (fv + \phi) \frac{u - q}{u + q}) + D_u \nabla^2 u$$

$$\frac{\partial v}{\partial t} = u - v \tag{1}$$

The variables u and v represent the local concentrations of activator, or excitatory component, and inhibitor, or refractory component. Parameter ϵ sets up a ratio of time scale for the variables u and v, q is a scaling parameter dependent on the rates of activation/propagation and inhibition, f is a stoichiometric factor. Constant ϕ is the rate of inhibitor production. In the light-sensitive BZ ϕ represents the rate of inhibitor production which is proportional to the intensity of illumination. We integrate the system using the Euler method with five-node Laplace operator, time step $\Delta t = 0.005$ and grid point spacing $\Delta x = 0.25$,

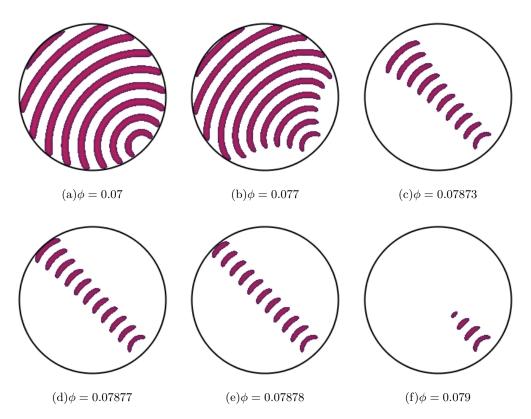


Fig. 1. Showing that the development of the initial excitation is sensitively dependent on the level of illumination ϕ . Excitation is initiated at the south-west edge of the vesicle.

 $\epsilon = 0.022, f = 1.4, q = 0.002$. The equations effectively map the space-time dynamics of excitation in the BZ medium and have proved to be an invaluable tool for studying the dynamics of collisions between travelling localized excitations in our previous work [Adamatzky, 2004], [Adamatzky & De Lacy Costello, 2007], [Toth et al, 2009; De Lacy Costello et al, 2009].

The parameter ϕ characterizes the excitability of the simulated medium. The medium is excitable and exhibits 'classical' target waves, e.g. when $\phi = 0.07$ (Fig. 1a) and the medium is sub-excitable with propagating localizations, or wave-fragments, when ϕ is between 0.07873 and 0.07878 (Fig. 1c-e). The medium becomes non-excitable for $\phi > 0.79$, and after this point wave-fragments collapse after relatively short time scales (Fig. 1f).

When the BZ reaction is in a sub-excitable mode asymmetric perturbations lead to the formation of propagating localized excitation, or excitation wave-fragments. Wave-fragments of this type may travel in a predetermined direction for a finite period of time. If wave-fragments kept their shape indefinitely, we would be able to build a collision-based computing circuit of any size. In reality, the wave-fragments are inherently unstable: after some period of conserved-shape/ distance travelled a wave-fragment either collapses or expands.

Recently [NeuNeu, 2010], [Adamatzky et al, 2010] we found a way to overcome the problem of wavefragment instability via the subdivision of the computing substrate into interconnected compartments, so called BZ-vesicles, and allowing waves to collide only inside the compartments. Each BZ-vesicle has a membrane that is impassable for excitation [Górecki, 2010], [NeuNeu, 2010]. A pore, or a channel, between two vesicles is formed when two vesicles come into direct contact. The pore is small such that when a wave passes through the pore there is insufficient time for the wave to expand or collapse before interacting with other waves entering through adjacent pores, or sites of contact.

A spherical compartment — BZ-vesicle — is the best natural choice as it allows for effortless arrangement of the vesicles into a regular lattice, has an almost unlimited number of input/output states and also loosely conforms to a structure likely to be achieved in experiments involving the encapsulation of excitable 4 Adamatzky, De Lacy Costello, Bull

chemical media in a lipid membrane [Górecki, 2010], [NeuNeu, 2010]. We simulate a vesicle filled with BZ solution as a disc with radius R centered in (x_0, y_0) . Sites inside the disc are excitable, sites outside the disc are not excitable. We imitate wave-fragment entering the vesicle by exciting (assigning values u = 1.) grid nodes inside the small disc with radius r, centered in $(x_0 + (R - s)cos(\theta), y_0 + (R - s)sin(\theta))$. The following parameters are used in the illustrations: $R = 100, r = 5, s = 5, \theta \in [0, 2\pi]$. Time lapse snapshots provided in the paper were recorded at every 150 time steps, and grid sites with excitation level u > 0.04 were displayed.

3. Binary collisions

If two wave-fragments x and y are initiated at the disc's edge at the same time they collide with each other, while approaching the centre of the disc. The outcome of the collision depends on the angle α between the velocity vectors \vec{x} and \vec{y} (Fig. 2). When the angle is less than some critical value β the colliding wave-fragments merge into a new wave-fragment z (Fig. 2b–g) whose velocity vector is positioned exactly between the velocity vectors of wave-fragments x and y: $\vec{z} = (\vec{x} + \vec{y})/2$ (Fig. 2a). When the angle between the vectors of colliding wave-fragments exceeds some critical value β , the colliding wave fragments annihilate (Fig. 2h–s).

Let β be a critical value such that wave-fragments colliding at angle $\alpha \leq \beta$ merge into a wave-fragment, which propagates over an indefinitely long distance, and wave-fragments colliding at angle $\alpha > \beta$ annihilate.

Proposition 1. Critical value β is inversely proportional to illumination level ϕ .

Dependence of β on ϕ calculated in computational experiments is shown in Fig. 3a. The dependence is essentially linear, the deviations shown are due to digitization of the space in numerical experiments. Each critical value β has its own illumination level ϕ , see examples in Fig. 3b–f. Therefore, by varying the illumination of the disc we can alter the outcomes of collisions between wave fragments.

4. Polymorphic gates

We consider two types of gates implemented in BZ-vesicles via the collision of wave-fragments (Fig. 4).

Proposition 2. Let Boolean values of x and y be represented by wave-fragments then a BZ-vesicle implements a two-input three-output switchable logical gate $\langle x, y, \phi \rangle \to \langle x\overline{y}, \chi(\phi)xy, \overline{x}y \rangle$ where $\chi(\phi) = 1$ (True) if $\phi = \phi_{low}$, and 0 (False) otherwise.

Let there be a maximum of two wave-fragments entering a BZ-vesicle. The wave-fragments enter the vesicle along trajectories x and y (Fig. 4a). We assume that presence of a wave-fragment at entry point x represents a logical value TRUE, absence — logical value FALSE. Similarly, if there is a wave-fragment entering BZ-vesicle along trajectory y we assume y=TRUE, otherwise y=FALSE. When just one of the input values is TRUE then the solitary wave-fragment passes through the vesicle without significant modification and exits the vesicle at the site opposite its entry point (Fig. 5a–d, x = 1, y = 0 and x = 0, y = 1). If two wave-fragments enter the vesicle they interact and do not follow their original trajectories. Thus the output trajectories along which the undisturbed wave-fragments x and y move represent functions $x\bar{y}$ and $\bar{x}y$, respectively (Fig. 4a).

Interaction of wave-fragments is determined by level of illumination. When illumination is low enough, say ϕ_{low} , the colliding wave-fragments merge in a new, i.e. travelling along new trajectory, wave-fragment (Fig. 5a and c, x = 1, y = 1). The new wave-fragment exiting the BZ-vesicle represents operation xy (Fig. 4a, left). For higher level of illumination, say ϕ_{high} , the colliding wave-fragments annihilate each other (Fig. 5b and d, x = 1, y = 1), no additional operation is realised.

This is true for wave-fragments colliding at almost any angle over $\pi/6$. However for any particular angle we must select unique values of ϕ_{low} and ϕ_{high} .

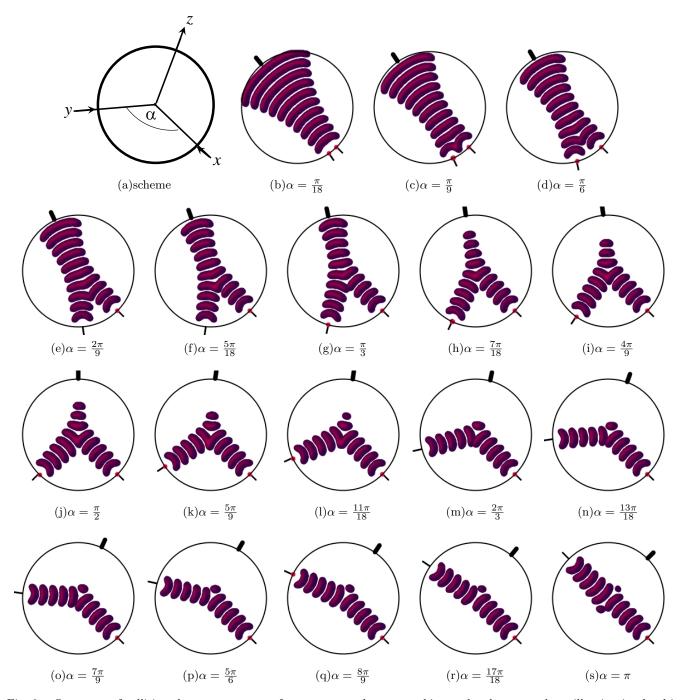
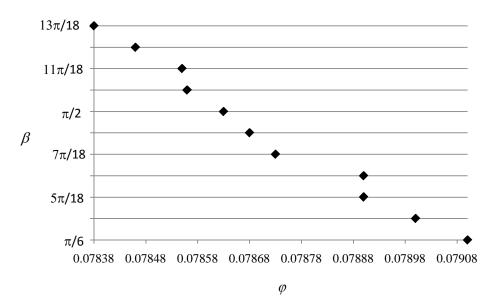


Fig. 2. Outcomes of collisions between two wave-fragments x and y approaching each other at angle α , illumination level is $\phi = 0.07873$; z shows orientation of velocity vector of the resultant wave-fragment, produced in the collision.

Proposition 3. Let Boolean values of x, y and z be represented by wave-fragments then a BZ-vesicle implements a three-input three-output switchable logical gate $\langle x, z, y, \phi \rangle \to \langle x\overline{y}\,\overline{z}, \chi(\phi)z(\overline{x\oplus y}) + \chi(\phi)\overline{x}\,\overline{y}z, \overline{x}y\overline{z} \rangle$ where $\chi(\phi) = 1$ (True) if $\phi = \phi_{low}$, and 0 (False) otherwise.

Outputs presented by trajectories of undisturbed signals $x(y) - x\overline{y}\overline{z}(\overline{x}y\overline{z})$ — are determined as follows. Wave-fragment x(y) continues traveling along its original trajectory only if neither wave-fragment y(x) nor wave-fragment z enter the vesicle (Fig. 4 and Fig. 6a and b, x=1, y=0, z=0 and x=0,y = 1, z = 0).





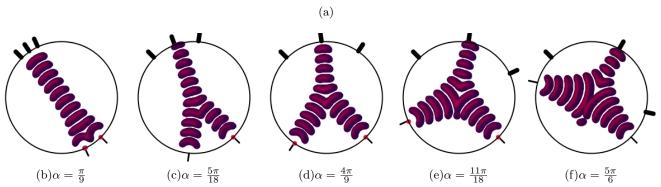


Fig. 3. Level of illumination determines critical angle of wave-fragments collision:(a) dependence of critical collision angle β on illumination parameters ϕ , time lapse snapshots of wave-fragments colliding at angles β for their critical values of illumination ϕ : (b) $\alpha = \frac{\pi}{9}$, $\phi = 0.0791$, (c) $\alpha = \frac{5\pi}{18}$, $\phi = 0.07883$, (d) $\alpha = \frac{4\pi}{9}$, $\phi = 0.07867$, (e) $\alpha = \frac{11\pi}{18}$, $\phi = 0.07850$, (f) $\alpha = \frac{5\pi}{6}$, $\phi = 0.078$.

The following scenarios take place for both low ϕ_{low} and high ϕ_{high} levels of illumination. If only wave-fragment z is present, it travels through the vesicle undisturbed (Fig. 6, x=0, y=0, z=1). When wave-fragment z is present and also either wave-fragment z or z the wave-fragments collide and form a wave-fragment whose velocity vector is an average of the velocity vectors of the colliding wave-fragments. The newly formed wave-fragment collides with the vesicle's wall just between the output channels and misses both of the potential exit points. Thus no output is generated (Fig. 6, z=1, y=0, z=1 and z=0, y=1, z=1).

For two combinations of inputs — x=1,y=1,z=0 and x=1,y=1,z=1 — the outcomes depend on the level of illumination. If only wave-fragments x and y or all three wave-fragments enter the vesicle they collide and annihilate when the level of illumination is high ϕ_{high} (Fig. 6a). The fragments merge and form a new wave-fragment, which hits the output channel thus generating output value True, when the level of illumination is low ϕ_{high} (Fig. 6b). Thus the output channel opposite to the input channel z generates $z(\overline{x} \oplus y)$ when the level of illumination is low, and it generates $\overline{x} \overline{y} z$ when the level of illumination is high.

By assigning constant TRUE to input z, we realize a two-input one-output gate $\langle x, y, \phi \rangle \rightarrow \langle \chi(\phi)z(\overline{x \oplus y}) + \overline{\chi(\phi)}\overline{x}\,\overline{y}z \rangle$. Thus we arrive at the main finding of the current paper:

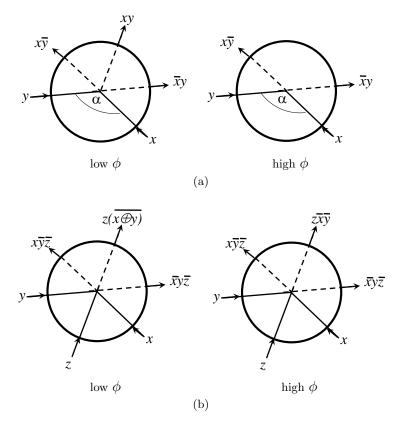


Fig. 4. Two types of logical gates controllable by illumination level ϕ .

gate switchable between functional states XNOR and NOR by changing the degree of illumination.

Conclusion

In a numerical model of the light-sensitive Belousov-Zhabotinsky (BZ) medium in a sub-excitable mode localized traveling excitation waves are formed. We interpreted these localizations as quanta of information, values of logical variables. When two or more localizations collide they annihilate or form a new localization. We interpreted post-collision trajectories of the localizations as the results of a computation. We demonstrated that by colliding wave-fragments in an encapsulated excitable chemical medium we can realise a number of logical gates. We showed that by changing the illumination of the chemical medium we could switch between different outcomes of the computation. Thus we were able to realise a polymorphic logical gate which could execute either function XNOR or NOR depending on the level of illumination. Gate NOR is a universal gate, thus, as a byproduct, we demonstrated the computational universality of the BZ medium when in a subexcitable state.

We would like to outline two main directions of further studies. In the theoretical part, we aim to focus on cascading BZ-based polymorphic gates into larger logical circuits and arithmetic schemes. In experimental part, we aspire to implement theoretical constructs in chemical laboratory experiments.

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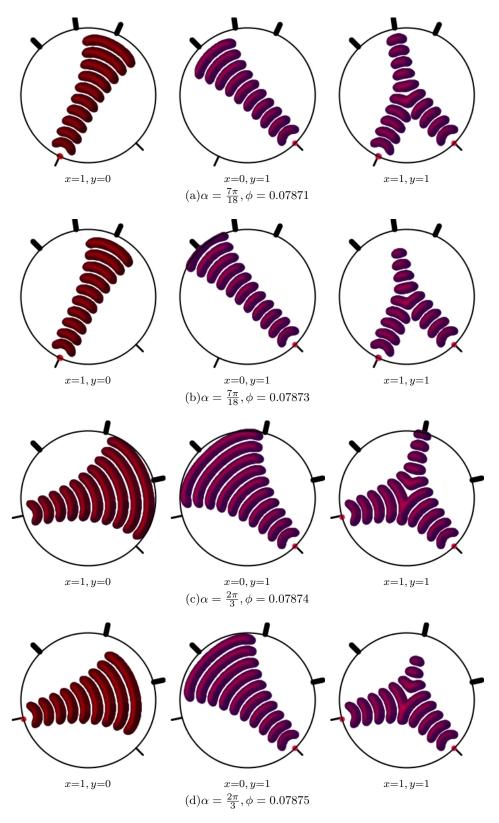


Fig. 5. Implementation of polymorphic gate $\langle x,y,\phi\rangle \to \langle x\overline{y},\chi(\phi)xy,\overline{x}y\rangle$. Scheme of the gate is shown in Fig. 4a. Time lapse snapshots of the sub-excitable media are shown for various illumination levels ϕ and collision angles α . Wave-fragments represent logical values of inputs x and y. Inputs (entry points, pores) are marked by thin lines, outputs (exit points, pores) are marked by thick lines.

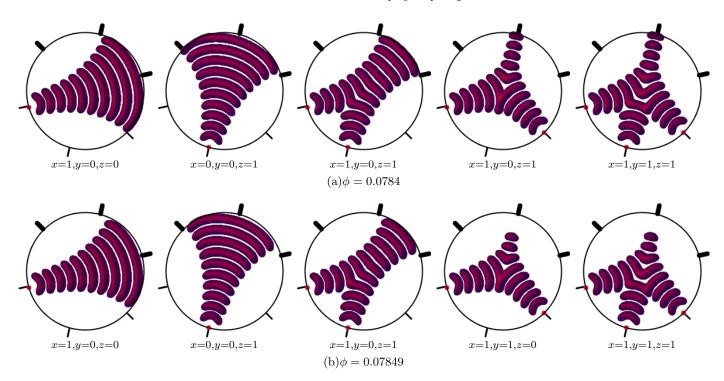


Fig. 6. Implementation of polymorphic gate $\langle x, z, y, \phi \rangle \to \langle x\overline{y}\,\overline{z}, \chi(\phi)z(\overline{x\oplus y}) + \overline{\chi(\phi)}\overline{x}\,\overline{y}z, \overline{x}y\overline{z} \rangle$. Scheme of the gate is shown in Fig. 4b. Time lapse snapshots of sub-excitable medium are shown for various illumination levels ϕ and collision angles α . Waves represent logical values of inputs x and y. Wave-fragments x and z, and z and y collide at angle $\frac{\pi}{6}$; wave-fragments x and y collide at angle $\frac{\pi}{3}$. Inputs (entry points, pores) are marked by thin lines, outputs (exit points, pores) are marked by thick lines.

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