

# An Analytical Framework for High-Speed Hardware Particle Swarm Optimization

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## Abstract

Engineering optimization techniques are computationally intensive and can challenge implementations on tightly-constrained embedded systems. Particle Swarm Optimization (*PSO*) is a well-known bio-inspired algorithm that is adopted in various applications, such as, transportation, robotics, energy, etc. In this paper, a high-speed *PSO* hardware processor is developed with focus on outperforming similar state-of-the-art implementations. In addition, the investigation comprises the development of an analytical framework that captures wide characteristics of optimization algorithm implementations, in hardware and software, using key simple and combined heterogeneous indicators. The framework proposes a combined Optimization Fitness Indicator that can classify the performance of *PSO* implementations when targeting different evaluation functions. The two targeted processing systems are a Field Programmable Gate Arrays for hardware implementations and a high-end multi-core computer for software implementations. The investigation confirms the successful development of a *PSO* processor with appealing performance characteristics that outperforms recently presented implementations. The proposed hardware implementation attains

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23300 improvement ratio of execution times with an elliptic evaluation function. In addition, an speedup of 1777 times is achieved with a Shifted Schwefels function. Indeed, the developed framework successfully classifies *PSO* implementations according to multiple and heterogeneous properties for a variety of benchmark functions.

*Keywords:* Particle Swarm Optimization, Hardware, Software, Performance Indicators, Analysis, Gate Arrays

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## 1. Introduction

Optimization is an important concept in the engineering domain [1, 2, 3, 4]. Indeed, all engineering applications involve some sort of optimization in order to realize the final product. Optimization involves reducing cost, power consumption, time delay or increases the yield, profit, quality of solution, etc. As engineering problems became more challenging; with properties such as large size, discontinuity, non-differentiability, non-linearity, multi-objectiveness, and mixed variable types; it becomes essential to develop new optimization paradigms that can reach acceptable solutions in less time.

Meta-heuristics is a substantial and considerably important optimization paradigm that can be used to tackle nowadays engineering problems. A major class of meta-heuristics is Population-based algorithms, which update a population of solutions over a number of iterations until some stopping condition is satisfied. Population-based algorithms are categorized based on the inspiration behind their population update scheme. These categories include Evolutionary Algorithms and Swarm Intelligence algorithms. Due to the heavy computational workload constituting of optimization with population-based algorithms, computational speed matters for solving many dynamic and real-time problems with Evolutionary Algorithms and Swarm Intelligence algorithms. For example, radio resource scheduling for recent generations of wireless communication networks requires a decision to be made within nano-seconds level, which is not viable with conventional computing infrastructures [5, 6]. Further research has

been conducted over the past two decades in order to speed up the execution of such algorithms, whether by manipulating parameters, developing multiple/dis-  
tributed versions or implementing them on specific hardware.

In this paper, we investigate the implementation of one Swarm Intelligence algorithm, namely Particle Swarm Optimization (*PSO*) [7, 8], on Field Programmable Gate Arrays (*FPGAs*) [9, 10, 11, 12]. The investigation benefits from the advancements in *FPGA* capabilities and aims at developing high-speed hardware cores. Such a hardware implementation enables embedding optimization algorithms in application to assist, or completely replace, a central processing component. The investigation is driven by the need for appealing performance characteristics, and the reliable operation within real-time applications, that hardware implementations can provide. Furthermore, the investigation comprises the development of a statistical analysis framework that captures wide characteristics of optimization computations. The proposed framework statistically combines the mathematical properties of optimization algorithms and their evaluation function complexities, besides, their implementations in *HW* and *SW*. To that end, the developed *PSO* implementations are employed to validate the proposed framework and verify its effectiveness in application. Indeed, limited work in the literature is found to analyze the performance of *PSO* implementations based on heterogeneous properties as in the proposed analysis framework. The general contribution of the paper is summarized as follows; a detailed discussion on the motivation, contributions, and objectives is presented in Section 2:

- Develop efficient hardware cores for the *PSO* algorithm on *FPGAs*.
- Develop an analytical framework that evaluates the fitness of optimization implementations based on heterogeneous performance indicators.

The rest of the paper is organized so that Section 2 present the motivation, research questions, and the paper contribution. In Section 3, a survey of the literature is presented. In Section 4, the processor design and implementation are presented. Section 5 introduces the statistical analysis model. A thorough

performance evaluation is presented in Section 6. Section 7 concludes the paper and sets the ground for future work.

## 55 2. Research Objectives

Challenges to optimization algorithms, including *PSO*, comprise performance characteristics (time, speed, efficiency, and complexity), storage requirements, reliability and accuracy, and first and foremost the dealing with the intrinsic sequential behavior of the algorithm. As related to *PSO*, the following research  
60 opportunities are highlighted:

- Identify and investigate the performance aspects of *SW* implementations of *PSO* while targeting high-performance multi-core processors.
- Develop efficient hardware cores for *PSO* under *FPGAs*.
- Identify and investigate the performance aspects of the *HW* implementa-  
65 tions.
- Identify a set of performance indicators that aids the evaluation of *HW* and *SW PSO* implementations with different benchmark evaluation functions.
- Develop combined performance indicators for *PSO* that capture the qual-  
70 itative and quantitative characteristics, and enables the classification of different implementations based-on combined *HW*, *SW*, and mathematical properties.
- Identify the type of problems that can be efficiently optimized using *PSO* based on heterogeneous *HW*, *SW*, and algorithmic properties.

75 The proposed investigation has several research objectives. The investigation aims at developing a high-speed hardware core for *PSO* on *FPGAs*. To this end, the focus is on outperforming similar state-of-the-art implementations reported in the literature under the same implementation environment, algorithm specifications, and the targeted set of Benchmark Evaluation Functions (*BEFs*).  
80 The hardware development includes the identification of effective implementation specifics and best practices. In addition, the investigation comprises the development of a statistical analysis model that captures wide characteristics of *PSO* implementations in *HW* and *SW*. Accordingly, the investigation includes

the development of high-speed *SW* implementations on high-end multi-core  
85 processors. The analysis model comprises simple and combined performance  
indicators including a main indicator called the Optimization Fitness Indica-  
tor (*OFI*). The developed indicators analyze *PSO* implementations in terms  
of performance, hardware size, throughput, success rate, and combined forms.  
The aim of the *OFI* is to classify the performance of *PSO* implementations  
90 when targeting different *BEFs*. Therefore, the type of problems that can be  
best solved using *PSO* can be identified. The evaluation confirms the success-  
ful implementation of an *FPGA* core for the *PSO* with accelerated processing  
throughput for different *BEFs*. The developed combined indicators successfully  
classified implementations using a variety of benchmark functions according to  
95 desired properties.

In relation to the similar work presented in Section 3, the proposed devel-  
opments enable the following comparisons:

- Compare the performance of partitioned versus nonpartitioned *FPGA*  
100 implementations. The comparison is done between the proposed all-in-  
hardware *FPGA* core with the partitioned implementation in [13]. Given  
that the same implementation environment, algorithm specifications, and  
the targeted set of *BEFs* are adopted in our investigation.
- Compare the performance of the proposed sequential core with parallel  
105 hardware versions of the *PSO*. The comparison includes the parallel-*PSO*  
version in [14] at a swarm population size of 8 particles. Besides, present-  
ing a wider analysis than that presented in [14] to include populations of  
16 and 32 particles. In addition, the comparison includes the multi-swarm  
parallel hardware implementation in [15].
- Present classifications of *PSO* implementations based on heterogeneous  
110 performance characteristics. The classifications enable straightforward  
identifications of the type of problems that can be best solved using a  
*PSO* implementation. Such straightforward identifications are proposed  
to replace tedious, intuitive, and multifaceted evaluations based on several  
single indicators—as usually adopted in the literature [16, 17, 18, 19, 20,  
115 15, 14, 20, 21, 22, 13].

### 3. Related Work

The emergence of high-performance *FPGAs* enabled their use in computationally-intensive applications, such as optimization. Many recent investigations are identified in the literature to target implementing the *PSO* algorithm on *FP-*  
120 *GAs*. In this section, state-of-the-art related work is identified and presented, while closely-related work is thoroughly addressed in Section 6.2. In presenting similar work, we focus on a variety of implementation-specific aspects, such as, target devices, the used metrics to analyze the attained performance, and the main achievement of each investigation. Table 1 accompanies the discussion and  
125 provides a summary of findings.

Several attempts to achieve high processing speeds are presented in the literature [19, 14, 15, 20, 23]. Calazan et al. [14] propose a *HW* implementation of a parallel version of the *PSO* to run on a *Xilinx Virtex-6* as a co-processor. The approach aims to improve the execution of *PSO* so that the performance  
130 can be optimized for solving benchmark problems. The results demonstrate a significant speedup achieved through solving benchmark functions. In addition, Tewelode et al. [23, 20, 15] develop a direct *HW* implementation of *PSO* to solve the problem of emission source localization within the context of environment monitoring in [23], and extended with two more numerical benchmark functions  
135 in [20] to achieve significant speedups. The speedup is studied with respect to execution time as well as the number of cycles, where the level of achievement is clearly indicated. The authors published further details of the study in [15], where parallel *HW* implementations under *Xilinx Spartan 3E FPGA* is compared to *MicroBlaze*-based *SW* implementations.

140 Improving accuracy using hardware implementations is the target of different investigations. Karakuzu et al. [17] present an implementation of neuro-fuzzy system trained with *PSO* to improve the learning and prediction performances. The implementation provides efficiency with avoiding some steps through the process in comparison to using look-up tables (*LUTs*). The proposed approach  
145 and implementation, using *Xilinx Virtex-5*, is tested with two scenario-based

benchmark system identifications and a realistic number-plate recognition. The implemented neuro-fuzzy system model was trained with swarm intelligence algorithms including *ABC* and ordinary *PSO* alongside the proposed *PSO* approach. The proposed *HW* implementation achieves the expected level of solution quality using significantly less *HW* resources. Furthermore, Li et al. [22] introduce a *HW/SW* co-design approach for *PSO* based-on *SOPC* technique and pipeline design, where the algorithm is partitioned between *SW* and *HW* to possibly improve the performance when solving various numerical benchmark functions. The algorithm is partitioned so that the fitness evaluation is developed in *SW*, while particle updating is implemented in *HW* and referred to as Particle Updating Accelerator. The proposed implementation is created to run the *SW* part on a *Nios II CPU*, while the *HW* part to run on a *Cyclone II FPGA*. The results demonstrate that a speedup of 20 times is achieved over a *SW* implementation.

A variety of investigations, on performance evaluation of *PSO* implementations, is presented in the literature. Common investigations include comparing the performance of Genetic Algorithms and *PSO*, optimizing *HW/SW* partitioned implementations, and integrating hardware *PSO* in engineering applications. Ben Ameer and Sakly [16] present parallel *HW* implementations for *PSO* and Genetic Algorithms. The implementations are formulated with finite state machines and target a *Xilinx Spartan-3 FPGA*. The implementations are tested with a number of benchmark functions to compare *PSO* with Genetic Algorithms; the reported results are in favor of the *PSO* algorithm. In addition, Abdelhalim et al. [24] present constrained and unconstrained *HW/SW* partitioning problem with *SW*-based *PSO* implementations. Optimizing the intended system is done using various heuristic algorithms including Genetic Algorithms and *PSO*. The results and comparative analysis suggest that the proposed *PSO*, so-called *Re-exited PSO*, help achieving near-optimum results. The *Re-exited PSO* algorithm is used in [18] to solve partitioning problems for the *JPEG* encoding system introduced by [25]. The developed embedded system is implemented under a *Cyclone FPGA* as the co-processor of a main

*Nios-II CPU*. The results are compared with findings of [25] to demonstrate the success of the proposed approach. The work presented in [26] proposes different approaches to implement *PSO* on *FPGAs*. To this end, the investigation tar-  
180 gets an *FPGA* and an *ARM* processor in a *Xilinx Zynq-7000* system on chip. The analysis includes testing three benchmark functions. Moreover, Ettouil et al. present a *PSO* implementation that targets an extended set of evaluation functions [27]; the investigation includes thorough analyses of hardware area utilization and the attained clock period. Applications of hardware *PSO* include  
185 training neural networks [28], implementing Multiple-Input Multiple-Output (MIMO) detection systems [29], to name but a few.



Table 1: Summary of related works.

| Ref. | Year | Implementation                      | Hardware                        | Metrics  | Main Achievement  |
|------|------|-------------------------------------|---------------------------------|--|---|
| [26] | 2018 | PSO; HW and SW                      | ARM and Xilinx<br>FPGA ZedBoard | Hardware speedup; area utilization;<br>execution time; period              | Improving multiple indicators<br>including hardware speedup per<br>HW/SW implementation |
| [16] | 2017 | PSO and Genetic<br>Algorithms       | Xilinx Spartan-3                | Area   | Small-sized hardware area   |
| [17] | 2016 | Neuro-Fuzzy system<br>with PSO      | Xilinx Virtex-5                 | Precision; accuracy of prediction  | Improved accuracy   |
| [19] | 2014 | PSO                                 | Xilinx Virtex-5                 | Execution time   | High processing speed   |
| [14] | 2014 | Parallel PSO                        | Xilinx Virtex-6                 | Execution time; speedup; area  | High processing speed   |
| [15] | 2012 | Parallel PSO                        | Xilinx Spartan-3                | No. of iterations; execution time  | High processing speed   |
| [18] | 2011 | Re-erited PSO                       | Altera Cyclone                  | Area; delay; power consumption;<br>communication time between HW<br>and SW | Optimizing performance per<br>HW/SW partitions  |
| [22] | 2011 | Core of PSO and<br>other components | Altera Cyclone                  | Execution time; and no. of<br>evaluations                                  | Improved accuracy   |
| [20] | 2009 | PSO                                 | Xilinx Spartan-3                | No. iterations; execution time; clock<br>cycles                            | High processing speed   |
| [23] | 2008 | PSO                                 | Xilinx Spartan-3                | No. Iterations, execution time; clock<br>cycles                            | High processing speed   |
| [24] | 2007 | PSO; HW/SW<br>partitioning          | N/A                             | A developed cost equation that<br>captures result quality; delay; power    | Optimizing result quality per<br>HW/SW Partition  |

#### 4. Hardware Design

An informal and systematic approach is adopted to develop hardware cores for the *PSO* algorithm [1, 30]. The approach is informal in the sense that it does not rely on engineering formal methods [31]. In addition, the approach  
190 does not rely on engineering formal methods [31]. In addition, the approach is systematic in the sense that its procedure can be reused to develop similar hardware solutions, however, the method is not yet automatic and does not include any code generations, compilations, or rapid prototyping of hardware circuits. Furthermore, the methodology is unified in the sense that it uses  
195 common software engineering techniques, such as flowcharts and state machines, to model the algorithm; accordingly, *HW* and *SW* designs are derived and implemented.

The development steps of the *HW* and *SW* implementations of the *PSO* are as follows:

- 200 1. Depict the algorithm using flowcharts.
2. Develop the software version.
3. Design the processor Datapath by identifying, allocating, and binding hardware resources at the register-transfer level [32].
4. Develop the Finite State Machine (*FSM*) of the control unit based on the  
205 flowchart.
5. Describe the developed hardware using a description language and synthesize the implementation for *FPGAs*.

The approach can be used to design partitioned hardware and software implementations of the *PSO* algorithm. However, the current use aims at developing independent hardware implementation for *FPGAs*. The adopted *PSO* is  
210 described in Algorithm 1 in pseudocode.

Figure 1 depicts the abstract behavior of the *PSO* algorithm. The main actions in the algorithm are (i) generate random numbers, (ii) initialize particles positions and velocities, (iii) evaluate a benchmark function to calculate the fitness value of a particle, (iv) update the particle's record with the best fitness  
215 value attained yet, and (v) update the swarm's global record with the best fitness value reached yet. At this point, update the particle's velocity and position with

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**Algorithm 1** The adopted PSO algorithm

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```
1: Initialize particles
2: do
3:   for  $i = 1$  to Number of Particles do
4:     if  $f(x_i) \leq f(p_{best_i})$  then
5:        $p_{best_i} = x_i$ 
6:     if  $f(x_i) \leq f(g_{best})$  then
7:        $g_{best} = x_i$ 
8:     end if
9:   end if
10:  for  $j = 1$  to Number of Dimensions do
11:     $v_{ij}^{t+1} = wv_{ij}^t + c_1r_1(p_{best_{ij}}^t - x_{ij}^t) + c_2r_2(g_{best_j} - x_{ij}^t)$  (1)
12:    if  $v_{ij}^{t+1} > v_{max}$  then
13:       $v_{ij}^{t+1} = v_{max}$ 
14:    end if
15:    if  $v_{ij}^{t+1} < v_{min}$  then
16:       $v_{ij}^{t+1} = v_{min}$ 
17:    end if
18:     $x_{ij}^{t+1} = x_{ij}^t + v_{ij}^{t+1}$  (2)
19:    if  $x_{ij}^{t+1} > x_{max}$  then
20:       $x_{ij}^{t+1} = x_{max}$ 
21:       $v_{ij}^t = 0$ 
22:    end if
23:    if  $x_{ij}^{t+1} < x_{min}$  then
24:       $x_{ij}^{t+1} = x_{min}$ 
25:       $v_{ij}^t = 0$ 
26:    end if
27:  end for
28: end for
29: while maximum iterations or minimum error is not reached
30:
31: where,
32:  $c_1$  and  $c_2$  are the acceleration constants.
33:  $r_1$  and  $r_2$  are random numbers between 0 and 1.
34:  $x_i(t)$  is the position of the  $i^{th}$  particle at iteration  $t$ .
35:  $v_i(t)$  is the velocity of the  $i^{th}$  particle at iteration  $t$ .
36:  $w$  is the inertia weight factor.
37:  $g_{best}$  is the best position among all particles.
38:  $p_{best_i}$  is the  $i_{th}$  particle best position.
39: Equation (1) is the velocity update of the  $i^{th}$  particle.
40: Equation (2) is for position update of the  $i^{th}$  particle.
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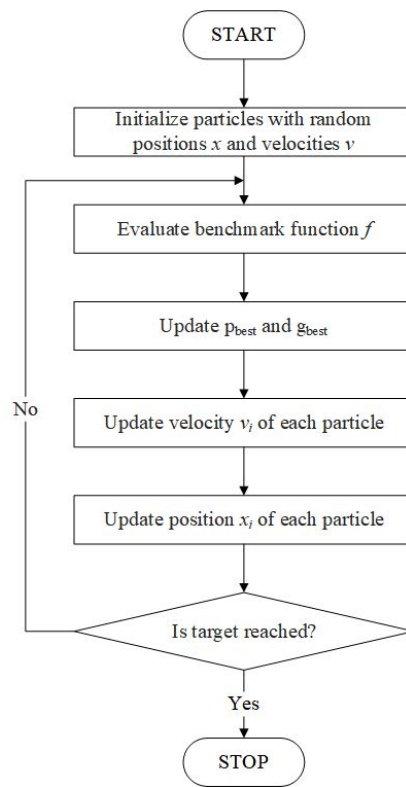


Figure 1: An abstract flowchart for the *PSO* algorithm

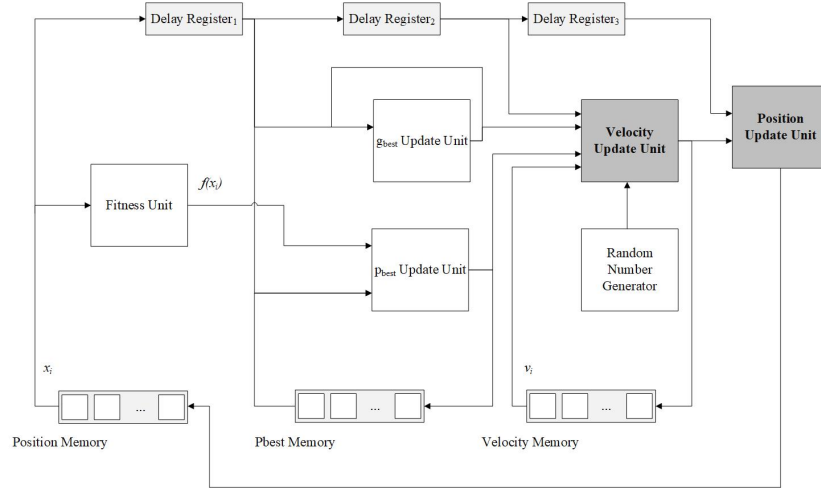


Figure 2: The developed datapath for the *PSO* algorithm

newly calculated values plays the main role. The procedure is repeated until a target number of iterations or a minimum error value is reached.

220 Based on to the *PSO* algorithm description, the datapath development includes the allocation of several computational hardware resources (See Figure 2). The main allocated hardware units are a Fitness unit,  $p_{best}$  Update unit,  $g_{best}$  Update unit, Velocity Update unit, Position Update unit, Random Number Generator (*RNG*), and three delay registers for the particle position  $x$ . Sample internal organizations of *PSO* computational units are shown in Figures 3 and 4. In Figure 3, the hardware structure is for the Velocity Update Unit, while Figure 4 presents a Fitness Unit depicting the Rosenbrock function. In both figures, the computational components run in parallel. Moreover, Figure 2 includes standard components, such as, registers and memory elements; 225 the units Position, Global, and Particle Updates are implemented using simple selection statements, variable assignments, or include a single operation. In the presented datapath, the Random Number Generator core is imported from the work presented in [33].

230 The behavior of the processor control unit is described in the *FSM* shown in Figure 5. States  $S_0$  through  $S_6$  are responsible for the position and velocity

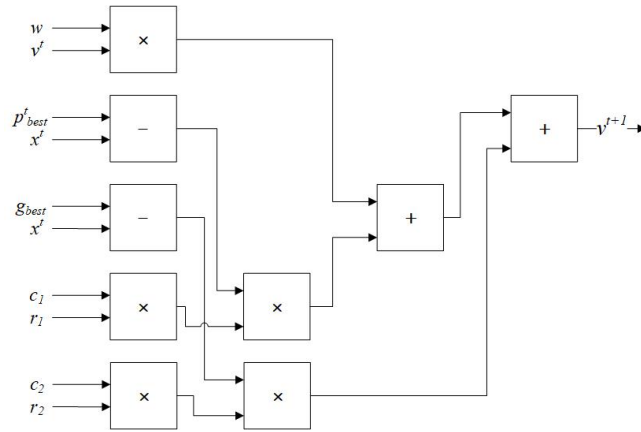


Figure 3: The hardware structure of the Velocity Update Unit

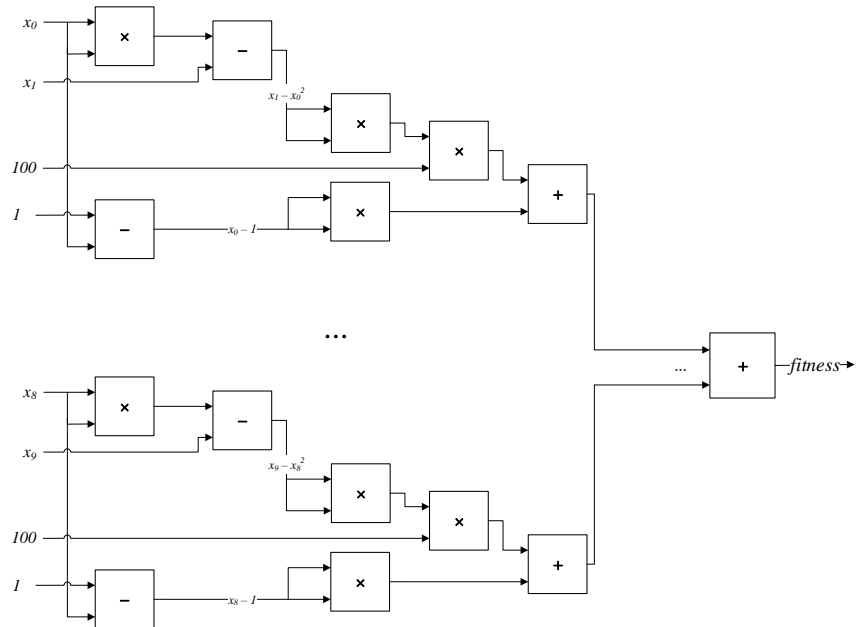


Figure 4: The hardware structure of the Fitness Unit depicting a Rosenbrock function.

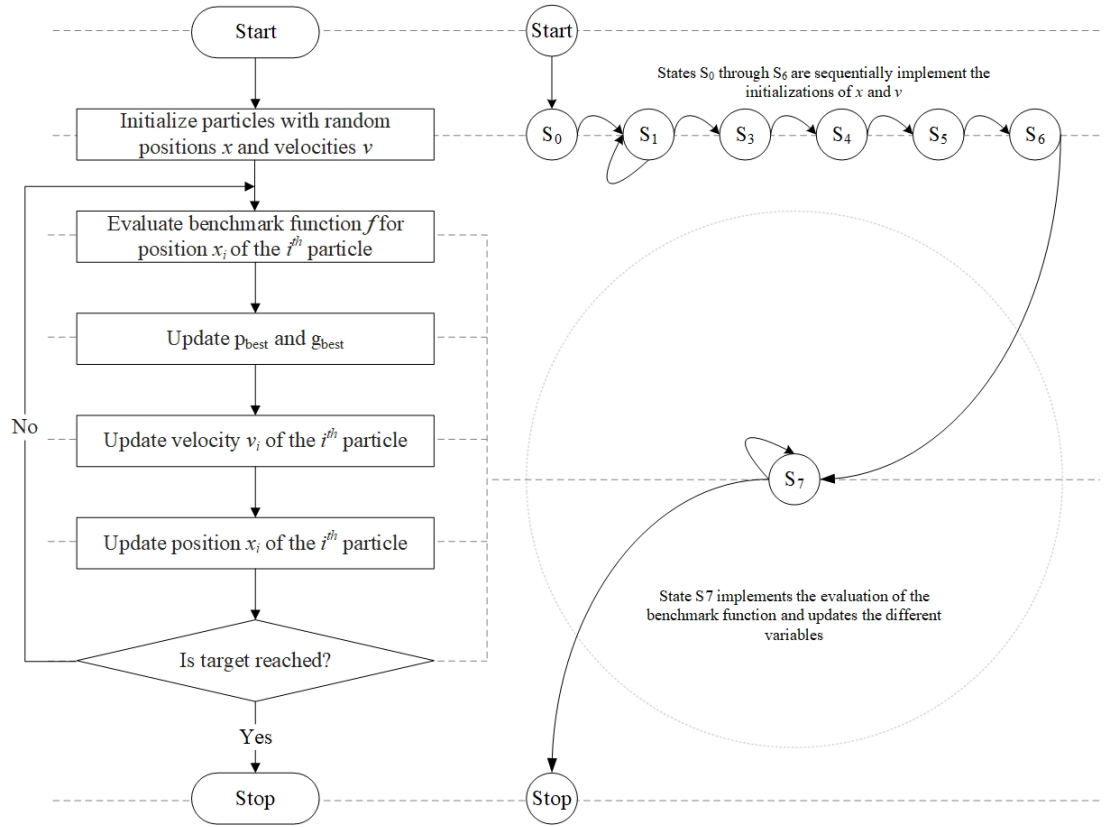


Figure 5: The developed *FSM* of the *PSO* Algorithm and its correspondence to the flowchart steps.

initialization of particles, preparation for the random number generation, and the forwarding of the position values through the three delay registers. State  $S_7$  is the main execution procedure that includes benchmark function evaluation, best positions updates, and velocity and position updates. In addition, state  $S_7$  repeats unit the stoppage criterion is satisfied.

## 5. Analytical Model Development

To present the proposed performance analysis model, we adopt the Generic Benchmark Model (*GBM*) of Damaj et al. [34]. The *GBM* comprises six elements that define the Goal, Inputs, Activities, Output, Outcomes, and the

245 desired Performance profile of the performance analysis framework. The model captures the relationships among the resources, implementation, mathematical formulation, and the obtained results. The Goal defines the aim of the analysis framework. Moreover, the Input identifies the algorithms under study, implementation environments, reference algorithm, performance metrics, etc. Furthermore, Activities present the algorithm implementations and the obtained 250 results. The Output is the formulation of the key indicators and development of their rubrics—if needed. The Outcomes are the formulations of the statistical assessment as combinations of the Output. In addition, the Performance is the application of the developed assessment framework to profile and classify 255 algorithms according to the obtained results.

### 5.1. Goal

Analyze the performance of a *PSO* implementations in *HW* and *SW*, and enable its comparison to similar work in the literature.

### 5.2. Input

260 The input identifies the targeted algorithms, computing systems, and the performance metrics. The analysis model targets a set of benchmark evaluation functions of different complexities and characteristics (See Tables 2 and 3). Moreover, the targeted *HW* development board is the DE2-70 by *Altera*. The board has a *Cyclone II FPGA* with a total of 68,416 Logic Elements (LEs) and a maximum frequency of 300 MHz. *SW* implementations are done on *Dell Precision T7500* with its dual quad-core *Xeon* processors and 24 GB of *RAM*. 265

The identified performance metrics of the *PSO* are classified into general algorithmic profile (*GAP*), hardware profile (*HWP*), and software profile (*SWP*). The general algorithmic profile includes the complexity of the benchmark evaluation functions. The *HWP* includes the number of benchmark evaluations, 270 resource utilization, maximum frequency, throughput, etc. Moreover, the *SWP* comprises the number of benchmark evaluations, throughput, execution time, etc.



Table 2: The targeted Benchmark Evaluation Functions.

| <b>BEF Index</b> | <b>Function</b>                           | <b>Variable No.</b> | <b>Search Domain</b> | <b>Optimal Solution</b> |
|------------------|---|---------------------|----------------------|-------------------------|
| F1               | B2  | 2                   | [-100, 100]          | 0                       |
| F2               | Branin                                    | 2                   | [-4, 4]              | 0.397887                |
| F3               | Goldstein-Price                           | 2                   | [-2, 2]              | 3                       |
| F4               | Rosenbrock                                | 2                   | [-9, 11]             | 0                       |
| F5               | Zakharov                                  | 2                   | [-10, 10]            | 0                       |
| F6               | Sphere                                    | 3                   | [-5.12, 5.12]        | 0                       |
| F7               | Hartmann                                  | 3                   | [0, 1]               | -3.863433               |
| F8               | Variably-dimensioned                      | 4                   | [-9, 11]             | 0                       |
| F9               | Shifted Sphere                            | 32                  | [-100, 100]          | 0                       |
| F10              | Shifted Rosenbrock                        | 32                  | [-100, 100]          | 0                       |
| F11              | Shifted Schwefel 1.2                      | 32                  | [-100, 100]          | 0                       |
| F12              | Shifted Rastrigin                         | 32                  | [-100, 100]          | 0                       |
| F13              | Shifted Rotated High Conditioned Elliptic | 32                  | [-100, 100]          | 0                       |

Table 3: Properties of the target Benchmark Evaluation Functions in terms of separability, scalability, and whether the function is unimodal or multimodal.

| <b>BEF Index</b> | <b>Function</b>                           | <b>Separable</b> | <b>Scalable</b> | <b>Unimodal</b> |
|------------------|---|------------------|-----------------|-----------------|
| F1               | B2  | Yes              | No              | No              |
| F2               | Branin                                    | No               | No              | No              |
| F3               | Goldstein-Price                           | No               | No              | No              |
| F4               | Rosenbrock                                | No               | Yes             | No              |
| F5               | Zakharov                                  | Yes              | Yes             | Yes             |
| F6               | Sphere                                    | Yes              | Yes             | Yes             |
| F7               | Hartmann                                  | No               | No              | No              |
| F8               | Variably-dimensioned                      | Yes              | Yes             | Yes             |
| F9               | Shifted Sphere                            | Yes              | Yes             | Yes             |
| F10              | Shifted Rosenbrock                        | No               | Yes             | Yes             |
| F11              | Shifted Schwefel 1.2                      | No               | Yes             | Yes             |
| F12              | Shifted Rastrigin                         | Yes              | Yes             | No              |
| F13              | Shifted Rotated High Conditioned Elliptic | No               | Yes             | Yes             |

### 5.3. Activities

275 The activities include hardware implementations under *VHDL*. The Software tools used for hardware implementation and profiling are *Quartus* and *ModelSim*. Software implementations are done under *MATLAB*.

### 5.4. Output

280 The outputs of the analysis framework are three sets of indicators that correspond to the proposed *GAP*, *HWP*, and *SWP*. The main *KI* of the *GAP* is the Benchmark Evaluation Function Complexity (*BEFC*), which is defined as follows:

- **Benchmark Evaluation Function Complexity (*BEFC*)**: an asymptotic complexity analysis using the Big- $O$ , small- $\omega$ , and  $\Theta$  notations.

285 To analyze the complexity of the evaluation functions, we study their asymptotic behavior. The asymptotic behavior classifies algorithms according to their rate of growth with respect to the increase in input size. The following standard complexity analysis classification is adopted from [35, 34]:

- $O(f(n))$ : The rate of growth of an algorithm is asymptotically no worse than the function  $f(n)$  but can be equal to it.
- $\omega(f(n))$ : The rate of growth of an algorithm is asymptotically no better than the function  $f(n)$ .
- $\Theta(f(n))$ : The rate of growth of an algorithm is asymptotically equal to the function  $f(n)$ .

295 Here,  $n$  is the size of input.

To facilitate the assessment of the studied ciphers, we adopt the rubric from [34] as shown in Table 4. In preparation for the statistical formulation, we map this qualitative properties onto quantities. For every point in the scale, we map it onto a fixed number. Hence, each point in the scale is mapped onto the values 300 20%, 40%, 60%, 80%, and 100% [34].

The hardware profile includes the following indicators:

Table 4: The rubric of the Complexity Analysis indicator

| General<br>Indicator   | Scale              |   |             |                                   |                          |
|------------------------|--------------------|---|-------------|-----------------------------------|--------------------------|
|                        | Logarithmic<br>Low | Logarithmic<br>High                           | Linear      | Almost<br>Quadratic               | Higher than<br>Quadratic |
| Complexity<br>Analysis | $O(\log n)$        | $\omega(\log n)$ but<br>better than<br>Linear | $\Theta(n)$ | $O(n^2)$ but worse<br>than Linear | $\omega(n^2)$            |

- 305
**Number of Benchmark Function Evaluations (NBFE):** the total number of calls of the benchmark function; equals the number of iterations times the total number of benchmark function calls per iteration. In this investigation, we report the average *NBFE* required for optimizing the benchmark functions.
- Execution Time (ET):** the time between the start and the completion of a task.
- 310
**Throughput (TH):** the total amount of work done in a given time. In this investigation, we calculate *TH* as the *NBFE* divided by *ET*; the results are represented in *Kilo BFE per Seconds (KBFEps)*.
- 315
**Logic Elements (LE):** the number of combinational logic elements required to implement an algorithm in hardware. The number of *LEs* is an indicator of the size of hardware in Altera devices.
- Logic Register (LR):** the total number of logic registers in the design.

The Software profile includes three indicators, namely, *NBFE*, *ET*, and *TH*.

### 5.5. Outcomes

320
 The Outcomes element is the formulation of Combined Measurement Indicators *CMIs* as function of *KIs*. Four *CMIs* are developed to analyze the performance of the *PSO* implementation, namely, **Success Rate (SR)**, **Performance Rate (PR)**, **Success Rate Density (SRD)**, and the **Optimization Fitness Indicator (OFI)**. The definitions of the *SR*, *PR*, and *SRD* are
 325
 as follows:

- SR:** The percentage number of runs that successfully converges to the minimum which is below the specified error divided by the total number of runs.
- PR:** The average *NBFE* divided by the percentage *SR*.

- **SRD**: The number of *LEs* divided by *SR*. *SRD* captures the size of hardware used per 1% *SR*.

The *OFI* is the main *CMI* calculation in the presented statistical analysis model. A higher *OFI* is achieved through a higher throughput, a lower execution time, with less resource utilization, and at a higher performance rate; while targeting the evaluation function with a higher complexity. The combination of indicators is done using the Geometric Mean of *KI* ratios. The generic equation of *CMIs* from [34] is as follows:

$$CMI = \sqrt[n]{ratio_1 \times ratio_2 \times \dots \times ratio_n}$$

340

$$\text{Where } ratio_i = \frac{KI_{i,j}}{KI_{i,j}^{ref}}$$

$KI_{i,j}$  is the  $i^{th}$  *KI* of the  $j^{th}$  profile,

$i \in \{1..n\}$  and  $j \in \{1..2\}$ ,

345 and  $KI_{i,j}^{ref}$  is the reference measurement of the indicator  $KI_{i,j}$

To calculate a *CMI*, the Geometric Mean is used as it is able to measure the central tendency of data values that are obtained from ratios. The attraction for using the Geometric Mean is that its ratio is equal to the Geometric Mean of performance ratios; which implies that when comparing two different implementations' performance, the choice of the reference implementation is irrelevant [34, 36]. In the current investigation, the reference measurements are considered as an evaluation function that attains an average performance as compared to the targeted *BEFs*. In other words, the reference measurement is calculated as the arithmetic average of results achieved by the targeted *BEFs*.

355 The *OFI* enables the classification of *PSO* algorithm according to its fitness in application. The *OFI* is either directly or inversely proportional to the indicators. The master *OFI* formula, using the developed indicators, is shown in Equation 1. The indicators that are common to the Software (*sw*) and Hardware

360 (*hw*) profiles are labeled with the profile name.

$$OFI = \sqrt[9]{GAP \cdot HWP \cdot SWP} \quad (1)$$

where,

$$GAP = \frac{BEFC}{BEFC_{ref}} \quad (2)$$

$$HWP = \frac{ET_{hw,ref}}{ET_{hw}} \cdot \frac{TH_{hw}}{TH_{hw,ref}} \cdot \frac{LE_{ref}}{LE} \cdot \frac{LR_{ref}}{LR} \cdot \frac{SR_{hw}}{SR_{hw,ref}} \quad (3)$$

$$SWP = \frac{ET_{sw,ref}}{ET_{sw}} \cdot \frac{TH_{sw}}{TH_{sw,ref}} \cdot \frac{SR_{sw}}{SR_{sw,ref}} \quad (4)$$

Besides the main *OFI*, two additional *CMIs* are proposed in Equations 5 and 6 to separately capture the optimization fitness of *HW* and *SW*:

$$OFI_{hw} = \sqrt[6]{GAP \cdot HWP} \quad (5)$$

and,

$$OFI_{sw} = \sqrt[4]{GAP \cdot SWP} \quad (6)$$

### 365 5.6. Performance

The analysis based on the *OFI Output* and *Outcomes* provides measurements for all *KIs* and enables the calculation of the defined *CMIs*. The results enable classifying the targeted evaluations. The six elements of the *OFI* are summarized in Figure 6.

## 370 6. Analysis and Evaluation

The analysis of the developed *PSO* implementations are produced to serve for several evaluation purposes. Important implementation aspects are presented in Section 6.1. In addition, a set of thirteen *BEFs*, namely *F1* through

Figure 6: The six elements diagram of the *PSO* performance analysis model

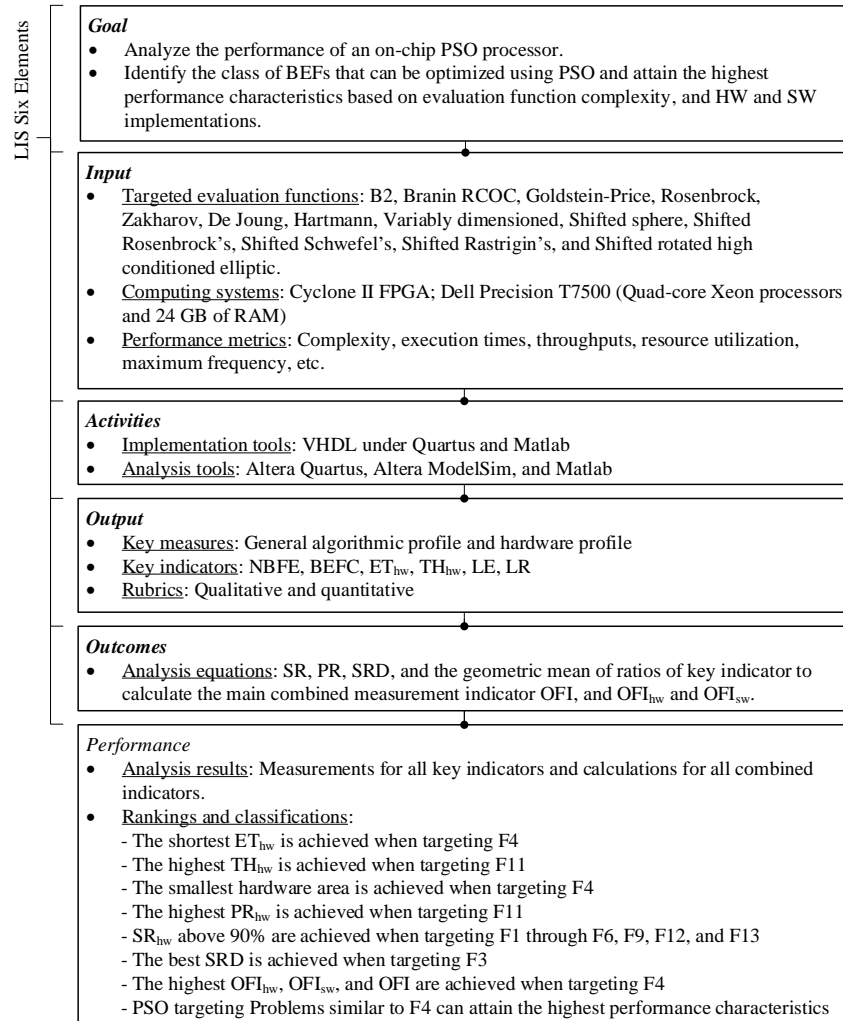


Table 5: PSO execution parameters.

| Parameter                    | Values                                 |
|------------------------------|--|
| Particle Coding              | Binary                                 |
| No. of Bits of Variables     | 8                                      |
| Population Size              | 8, 16, 32                              |
| No. of Independent Runs      | 100                                    |
| Maximal Function Evaluations | 10,000 for F1–F8<br>200,000 for F9–F13 |
| $c_1.r_1$                    | 0–2                                    |
| $c_2.r_2$                    | 0–2                                    |
| Inertia Weight $w$           | 0.25                                   |
| Termination Error Threshold  | $< 10^{-4}$                            |

*F13*, is targeted to perfectly match the test-cases of the work presented in [13] and enable comparisons with similar work. To that end, the *HW* analysis is presented in Section 6.2 with comparisons to similar findings from closely-related work in the literature. A second set of six *BEFs*; namely *F1*, *F3*, *F4*, *F5*, *F6*, and *F8*; is targeted to compare the *HW* and *SW* implementations and evaluate the effectiveness of the proposed *CMIs* (See Sections 6.3). The analysis is done using the developed *KIs* and *CMIs*. The values of the execution parameters are shown in Table 5. In addition, Section 6.4 presents a thorough general evaluation of achievements of the research objectives.

### 6.1. Implementation Aspects

A variety of tools is used to develop, validate, and analyze the hardware implementations. The targeted *FPGA* is *Cyclone II* by *Altera*. The tools used for hardware synthesis and analysis are *Quartus* and *ModelSim*. The hardware implementations are done under *VHDL*. The adopted *VHDL* style mixes structural and behavioral implementations. The units Fitness Module,  $p_{best}$  Update,  $g_{best}$  Update, Velocity Update, Position Update, *RNG*, and the three delay registers are implemented as separate *VHDL* components. The *RNG* is implemented using neighborhood-of-four cellular automata for *FPGAs* [33]. In the proposed hardware implementation, the fixed-point package from [37] is used to express floating-point numbers; the implementation varies in widths

among the different computational entities. The *ieee\_proposed.fixed\_pkg.ALL*  
395 and *ieee\_proposed.math\_utility\_pkg.ALL* VHDL libraries are employed, where  
the highest utilized width is of 64 bits and the highest adopted precision is with  
a fraction part of 9 bits. The adopted fixed-point representation provides a set  
of efficient operations that can replace an intrinsically complex floating-point  
alternative at a compromised but adequate accuracy per context.

## 400 6.2. Hardware Performance Analysis

### 6.2.1. Partitioned versus Nonpartitioned Hardware Implementations

Li et al. in [13] adopt a *HW/SW* co-design approach to improve the execu-  
tion performance of *PSO* for embedded applications. The investigation targets  
the *DE2-70* board from *Altera* with its *Cyclone II FPGA* for *HW* implementa-  
405 tions, and *Nios II* processor for *SW* implementations. The main features of the  
presented approach comprise partitioned *HW* and *SW* implementations of the  
*PSO*. The main proposed system components are a partitioned *HW* and *SW*  
evaluation, and a *HW* particle updating accelerator. The *HW* and *SW* subsys-  
tems communicate through the board interfaces and use an on-board *SDRAM*.  
410 Furthermore, the features include the design of a *HW RNG*. Experimental re-  
sults demonstrate that the proposed *HW* design attains adequate efficiency and  
accuracy. The reported results, of the partitioned implementations, are com-  
pared with *SW* implementations.

In our investigation, exactly the same development board, *FPGA*, *BEFs*,  
415 and the execution parameters of [13] are targeted—to enable a sound compari-  
son. However, we provide a fully-autonomous *HW* implementation on *FPGAs*  
and adopt a different *RNG* algorithm (See Section 4). Tables 6 and 7 present  
the results of the developed *HW* implementation. Here, thirteen *BEFs* are tar-  
geted to enable the comparison with the work reported in [13]. Table 6 shows  
420 that the shortest  $ET_{hw}$  of 2.31 *msec* is achieved when targeting *F4*, and the  
highest  $TH_{hw}$  of 1777.48 *KBFeps* is attained when targeting *F11*. The small-  
est attained hardware area is for targeting *F4* with 6055 *LEs* and 74 *LRs*. On  
the other hand, the longest  $ET_{hw}$  is taken by *F13* with a maximum value of



302.99 *msec* for a population size of 32. Moreover, the lowest  $TH_{hw}$  is attained  
 425 by targeting *F5* with a population size of 32. The largest *HW* areas are required  
 by *F13*. The highest  $PR_{hw}$  of 3561.84 is reached when targeting *F11*; here, the  
 smallest is attained by *F2* with a value of 1.42. To that end, the function that  
 reached the highest *SRD* is *F11* with a maximum of 1418.19 at a population  
 size of 8.

430 In this investigation, adopting the same *FPGA* board and execution param-  
 eters as in [13] supports the conclusion that the achieved performance gains  
 are due to the differences in the proposed *HW* system architectures. With  
 no doubt, the communication cost between the partitioned *HW* and *SW* sub-  
 systems affects the overall performance as reported in [13]. In addition, the  
 435 communication cost increases with the increase in *NBFE*; such an increase in  
 communication further degrades the performance of the developed system. A  
 replacement all-*HW* system is proposed by the authors that targets *F9*. The  
 all-*HW* achieves an *ET* of 13.4673 *ms* with a performance improvement ratio of  
 12115 over their partitioned implementation and 4.29 over our implementation.

Table 6: Hardware Profile: *ET* and *TH*; *BEFs* F1 through F13 are included to enable the comparison with the work presented in [13].

| <b>BEF</b> | <b>ET<sub>(msec)</sub> per Population Size</b> |           |           | <b>TH<sub>(KBFEps)</sub> per Population Size</b> |           |           |
|------------|--|-----------|-----------|--|-----------|-----------|
|            | <b>8</b>                                       | <b>16</b> | <b>32</b> | <b>8</b>   | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 14.04  | 28.84     | 59.27     | 8.83   | 5.89      | 4.57      |
| <b>F2</b>  | 5.41   | 10.37     | 22.46     | 23.66  | 26.52     | 14.16     |
| <b>F3</b>  | 8.29   | 16.14     | 34.77     | 23.88  | 17.29     | 8.86      |
| <b>F4</b>  | 2.31   | 3.89      | 9.23      | 477.49   | 287.15    | 103.47    |
| <b>F5</b>  | 20.87  | 42.64     | 88.35     | 6.76   | 3.94      | 3.62      |
| <b>F6</b>  | 25.31  | 51.91     | 107.28    | 9.25   | 5.82      | 4.25      |
| <b>F7</b>  | 29.63  | 60.93     | 125.69    | 8.07   | 5.58      | 4.18      |
| <b>F8</b>  | 32.82  | 67.55     | 139.2     | 27.79  | 18.76     | 12.22     |
| <b>F9</b>  | 57.85  | 119.81    | 245.9     | 909.96   | 452.55    | 227.11    |
| <b>F10</b> | 66.01  | 136.85    | 280.68    | 506.70   | 251.74    | 126.42    |
| <b>F11</b> | 62.12  | 128.73    | 264.12    | 1777.48  | 883.48    | 443.52    |
| <b>F12</b> | 66.99  | 138.89    | 284.86    | 523.20   | 259.92    | 130.53    |
| <b>F13</b> | 71.24  | 147.77    | 302.99    | 380.81   | 189.10    | 94.99     |

440 In Tables 8 and 9, the  $SR_{hw}$ ,  $PR_{hw}$ , and *SRD* are shown. Targeting the  
 evaluation functions *F2*, *F9*, *F12*, and *F13* enables the achievement of the best  
*SR* value of 100%; while *F7*, *F8*, and *F11* achieve the smallest values with a

Table 7: Hardware Profile:  $LE$  with Percent Hardware Utilization and  $LR$ . The Percent Hardware Utilization is calculated as the ratio of measured  $LE$ s divided by 68416, which is the total number of  $LE$ s available in the target FPGA.  $BEFs$  F1 through F13 are included to enable the comparison with the work presented in [13]

| <b>BEF</b> | <b>LE per Population Size</b> |                        |                        | <b>LR per Population Size</b> |           |           |
|------------|-------------------------------|------------------------|------------------------|-------------------------------|-----------|-----------|
|            | <b>8</b>                      | <b>16</b>              | <b>32</b>              | <b>8</b>                      | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 10340 <sub>15.1%</sub>        | 11534 <sub>16.9%</sub> | 12770 <sub>18.7%</sub> | 239                           | 278       | 309       |
| <b>F2</b>  | 9753 <sub>14.3%</sub>         | 10882 <sub>15.9%</sub> | 12048 <sub>17.6%</sub> | 217                           | 254       | 282       |
| <b>F3</b>  | 9948 <sub>14.5%</sub>         | 11098 <sub>16.2%</sub> | 12288 <sub>18%</sub>   | 224                           | 262       | 291       |
| <b>F4</b>  | 6055 <sub>8.9%</sub>          | 6774 <sub>9.9%</sub>   | 7500 <sub>11.0%</sub>  | 74                            | 95        | 105       |
| <b>F5</b>  | 10943 <sub>16.1%</sub>        | 12203 <sub>17.8%</sub> | 13512 <sub>19.7%</sub> | 262                           | 304       | 338       |
| <b>F6</b>  | 12486 <sub>18.3%</sub>        | 13917 <sub>20.3%</sub> | 15409 <sub>22.5%</sub> | 322                           | 370       | 412       |
| <b>F7</b>  | 14171 <sub>20.7%</sub>        | 15789 <sub>23.1%</sub> | 17482 <sub>25.6%</sub> | 387                           | 443       | 493       |
| <b>F8</b>  | 15756 <sub>23.1%</sub>        | 17549 <sub>25.7%</sub> | 19432 <sub>28.4%</sub> | 448                           | 510       | 569       |
| <b>F9</b>  | 42295 <sub>61.8%</sub>        | 47022 <sub>68.7%</sub> | 52075 <sub>76.1%</sub> | 1472                          | 1647      | 1838      |
| <b>F10</b> | 45608 <sub>66.7%</sub>        | 50702 <sub>74.1%</sub> | 56150 <sub>81.1%</sub> | 1599                          | 1788      | 1996      |
| <b>F11</b> | 43964 <sub>64.3%</sub>        | 48876 <sub>71.4%</sub> | 54127 <sub>79.1%</sub> | 1536                          | 1718      | 1918      |
| <b>F12</b> | 47056 <sub>68.8%</sub>        | 52310 <sub>76.5%</sub> | 57931 <sub>84.7%</sub> | 1655                          | 1850      | 2065      |
| <b>F13</b> | 48725 <sub>71.2%</sub>        | 54164 <sub>79.2%</sub> | 59984 <sub>87.7%</sub> | 1719                          | 1921      | 2145      |

minimum of 24% for  $F8$  with a population size of 8. Indeed, the results show that the best  $SR_{hw}$  and  $PR_{hw}$  are achieved, in most cases, at a population size of 32. Furthermore, the evaluation function  $F4$  achieves the lowest  $SRD$  score; this reflects the smallest hardware area utilization per percent success among all populations.

The results achieved by the proposed hardware implementation show significant improvements, in terms of the measured indicators, over the work reported in [13].  $BEFs$   $F9$  through  $F13$  achieve the best  $ET_{hw}$  improvement ratios that reached 23300, 11233, and 5478 times better than the work reported in [13] for  $F13$  (See Figure 7). In terms of  $TH_{hw}$ , functions  $F4$  and  $F9$  through  $F13$  significantly outperform the implementation in [13] with a maximum speedup of 1777 for  $F11$  (See Figure 8). The best  $SR$  improvement ratio is achieved when targeting  $F11$  with a maximum of 195 (See Figure 9).

### 6.2.2. Sequential versus Parallel Hardware Implementations

In [14], Calazan et al. present a parallel co-processor for  $PSO$  on  $FPGAs$ . In the proposed implementation, all-particles computations are executed simultaneously until finding the  $g_{best}$ . To well-synchronize the computations, and

Figure 7: *ETs* performance improvement ratio of the achieved execution time over the results reported in [13].

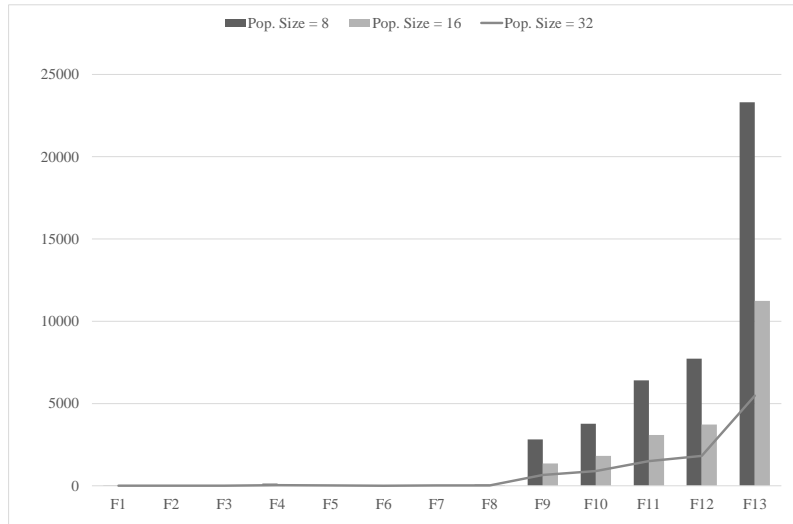


Figure 8: *TH* speedup ratio of the achieved throughput over the results reported in [13].

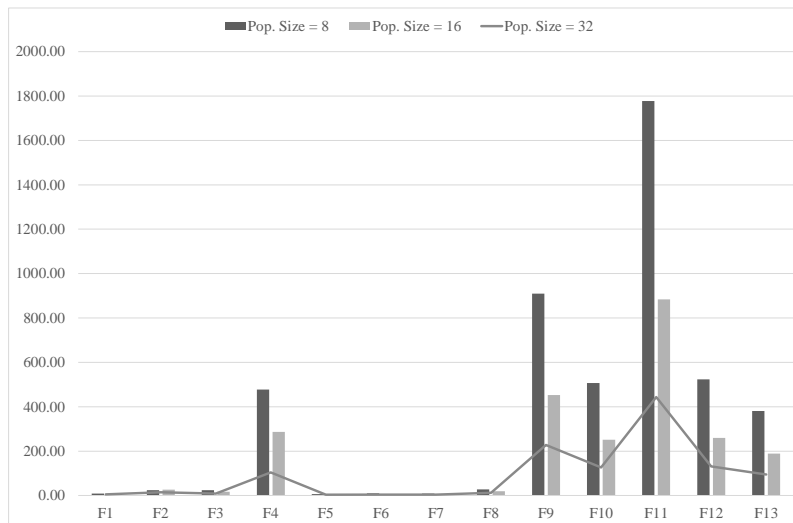


Table 8: Hardware *CMIs*:  $SR_{hw}$  and  $PR_{hw}$ ; *BEFs* *F1* through *F13* are included to enable the comparison with the work presented in [13].

| <b>BEF</b> | $SR_{hw}$ % per Population Size |           |           | $PR_{hw}$ per Population Size |           |           |
|------------|---------------------------------|-----------|-----------|-------------------------------|-----------|-----------|
|            | <b>8</b>                        | <b>16</b> | <b>32</b> | <b>8</b>                      | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 84                              | 98        | 96        | 1.48                          | 1.73      | 2.82      |
| <b>F2</b>  | 90                              | 91        | 100       | 1.42                          | 3.02      | 3.18      |
| <b>F3</b>  | 77                              | 89        | 95        | 2.57                          | 3.13      | 3.24      |
| <b>F4</b>  | 56                              | 83        | 95        | 19.7                          | 13.46     | 10.05     |
| <b>F5</b>  | 92                              | 95        | 89        | 1.53                          | 1.77      | 3.60      |
| <b>F6</b>  | 76                              | 93        | 90        | 3.08                          | 3.25      | 5.07      |
| <b>F7</b>  | 45                              | 77        | 87        | 5.31                          | 4.42      | 6.05      |
| <b>F8</b>  | 24                              | 81        | 93        | 38                            | 15.64     | 18.29     |
| <b>F9</b>  | 100                             | 100       | 100       | 526.41                        | 542.20    | 558.47    |
| <b>F10</b> | 62                              | 69        | 83        | 539.47                        | 499.28    | 427.52    |
| <b>F11</b> | 31                              | 45        | 59        | 3561.84                       | 2527.33   | 1985.46   |
| <b>F12</b> | 100                             | 100       | 100       | 350.49                        | 361.00    | 371.83    |
| <b>F13</b> | 100                             | 100       | 100       | 271.29                        | 279.43    | 287.81    |

460 prevent racing in the values of  $g_{best}$ , the velocity and position computations can only start once  $g_{best}$  is identified among all particles. The execution results are obtained under *Xilinx MicroBlaze* and a high-end *Vertex 6 FPGA*. In addition, the execution parameters are comparable to the ones adopted in this investigation; with the exception to that the authors did not specify the termination error threshold of the stoppage criterion. For a population size of 8, the reported *ETs* attain performance ratios that are between 2.4 and 67.27 times better than those achieved by the hardware implementation proposed in this investigation. However, the proposed implementation outperforms the reported *ET* under the *Xilinx MicroBlaze*; the performance improvement is between 3 to 85 times (See Figure 10). *Vertex 6* is a high-end *FPGA* by *Xilinx*, while *Cyclone II* is presented as a low-end *FPGA* by *Altera*.

In [23], Tewlode et al. present *HW* architectures that significantly accelerates execution performance of *PSO* over *SW* implementations. The proposed *HW* implementation targets a *Xilinx Spartan 3E FPGA*, while *SW* implementations are done using a *Xilinx MicroBlaze* and a Freescale *MC9S12DP256B* microcontroller. The authors also present a multi-swarm parallel *HW* implementation. The parallel implementation achieves a maximum speedup of 3.89 for *F4* and 6.96 for *F9* over the sequential *HW* implementation—with 30 parti-

Figure 9: *SR* improvement ratio of the achieved success rates over the results reported in [13].

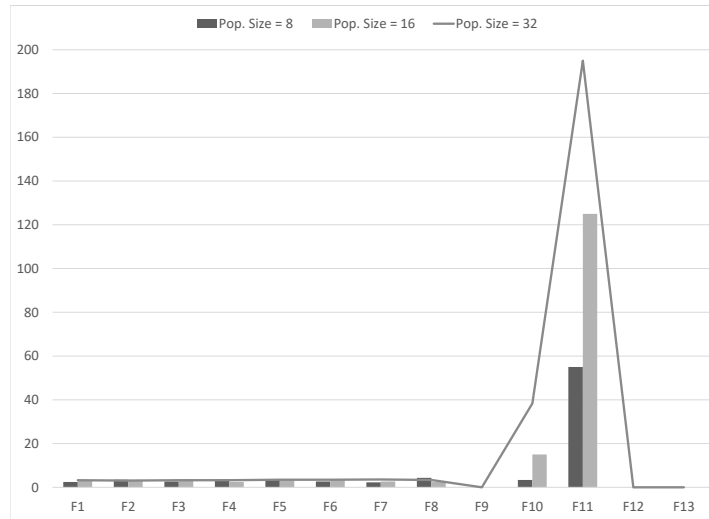


Figure 10: Improvement ratios of the achieved *ET* in *HW* as compared with the results reported in [14]. The results achieved by the *Virtext 6 FPGA* are represented in the negative range as they outperform the *Cyclone II* implementation proposed in this investigation.

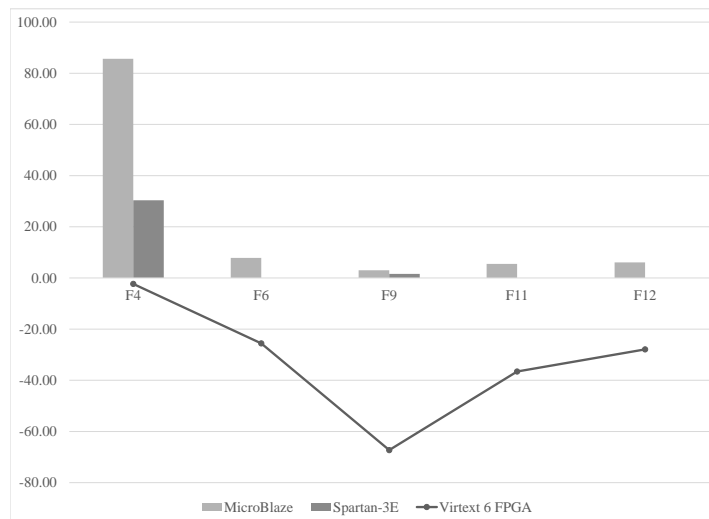


Table 9: Hardware *CMIs*: *SRD*; the *BEFs* *F1* through *F13* are included to enable the comparison with the work presented in [13].

| <b>BEF</b> | <b>SRD per Population Size</b> |           |           |
|------------|--------------------------------|-----------|-----------|
|            | <b>8</b>                       | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 123.10                         | 117.69    | 133.02    |
| <b>F2</b>  | 108.37                         | 119.58    | 120.48    |
| <b>F3</b>  | 129.19                         | 124.70    | 129.35    |
| <b>F4</b>  | 108.13                         | 81.61     | 78.95     |
| <b>F5</b>  | 118.95                         | 128.45    | 151.82    |
| <b>F6</b>  | 164.29                         | 149.65    | 171.21    |
| <b>F7</b>  | 314.91                         | 205.05    | 200.94    |
| <b>F8</b>  | 656.50                         | 216.65    | 208.95    |
| <b>F9</b>  | 422.95                         | 470.22    | 520.75    |
| <b>F10</b> | 735.61                         | 734.81    | 676.51    |
| <b>F11</b> | 1418.19                        | 1086.13   | 917.41    |
| <b>F12</b> | 470.56                         | 523.10    | 579.31    |
| <b>F13</b> | 487.25                         | 541.64    | 599.84    |

cles divided among 5 sub-swarms. However, the *HW* implementation presented  
 480 in this paper outperforms the sequential core in [23] by 30.34 times for *F4* and  
 1.59 times for *F9*.

### 6.3. Analysis of Combined Indicators

To enable the calculation of *OFI* as a main combined indicator, Tables 10  
 and 11 present the implementation results of the general algorithmic and *SW*  
 485 profiles. Table 10 presents the the complexity of the targeted *BEFs* that are  
 needed for the *OFI* calculations and comparisons. Table 11 presents the *KI*  
 results for the *SW* implementation. Moreover, Table 12 shows the measurements  
 of the developed *CMIs* for the *SW* implementations. The calculated results of  
*OFI<sub>hw</sub>*, *OFI<sub>sw</sub>*, and *OFI* are shown in Figures 11, 12, and 13. The results  
 490 confirm that *F4* attains the best *OFI<sub>hw</sub>*, *OFI<sub>sw</sub>*, and *OFI* ranking with values  
 of 3.04, 3.15, and 3.04—for the three different population sizes of 8, 16, and  
 13. Accordingly, the proposed *PSO HW* and *SW* implementations can best  
 perform when targeting the types of problems that are similar to *F4*.

Closely-related work in the literature, including [16, 17, 18, 19, 20, 15, 14,  
 495 20, 21, 22, 13], relies on an almost identical patterns of simple *KIs* to analyze  
 and evaluate their implementations. The adopted analysis patterns can success-

Table 10: General Algorithmic Profile

| <b>BEF</b> | <b>BEFC</b> | <b>Mapped BEFC</b> |
|------------|-------------|--------------------|
| <b>F1</b>  | AQ          | 0.8                |
| <b>F3</b>  | AQ          | 0.8                |
| <b>F4</b>  | HQ          | 1                  |
| <b>F5</b>  | HQ          | 1                  |
| <b>F6</b>  | AQ          | 0.8                |
| <b>F8</b>  | AQ          | 0.8                |

Table 11: Software Profile: *ET* and *TH*.

| <b>BEF</b> | <b>ET<sub>(msec)</sub> per Population Size</b> |           |           | <b>TH<sub>(KBFEps)</sub> per Population Size</b> |           |           |
|------------|--|-----------|-----------|--|-----------|-----------|
|            | <b>8</b>                                       | <b>16</b> | <b>32</b> | <b>8</b>   | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 2.879  | 2.915     | 2.651     | 94.98  | 145.92    | 270.75    |
| <b>F3</b>  | 2.377  | 2.285     | 1.96      | 85.07  | 142.60    | 265.31    |
| <b>F4</b>  | 23.11  | 11.438    | 6.301     | 97.54  | 198.62    | 358.70    |
| <b>F5</b>  | 2.402  | 2.033     | 1.845     | 60.88  | 115.14    | 210.73    |
| <b>F6</b>  | 2.752  | 2.09      | 1.909     | 66.02  | 129.15    | 241.38    |
| <b>F8</b>  | 106.86   | 8.015     | 6.199     | 8.35   | 144.75    | 253.87    |

Figure 11: The  $OFI_{hw}$  classification

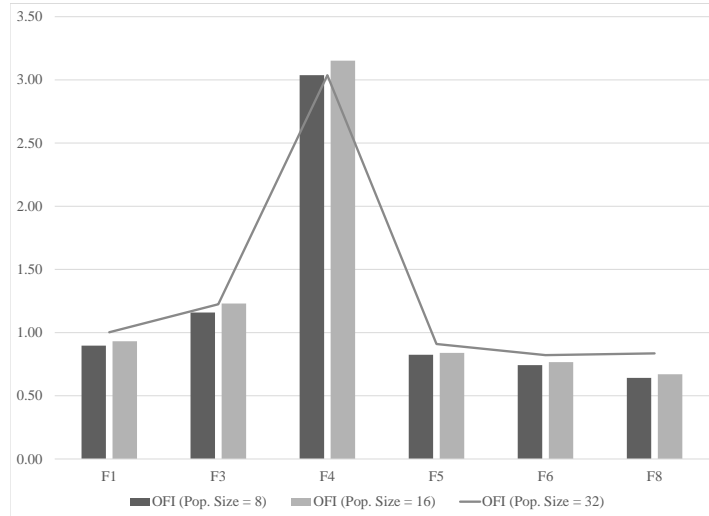


Figure 12: The  $OFI_{sw}$  classification

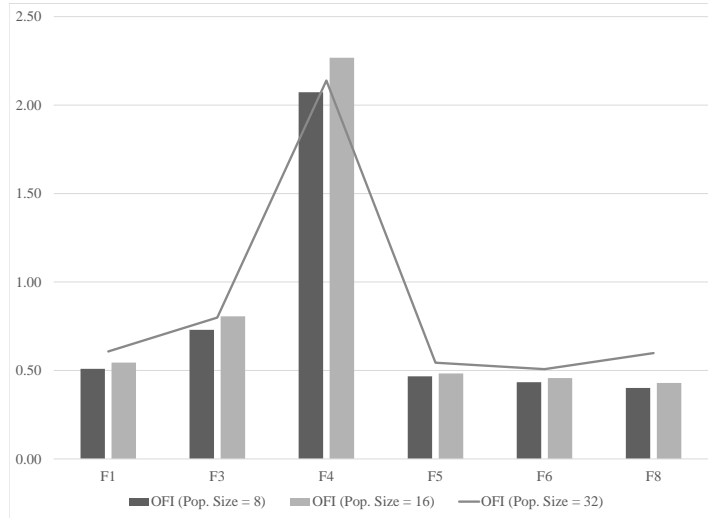


Figure 13: The  $OFI$  classification

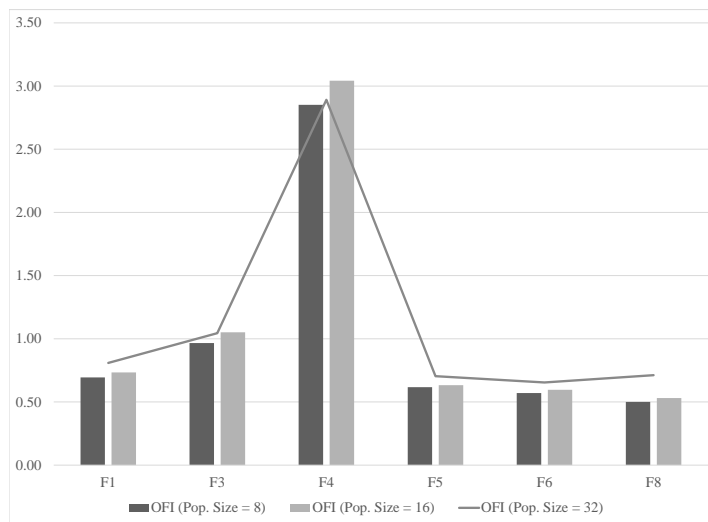




Table 12: Software *CMIs*:  $SR_{sw}$  and  $PR_{sw}$ .

| <b>BEF</b> | $SR_{sw}$ % per Population Size |           |           | $PR_{sw}$ per Population Size |           |           |
|------------|---------------------------------|-----------|-----------|-------------------------------|-----------|-----------|
|            | <b>8</b>                        | <b>16</b> | <b>32</b> | <b>8</b>                      | <b>16</b> | <b>32</b> |
| <b>F1</b>  | 94                              | 100       | 100       | 2.91                          | 4.25      | 7.18      |
| <b>F3</b>  | 87                              | 99        | 100       | 2.32                          | 3.29      | 5.20      |
| <b>F4</b>  | 71                              | 100       | 100       | 31.75                         | 22.72     | 22.60     |
| <b>F5</b>  | 100                             | 100       | 100       | 1.46                          | 2.34      | 3.89      |
| <b>F6</b>  | 100                             | 100       | 100       | 1.82                          | 2.70      | 4.61      |
| <b>F8</b>  | 60                              | 100       | 100       | 14.87                         | 11.60     | 15.74     |

fully classify implementations with-respect-to a single or a limited set of *KIs*. For example, the investigations in [14, 20, 13] successfully rank implementations per *ET*. However, combined indications and evaluative conclusions can hardly be made due to the absence of formal representations of *CMIs*. For instance, it is not straightforward to identify the evaluation function that can best perform in terms of a compromise that includes *ET*, *TH*, *SR*, etc. Our investigation confirms that classifications of implementations based on heterogeneous properties is limitedly addressed in the literature. With no doubt, the identification of the type of problem that can be effectively performed per algorithm implementation is an important evaluation. Such identifications can soundly identify suitable implementation options per application.

#### 6.4. General Evaluation

The current investigation can be evaluated as related to the developed hardware processor, and analysis framework development and application. The developed processor fully maps the *PSO* algorithm onto an *FPGA*. As compared with similar work, the proposed processor attains higher-speeds than similar implementations in the literature. In addition, the results show that, when using partitioned *HW* and *SW* implementations on *FPGA* boards, communication between the *FPGA* and other on-board components can significantly reduce the processing throughput.

The developed framework is unique in combining algorithmic, hardware, and software characteristics to provide unified performance evaluation criteria and useful performance indicators. The investigation proposes the creation of uni-

520 fied indicators that can capture specific qualities in terms of a wide range of heterogeneous key performance indicators, such as the *OFI*. The *OFI* serves as a master *CMI* while an indicator like the *BEFC* is developed with focus on evaluation function complexity. Indeed, the framework is scalable and upgradeable without changing the statistical computation or the structure of the measurement. For instance, an additional profile can be incorporated into the 525 calculations of the *OFI* to include the performance characteristics of Graphics Processing Units.

At the application level, the developed framework can be used to examine qualities of importance and interest to optimization specialists. For example, 530 the developed *OFI* successfully identifies the type of evaluation function that can be best solved by *PSO* and achieve the highest overall performance in terms of the identified *KIs*. The *OFI* enables classifying the *PSO* algorithm performance as targeting a heterogeneous set of evaluation functions. In addition, the framework produces a rich and comprehensive set of reference *KIs*. *KIs*, such 535 as *ET*, *TH*, *LE*, and *LR*, are independent of the context of application and thus highly reusable. Other *KIs*, such as *NBFE*, *SR*, *PR*, and *SRD* are specific to optimization algorithms including the *PSO*.

The proposed framework aims at capturing the *HW* and *SW* properties. The current investigation doesn't include partitioned *HW* and *SW* implemen- 540 tations. However, partitioned implementations can be analyzed, based on the proposed framework, by enabling measurements of *KIs* under the *HW* and *SW* subsystems. The proposed partitioned *KI* measurements can capture subsystems' characteristics. In addition, well-defined *CMIs* can classify different partitioning strategies per optimization target, such as, area, speed, power consumption, etc. 545

## 7. Conclusion

Optimization is a key approach in engineering that enables effective solutions. *PSO* is a current and widely used heuristic; it is well-known for its

effectiveness in application. In this paper, an on-chip *PSO* implementation is  
550 developed and mapped onto an *FPGA*. The developed processor significantly  
outperform the partitioned *HW* and *SW* implementations of [13] that target  
the same development board, *FPGA*, *BEFs*, and the execution parameters. Our  
proposed *HW* implementation achieves an  $ET_{hw}$  improvement ratio of 23300  
for *F13*, a  $TH_{hw}$  speedup of 1777 for *F11*, and the best *SR* improvement ra-  
555 tio of 195 for *F11* over the results reported in [13]. This paper includes the  
development of a statistical framework that enables thorough analysis and eval-  
uation of optimization algorithms, such as *PSO*. The proposed indicators include  
*NBFE*, *BEFC*, *ET*, *TH*, *LE*, *LR*, *SR*, *PR*, *SRD*,  $OFI_{hw}$ ,  $OFI_{sw}$ , and *OFI*. The  
analysis of results confirms that, when targeting *F4*, *PSO* achieves the highest  
560 performance characteristics with the highest *OFI* value of 3.15. The presented  
framework enjoys being reusable in the wider optimization context. Future  
work includes the development of pipelined, parallel, and multi-swarm *PSO*  
processors. The statistical framework can be expanded to capture partitioned  
implementations and to consider additional processing systems, such as Graph-  
565 ics Processing Units. Furthermore, the statistical framework can be applied to  
other metaheuristic algorithms for a wider study. The proposed framework is  
applicable outside the context of optimization [34, 38].

## Appendix

| <b>Acronym</b> | <b>Definition</b>                        |
|----------------|--|
| BEF            | Benchmark Evaluation Function            |
| CMI            | Combined Measurement Indicator           |
| ET             | Execution Time                           |
| FPGA           | Field Programmable Gate Arrays           |
| FSM            | Finite State Machine                     |
| HW             | Hardware                                 |
| GBM            | Generic Benchmark Mode                   |
| GAP            | General Algorithmic Profile              |
| HWP            | Hardware Profile                         |
| KI             | Key Indicator                            |
| BEFC           | Benchmark Evaluation Function Complexity |
| LE             | Logic Element                            |
| LR             | Logic Register                           |
| LUT            | Look-up Table                            |
| NBFE           | Number of Benchmark Function Evaluations |
| OFI            | Optimization Fitness Indicator           |
| PSO            | Particle Swarm Optimization              |
| PR             | Performance Rate                         |
| RNG            | Random Number Generator                  |
| SR             | Success Rate                             |
| SRD            | Success Rate Density                     |
| SW             | Software                                 |
| SWP            | Software Profile                         |
| TH             | Throughput                               |

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