Audio Localization for Robots using Parallel Cerebellar Models

M. D. Baxendale¹, M. J. Pearson², M. Nibouche³, E. L. Secco⁴, and A. G. Pipe²

Abstract—A robot audio localization system is presented that combines the outputs of multiple adaptive filter models of the Cerebellum to calibrate a robot’s audio map for various acoustic environments. The system is inspired by the MOdular Selection for Identification and Control (MOSAIC) framework. This study extends our previous work that used multiple cerebellar models to determine the acoustic environment in which a robot is operating. Here, the system selects a set of models and combines their outputs in proportion to the likelihood that each is responsible for calibrating the audio map as a robot moves between different acoustic environments, or contexts. The system was able to select an appropriate set of models, achieving a performance better than that of a single model trained in all contexts, including novel contexts, as well as a baseline GCC-PHAT sound source localization algorithm. The main contribution of this work is the combination of multiple calibrators to allow a robot operating in the field to adapt to a range of different acoustic environments. The best performances were observed where the presence of a Responsibility Predictor was simulated.

Index Terms—Localization, Learning and Adaptive Systems, Robot Audition.

I. INTRODUCTION

AUDIO can be used by autonomous mobile robots in unstructured environments when other senses, such as vision, break down. For example, in a disaster situation, where it is common to find high concentrations of airborne particles, vision could become impaired as the robot navigates the environment. The motivation for this study is for a robot to be able to locate an entity (such as a person in distress) based on the sounds it produces.

The proposed system uses models of cerebellar microzones [1], each of which has learned to calibrate the output of a robot’s Sound Source Localization (SSL) unit in a different environment, to select a set of models for each environment that the robot operates in. The approach is inspired by the MOdular Selection and Identification for Control (MOSAIC) framework [2], developed in the context of motor control framework [2], developed in the context of motor control.

Responsibility Predictor was simulated.

II. BACKGROUND

A. Robot Audition and Sound Source Localization

Robot audition is a relatively recent area of research developing the ability for robots to listen [5], and is related to Computational Auditory Scene Analysis (CASA) [6]. According to Okuno et al. [7], robot audition consists of three key functions: SSL, sound source extraction (separation of the sources in the audio scene) and source recognition. SSL forms the focus of this work, which draws on robot audition, the adaptive filter model of the cerebellum and MOSAIC to calibrate SSL in different acoustic contexts. A number of efforts have been made to allow a robot to navigate by sound [8], [9], however these systems are typically set up in a specific acoustic environment and can break down if the robot moves to an unexplored environment. Practical SSL schemes typically utilise arrays of multiple microphones, e.g. [10], [11], [12], [13], however size, computation and power constraints on a mobile robot make the study of binaural techniques a compelling choice [14], and that is the approach used in this study. Binaural cues are reviewed in [15], and the two most commonly used are Inter-aural Time Difference (ITD) of arrival of sounds and Inter-aural Level Difference (ILD) [16]. ILD is effective at higher frequencies as it is based on the difference in intensity at the two sensors caused in which a responsibility estimator determines the degree to which each model is appropriate for the context, producing a set of posterior probabilities known as responsibility signals. The system combines the outputs of the cerebellar calibration models in proportion to the responsibility signals. This study extends previous work in which cerebellar calibration of a distorted audio map was used with multiple models to determine a robot’s acoustic environment [3] and to calibrate the visual-tactile map of a whiskered robot [4]. Here, the models are combined in such a way as to improve calibration of the SSL output in different acoustic contexts. For the purposes of this study, a basic cross-correlation SSL algorithm was used. However, in principle, any SSL algorithm could be substituted for the one used, potentially improving robustness of the overall system to background noise, multiple sound sources and so on. The main contribution of this work, rather than demonstrating a robust SSL algorithm, is the demonstration that the combination of multiple cerebellar models allows a robot that has learned to calibrate SSL output in different environments, to select an appropriate set of models as it moves between the different acoustic environments, including, to a limited extent, novel environments.
by frequency dependent scattering by the head of the robot, whereas ITD is limited to lower frequencies as the period of the sound wave becomes comparable to the maximum ITD, giving rise to phase ambiguity [16]. This work focuses on ITD, with microphones mounted in free field, corresponding to Auditory Epipolar Geometry (AEG) [8], [5], and the Head Related Transfer Function (HRTF) is not considered. Sound from a source to either side of zero azimuth \( \theta \) (see Fig. 1) will reach the sensors at different times. ITD is sensitive to environmental characteristics such as reverberation, which can result in distortion of the SSL estimate. In this study we consider SSL only in the azimuthal plane. Most binaural SSL systems have been tested under controlled, limited conditions [17], [18], [19], [20], [21]. A recent area of research related to CASA is Acoustic Scene Classification (ASC), which seeks to identify the acoustic environment from the audio stream [22], however limited work appears to have been carried out on how SSL systems can identify and adapt to different acoustic environments. This work aims to provide a means for SSL systems to be calibrated in various acoustic contexts. The robot head and SSL method are described more fully in section IV.

**B. Cerebellar calibration of the audio map**

Cerebellar calibration of the audio map is based on the adaptive filter model of the cerebellum [1], [23], which has proven to be a robust algorithm in a variety of robotics applications [4], [24], [25]. The technique used here is described more fully in [3], and is adapted from [4]. The adaptive filter model of the cerebellum analyses input(s) into a number of parallel fibres, which synapse onto the Purkinje Cell, which in turn forms the output of the adaptive filter. An error signal adapts the parallel fibre/Purkinje Cell weights (in the Cerebellum this is via the climbing fibres). In [4] a distinct visual marker attached to the target was used to determine the error in location estimation after the motor action. Here, we derive the error using the ground truth azimuth taken directly from the odometry of the test platform during the training of the different models (described in section IV). It is envisaged however, that a robot operating in the field could use vision to determine the error in localization during training of the models.

For audio calibration, shown in Fig. 2, parallel fibre input is activated by input from the underlying SSL unit and transmits a course coded, probabilistic representation of the estimated sound source azimuth as provided by the SSL unit.

The output of each model is the weighted sum of its inputs:

\[
\delta \theta = \sum_{i=0}^{n} w_i p_i
\]

where \( n \) is the number of parallel fibres, \( p_i \) the activity on the \( i \)th parallel fibre and \( w_i \) is the weight of the \( i \)th synapse. This output represents a compensatory bias that is added to the SSL unit estimate, resulting in a calibrated estimate of sound source azimuth.

The weights \( w_i \) are updated using the covariance learning rule [26], [4]:

\[
\Delta w_i = -\beta e p_i
\]

where \( \beta \) is the learning rate and \( e \) is the estimation error (the difference between the ground truth sound source position and the calibrated estimate).

The cerebellar calibration model in learning mode is shown in Fig. 3. The error in sound source estimation (derived in this study using the platform odometry as mentioned earlier in this section) is used to train the model. Post learning, the cerebellar model is then able to apply a shift to compensate for SSL errors. As mentioned in section II-A, the system currently operates in 1 dimension, but could be extended to 2 dimensions (indeed, the work from which the system is adapted operated on a 2 dimensional whisker map [4]). Extension to 2 dimensions or even 3 would involve the same number of models, but with an increase in structural complexity.

**C. Multiple models**

A problem with a single model is that it would need to be highly complex to capture the range of contexts (acoustic environments) within which a robot operates in the field, or would
need to adapt for each context. It has been proposed that the brain makes use of multiple models, each of which has learned to perform in a particular context [2]. A candidate approach to selecting models for a range of contexts is the MOSAIC framework [2], which was developed in the context of motor control but is re-purposed here for audio map calibration by adaptive filter models of the cerebellum. MOSAIC consists of an array of modules each of which could be responsible for control in a particular context. Each module consists of three main elements, a forward model, inverse model and Responsibility Predictor (RP). There is a separate responsibility estimator that operates across the modules. Inputs to the system are sensory feedback (of the consequences of action) and contextual signals. The forward models learn to predict the consequences of action in a particular context while the inverse models learn to control in the same context. The forward model’s prediction error is transformed into a likelihood that its module is responsible for control. At each point in time, all models make a prediction, and the prediction error of each is normalized across all modules as in the MOSAIC framework using an adaptive filter models of the cerebellum. The system has a single model that is used for control but is re-purposed here for audio map calibration by adaptive filter models of the cerebellum. MOSAIC possesses.

where $x_t$ is the true value of the next state of the system, $x_i$ is the estimate produced by the $i$th model, $n$ is the number of estimates (models) and $\sigma$ is a scaling factor. The responsibility signal is used to modulate the output of the module, before summing outputs across modules to produce an overall output. The likelihoods are posterior in that they cannot be determined until after action has taken place, which may lead to transient performance errors when the context changes, and the RP in MOSAIC uses contextual signals to produce a prior prediction of the responsibility signals. The number of models is equal to the number of contexts that the robot has experienced and learned in. However, a claim of the MOSAIC framework is that it should be possible for the system to generalize to novel contexts that are characterized by features that fall intermediate to those of the contexts in which each model has been specifically trained. This means that the robot should be able to cope with more contexts than the number of models it possesses.

III. PROPOSED SYSTEM

The system developed in this study is shown in Fig. 4. It is MOSAIC-inspired rather than being a faithful reproduction of the framework. Rather than MOSAIC’s forward/inverse model pair, the proposed system has a single model that is used for both prediction of the sound source position and calibration of the audio map. The system also implements MOSAIC’s responsibility estimator, the outputs of which are used to modulate the outputs of the model. The system has a single ITD based SSL unit that produces an estimate of sound source azimuth using a cross-correlation algorithm (see section IV-B).

Each cerebellar model, having been trained in a particular context (section IV-C), produces a map-shift signal based on the output of the SSL unit and each shift is individually added to the SSL unit output to form the prediction for each model. Each model prediction is compared to the ground truth position of the sound source.

Each model’s prediction error is transformed and normalized across all models, by the responsibility estimator, the outputs of which are used to modulate the outputs of the model. The system has a single ITD based SSL unit that produces an estimate of sound source azimuth using a cross-correlation algorithm (see section IV-B). Each cerebellar model, having been trained in a particular context (section IV-C), produces a map-shift signal based on the output of the SSL unit and each shift is individually added to the SSL unit output to form the prediction for each model. Each model prediction is compared to the ground truth position of the sound source.

where $\theta_t$ is the ground truth azimuth and $\theta_i$ is the estimate produced by the $i$th model. As explained in section II-B, in
the experiments described here, \( \theta_t \) is derived directly from the odometry, whilst in the field a robot would find \( \theta_t \) through sensory feedback, as in MOSAIC, via another modality such as vision. The ground truth may not always be available to a robot operating in the field (e.g. through obscured vision), and it is assumed that a robot operating in the field would use the most recently available ground truth value to compute the responsibility signals. The modulated model outputs are summed to produce an overall map shift, with a contribution from each model in proportion to its responsibility signal.

In one experiment, described in section V-D, the presence of an RP is simulated. In its current form, the system cannot update the responsibility values until after the ground truth becomes available. In the MOSAIC framework, the RP introduces a prior prediction of the posterior responsibility based on contextual signals. This results in a modified responsibility

\[
\lambda_i = \frac{\lambda_{pi} e^{-|\theta_t - \theta_i|^2/\sigma^2}}{\sum_{j=1}^{n} \lambda_{pj} e^{-|\theta_t - \theta_j|^2/\sigma^2}}
\]

where \( \lambda_{pi} \) is the predicted value of the responsibility of the \( i \)th model. In the field, this would allow the responsibility to be updated even before the robot were to orient toward the sound source, based on features extracted from the audio stream. The RP is simulated here and an implementation is the subject of future work.

IV. METHOD

A. Experimental setup

Matlab (The Mathworks Inc.) was used to control experiments and for implementation of algorithms. Two microphones (Audio-Technica ATR-3350 omnidirectional condenser lavalier) were mounted in free field at the extremities of a horizontal bar (Fig. 6), with an inter-microphone distance of 0.25m and were connected to a computer using a M-Audio MobilePre USB audio capture unit. A sampling rate of 44100Hz was used. Sound pressure level at the microphones was measured using a Max Measure MM-SMB01 sound level meter and was maintained at approximately 70dBA with the sound source directly facing the robot head. Background noise was present in all experiments including acoustic noise generated by the PTU, even while the motion control system was stationary.

A sound source (Logitech Z150 Speaker) was positioned at a fixed distance from the robot head (Fig. 5) and was connected to the computer sound card. Short distances were used due to experimental constraints (0.4m-1m). Although this potentially violates the far field assumption made in this work, localization has been successfully carried out at comparable distances [27], also any violation should be constant across conditions for comparison purposes. Different acoustic contexts were created by rotating the sound source on its vertical axis using a stepper motor under computer control such that it could face away from the robot head at an angle \( \phi \) as shown in Fig. 7. The sound source/stepper motor assembly was suspended from a beam which itself was mounted on a tripod whose central column was placed over the robot head. A geared stepper motor was used to rotate the beam, using a motion control platform (Dynamic Perception Stage R) such that the sound source could be placed in robot-head centric space under computer control at any azimuth between -45° (left with respect to the robot head) and +45°.

B. SSL unit

The SSL unit used a cross-correlation algorithm to generate an estimate of the azimuthal position of a sound source:

\[
r_{lr} = \sum_{k=0}^{n} R(k)L(k - \tau)
\]

where \( R \) is the right- and \( L \) the left channel audio signal, \( k \) is the sample number, \( n \) is the number of samples and \( \tau \) is the time lag between audio channels. The ITD value corresponds to the time difference that results in maximum
similarity between the two channels. The estimated azimuthal position can be calculated from the ITD value as:

\[ \theta = \frac{180}{\pi} \sin^{-1}\left(\frac{c\tau}{f_s}\right) \]  

(7)

where \( c \) is the velocity of sound, \( \tau \) is the estimated ITD, \( d \) is the inter-aural distance and \( f_s \) is the audio sampling frequency.

C. Cerebellar models

Each cerebellar model was trained in one acoustic context with the sound source facing at a different angle (\( \phi \) in Fig. 7) for each context (90° left, 0° and 90° right with respect to the robot head). During learning, the robot head was presented with audio (a 1 second duration Gaussian noise signal) from randomized directions (\( \theta \) in Fig. 7). After training, the robot head was presented with a sequence of audio stimuli in different contexts, with 5 stimuli per context having randomized sound source azimuth. The values of \( \phi \) were chosen as multiples of the resolution of the sound-source mounting stepper motor, 1.8°. Audio stimuli were generated at 1° increments and recorded for off-line training and testing of the system. In the first two experiments (section V-B and V-D), the same 3 contexts were used that the models were trained in. In the third experiment (section V-F), 2 novel contexts were used with values of \( \phi \) that lay between those in which the models were trained. Responsibility signals were initialized to be uniformly equal at the start of each experimental run. The value of \( \sigma \) in equations 4 and 5 was tuned by hand as in [2].

V. Results

A. Overview

In each experiment, the robot head was presented with a sequence of acoustic contexts at 5 randomly selected azimuths. The order of the context sequence is important, as it will affect the development of responsibility values as the system progresses through the trials. In each trial, an uncalibrated sound source localization was made, based on which each model generated a prediction of source location. Each model’s prediction was compared to the ground truth position of the sound source to generate a prediction error for that model.

This was carried out in the next trial, in order to simulate the availability of ground truth in the field through sensory feedback, which would therefore not become available until after the robot had oriented its camera toward the sound source. Plots were produced of each model’s responsibility as the system progressed through the trials to demonstrate the variation of responsibility of each model in different contexts. Results are limited by the resolution of the SSL algorithm, which varies from 1.7° at zero azimuth to 2.4° at 45° azimuth. The resolution is affected by the sampling frequency (44100Hz in this study) and inter-microphone distance (0.25m in this study). In all experiments the scaling factor \( \sigma \) in equation 4 was set to a value of 2 (chosen so as to result in a low performance error over a large number of trials in learned contexts). Localization performance figures were calculated from 10 runs of each experiment of 15 trials.

B. Performance in learned contexts

Fig. 8 shows plots of the responsibility signals of each model as the system progresses through the 15 trials. The coloured regions on the plots indicate the 3 different contexts used, and are labeled according to the corresponding context number. For example, the blue sections represent the 5 trials in context 1. The plots show that it is the model trained in a given context that dominates, with some sharing of responsibility, especially with the adjacent model. The posterior nature of the responsibility signal can be clearly seen, with a delay of one trial before the system responds to a change in context (which causes an increase in performance error during transitions of context)- here we assume that the ground truth would become available during the next trial as discussed in section V-A, and this would correspond to the robot orienting toward the sound source in the field. Rows 1-3 of Table I show that performance of the proposed system is better than that of a single model trained in all contexts, as well as Generalized Cross-Correlation [28] with Phase Transform (GCC-PHAT), which was chosen as a popular SSL algorithm for comparison.
C. Performance in learned contexts with redundant models

As mentioned in section II-C, there would normally be one model per context, but there is a question of how well the system would perform if operating in a subset of the learned contexts, i.e., there were more models operating than required for the currently experienced sequence of contexts. The experiment was repeated with 7 models: the 3 used already plus models trained in contexts with values of \( \phi \) of 135° left, 45° left, 45° right and 135° right. It can be seen from figure 10 that the models trained in the 3 presented contexts (models 2, 4 and 6) still dominated, with some sharing of responsibility with the additional models, but that the system has a comparable performance to that where only the trained models were present (row 4 of Table I).

D. Responsibility prediction

As mentioned in section II-C, the system based on the responsibility estimator alone is only able to determine responsibility after the ground truth sound source position is known; including a responsibility predictor, which makes a prior estimate of responsibilities, should reduce the resulting overall error. Although a responsibility predictor was not implemented in this study, the experiment (using the same data set) was repeated as though a responsibility predictor were present which was able to perfectly predict the posterior responsibilities (using the posterior responsibilities as the value of \( \lambda_p \) in equation 5). The results of this simulation are shown in Fig. 9, where earlier switching of responsibility can be observed between contexts. The localization performance (Table I row 5) is improved. Although the accuracy rate appears excellent, an implementation of the PR may not provide such good results.

E. Performance where the ground truth becomes unavailable

As mentioned in section III the ground truth may not always be available. The ground truth was made unavailable during one trial (trial 6). Fig. 11 shows plots of the responsibility signals of each model (blue curves). In this case the dominance of model 1 is extended into context 2, where dominance of model 2 would have been expected. This extension of the dominant model’s responsibility did not always happen; depending...
on the value of the SSL output, sometimes dominance of the responsibility switched temporarily to an altogether different model. In this experiment, the ground truth becomes available again during trial 7, and the system adjusts the responsibilities accordingly. Row 6 of Table I shows that the performance with this missing ground truth value has deteriorated slightly (we would expect more pronounced deterioration with prolonged absence of the ground truth). The RP potentially plays an important role in such situations, since an actual implementation of the RP would continue to receive contextual signals from the audio stream, even when the ground truth is unavailable. Plots of the RP output are also shown in Fig. 11 (orange curves), and the overall responsibility (broken red curves), calculated using equation 5, shows that the presence of a simulated RP causes more appropriate switching of the responsibilities. Row 7 of Table I shows that the poorer performance is mitigated to an extent by the presence of the RP.

F. Performance in novel contexts

As described in section II-C, a claim of the MOSAIC framework is that combining the outputs of modules that have learned existing behaviours allows the generation of new behaviours to deal with new contexts. By analogy, the system proposed here ought to be able to combine existing cerebellar calibration to new, but similar contexts, by presenting the robot head with acoustic contexts that are intermediate to the ones in which the models were learned. The robot head was presented with contexts corresponding to sound source angles ($\phi$ in Fig. 7) of 72° left; and 72° right with respect to the robot head. Figure 12 shows plots of the responsibilities as the system progressed through the trials in the two contexts. It can be seen that the models that have learned in contexts closest in characteristics to the novel contexts (models 1 and 3) tend to dominate, but less distinctly than in figure 8, so that there is more sharing between adjacent models. Rows 8-10 of Table I show that the performance is better than a single model that was trained in the 3 previous contexts, and is similar to that of the GCC-PHAT SSL method.

G. Performance in domestic contexts

In recognition that the experiments were carried out under constrained conditions, a further experiment was conducted in a domestic dining room. The room was empty apart from the experimental apparatus, which was the same as that used in the other experiments. The dimensions of the room were 3.9m x 3.1m. Background noise was present such as traffic and other urban sources. Trials were conducted in two contexts. In the first context, the experiment was conducted in the middle of the room, with a distance to source of 1m and sound source angle $\phi$ set to 90° right. In the second context, the experiment was conducted in the corner of the room, with a distance to source of 0.5m and $\phi$ set to 135° left. Performance was poorer than in previous experiments, however the proposed system still outperformed the single model trained in all contexts as well as the GCC-PHAT algorithm (rows 11-13 of Table I).

VI. DISCUSSION AND FUTURE WORK

We have presented a multiple-models-inspired cerebellar calibration system for an audio map which was able to automatically select an appropriate set of models and combine the outputs of those models to calibrate the robot’s audio map in different acoustic contexts. The performance of the combined models was better than that of a single model trained in all contexts, as well as the baseline GCC-PHAT SSL algorithm, in both novel contexts and contexts in which the models had been trained. Including the simulation of a
responsibility predictor further increases the performance by providing a prior prediction of responsibility, especially during transitions between contexts. However, an implementation of the RP may not behave in the same way, especially for novel contexts, and this is the subject of future work. The current study is restricted to SSL in 1 dimension, however, as mentioned in section II-B, we are confident the approach can scale up to 2 dimensions and this is a potential area of future work. In the current study, models are pre-trained, whereas a robot operating in the field will need to adapt to partly and completely novel acoustic contexts, and so future work will also include the investigation of adaptation and tabula rasa learning of the models, as described in [29].

REFERENCES


