

# **Droid Geometry**

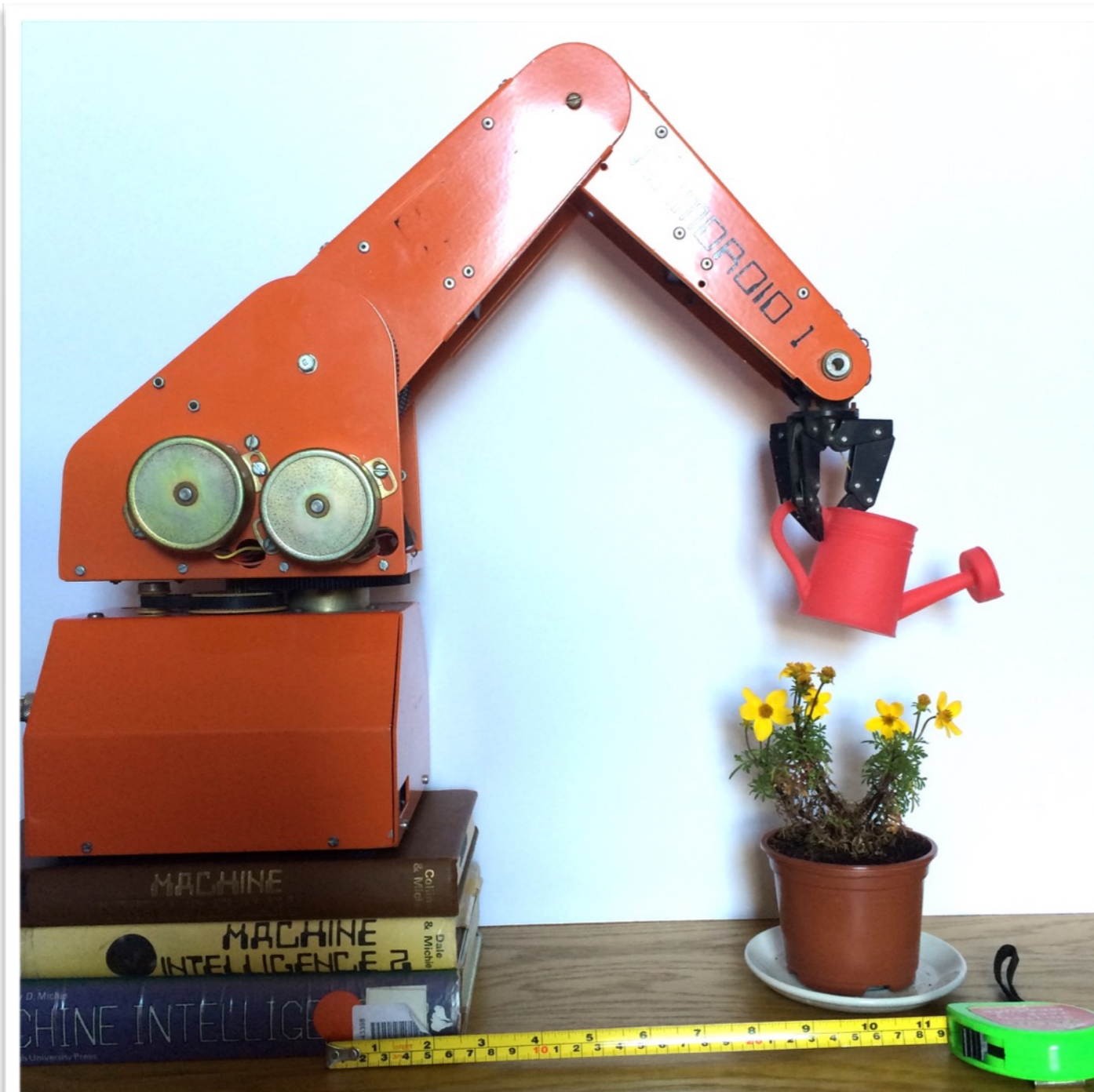
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Maintenance drones are eco-friendly

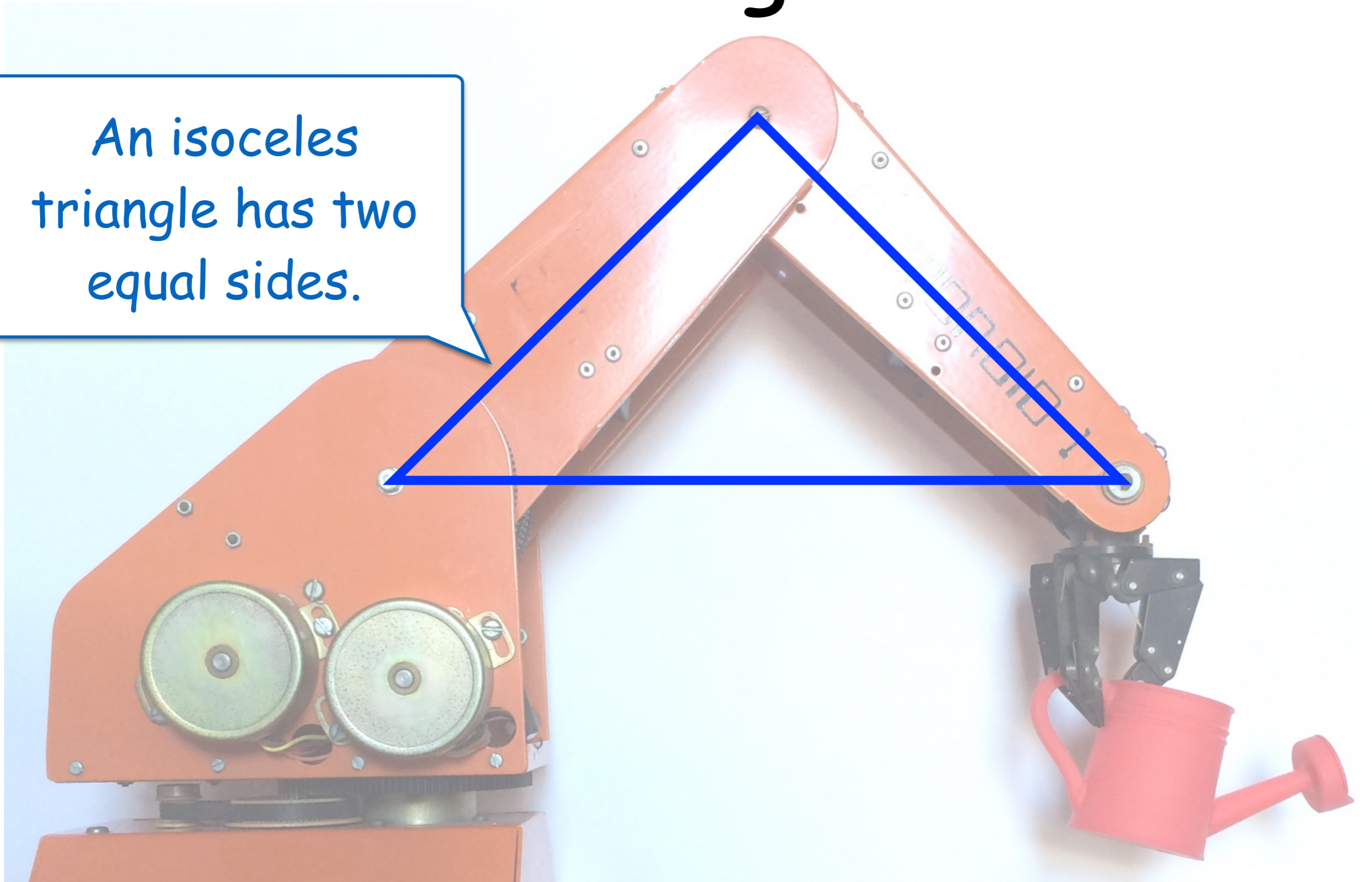
# Flower Power



- How can we make a robot arm water a flower.
- This is the 1981 Armdroid 1.

# Triangles

An isosceles triangle has two equal sides.



# Circles and Angles

A full  $360^\circ$  turn returns the angle to  $0^\circ$

A  $45^\circ$  angle goes anti-clockwise

Angles increase as you go anti-clockwise

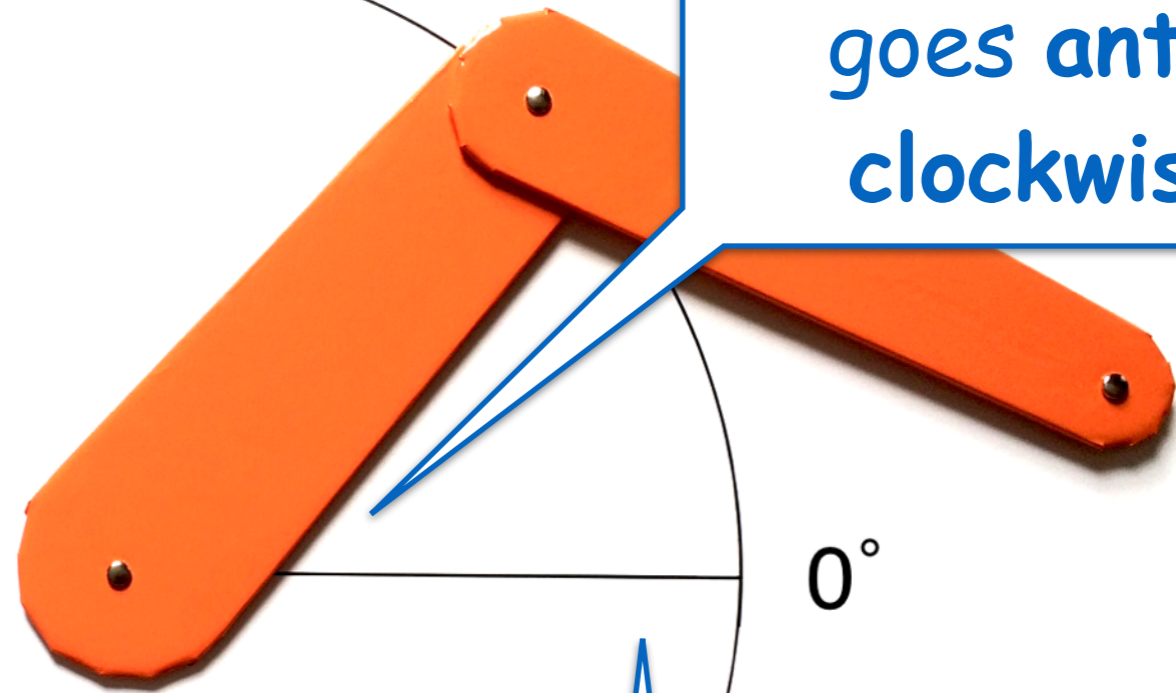
$0^\circ$  is at 3 o'clock

$90^\circ$

$180^\circ$

$0^\circ$

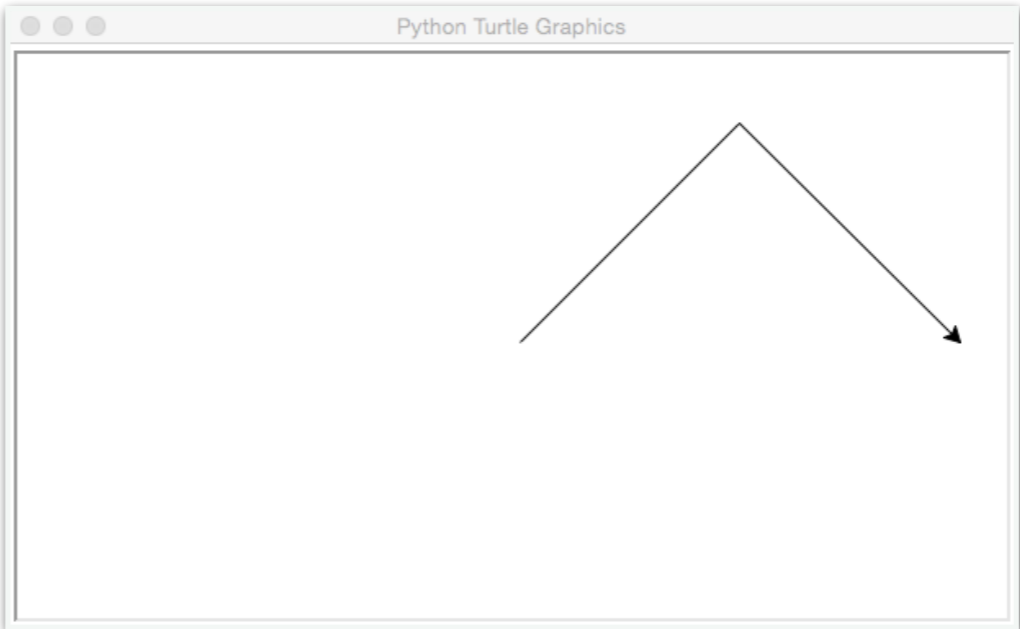
$270^\circ$





# Turtles all the way down

```
Python 3.4.3 Shell
Python 3.4.3 (v3.4.3:9b73f1c3e601, Feb 23 2015, 02:52:03)
[GCC 4.2.1 (Apple Inc. build 5666) (dot 3)] on darwin
Type "copyright", "credits" or "license()" for more information.
>>> from turtle import *
>>> left(45)
>>> forward(190)
>>> right(90)
>>> forward(190)
>>>
```



Ln: 9 Col: 4

Same measurements as the Armdroid

- We can simulate this in Python.
- IDLE is a Python program editor.

# turtle functions

forward(**length**)

backward(**length**)

left(**angle**)

right(**angle**)

penup()

pendown()

done()

speed(**s**)

*e.g. 'slow', 'fast', 'fastest'*

shape(**name**)

*e.g. 'turtle', 'classic'*

goto(**x,y**)

*x,y coordinates*

# Robot Simulator

```
arm1.py - /Users/St  
from turtle import *  
  
length = 190  
  
def arm(angle):  
    left(angle)  
    forward(length)  
  
speed('slow')  
  
arm(45)  
arm(-45)  
  
done()
```

variable

Function definition and parameters

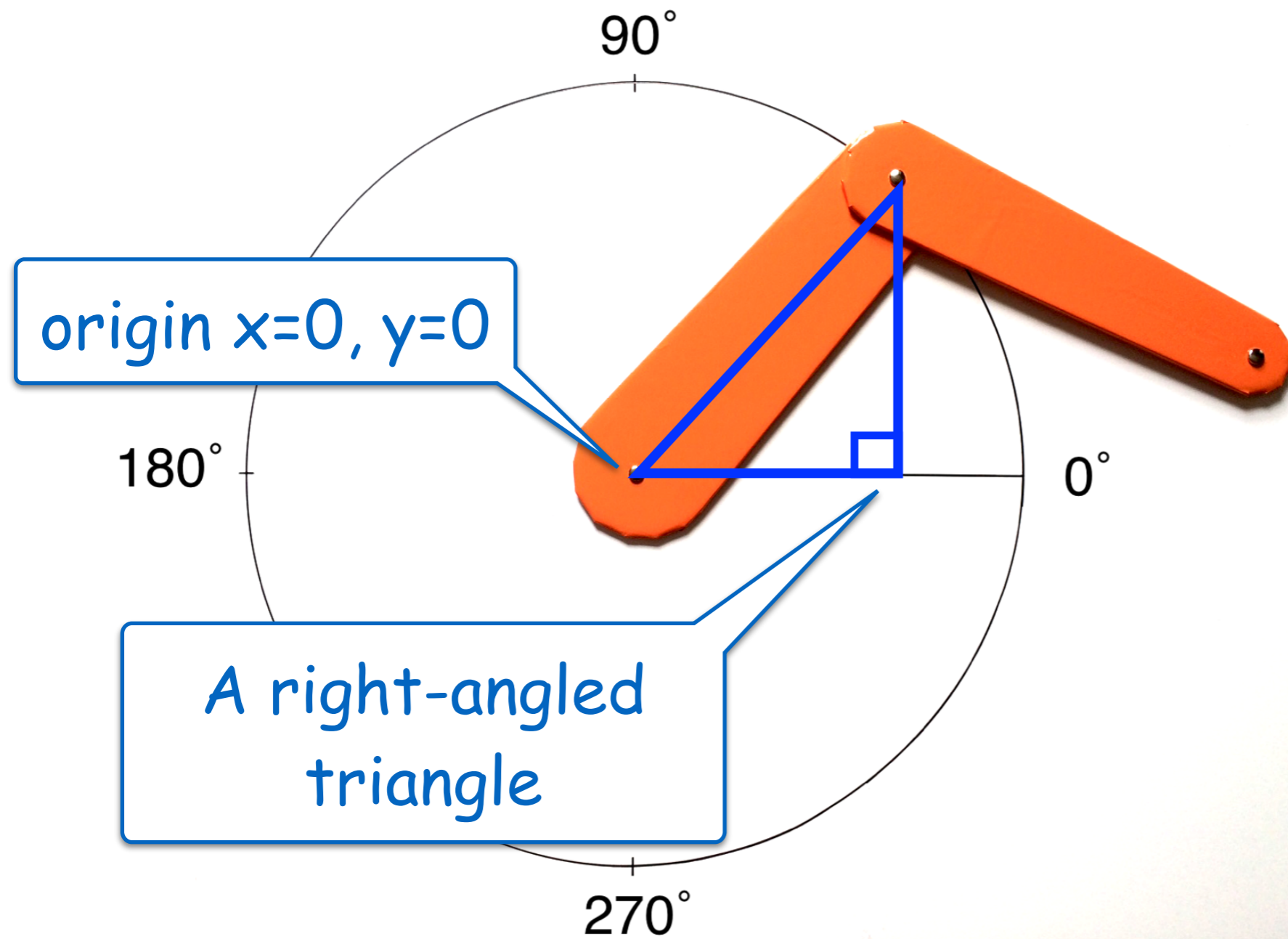
Function call with arguments

try changing the angles

- **File > New File**
- **File > Save**
- **Run > Run Module**

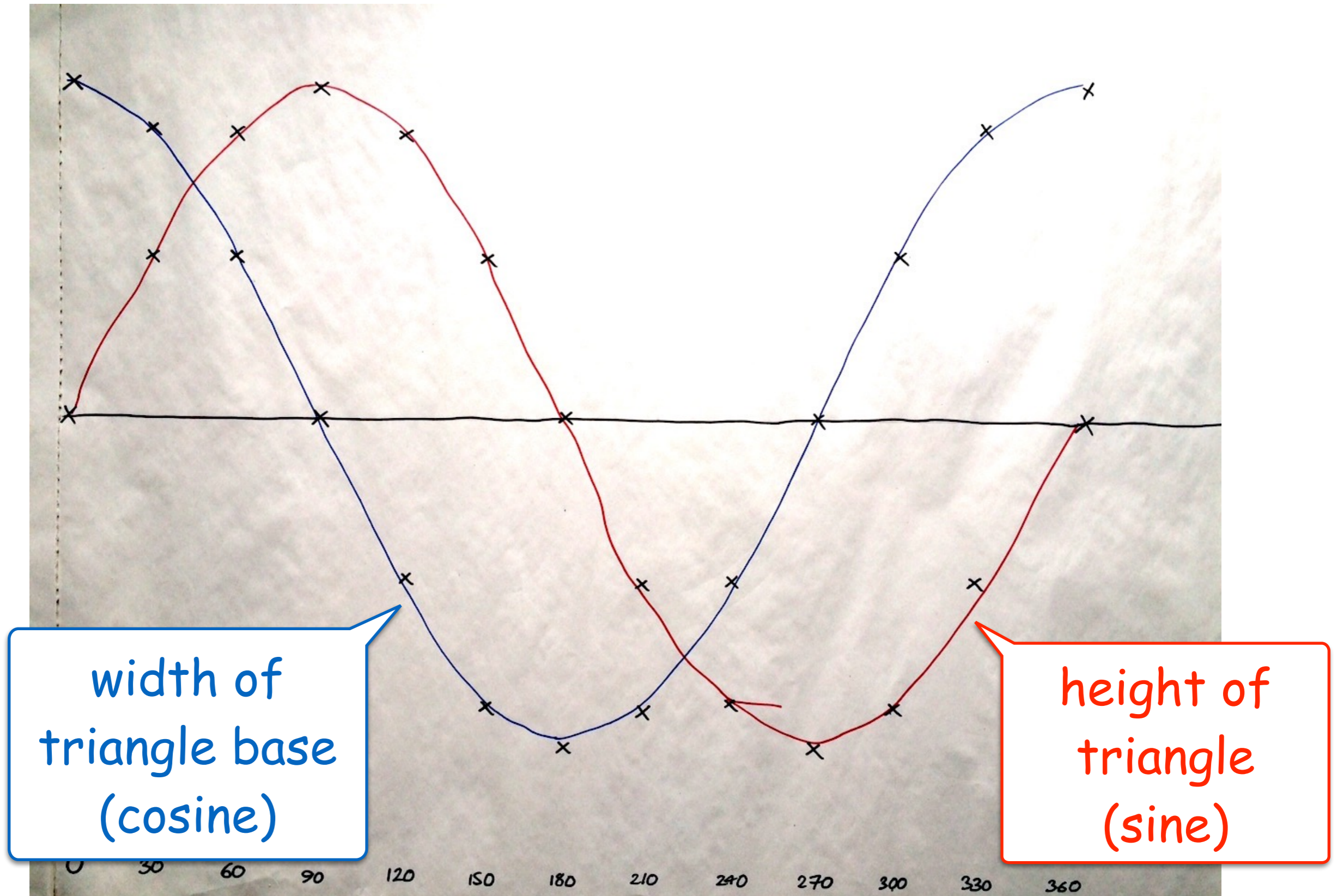


# Robot Kinematics: How far does it reach?



- Break the problem down into triangles.
- We know the arm lengths.

# Triangle width & height



# Analogue vs Digital

- To work out the reach of the upper arm read out the **width** (cosine),  $w$ , in the plot for the angle (eg.  $a=45^\circ$ ).

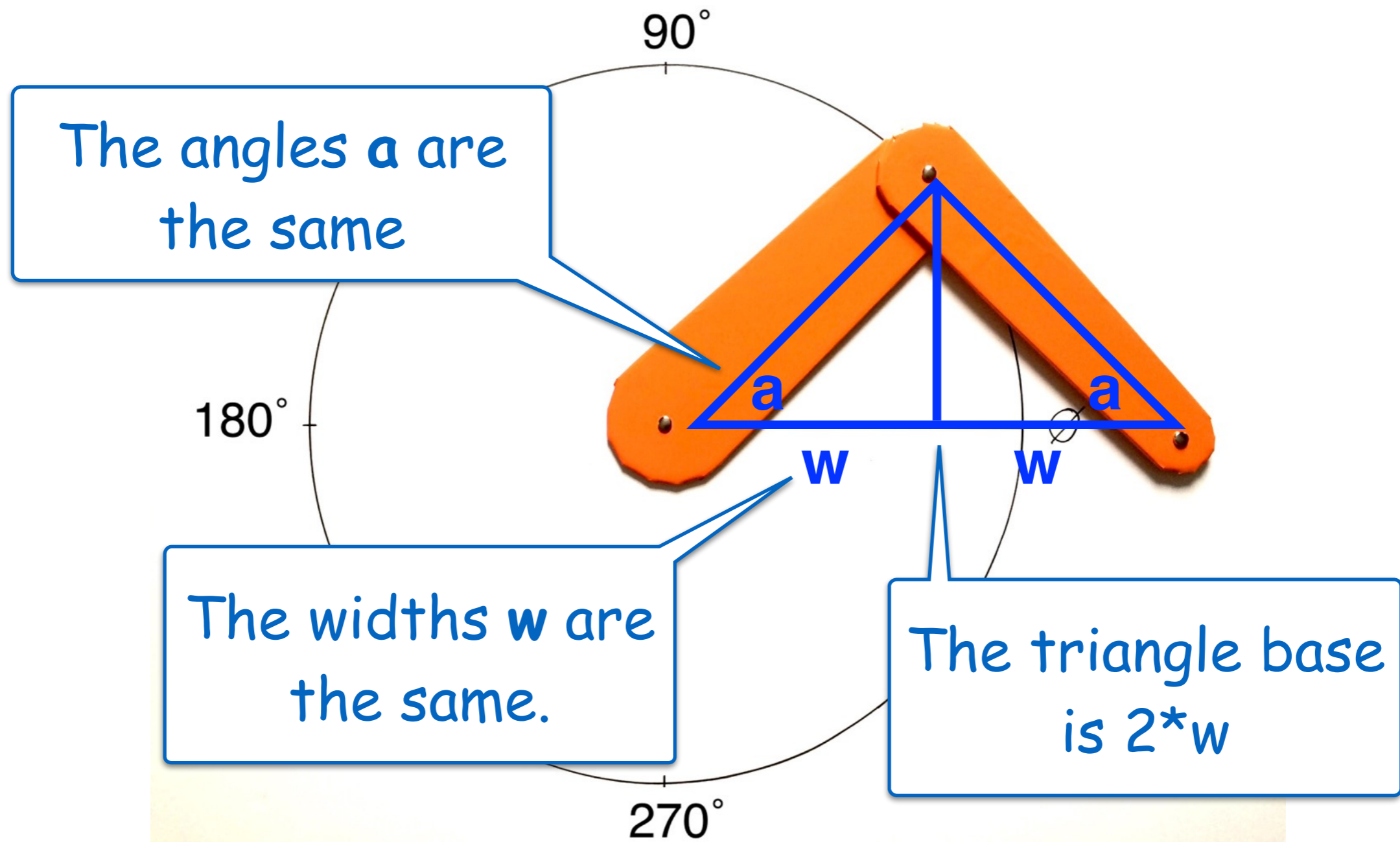
```
*arm.py - /Users/Steve/Documents/Python/arm.py (3.4.3)*  
  
a = 45  
b = 90  
  
arm(a)  
arm(b)  
  
from math import *  
  
w = cos(radians(a))*length  
print(w)  
  
done()
```

Python does this with the `cos` function.

Uses degrees radians.

3 Col: 0

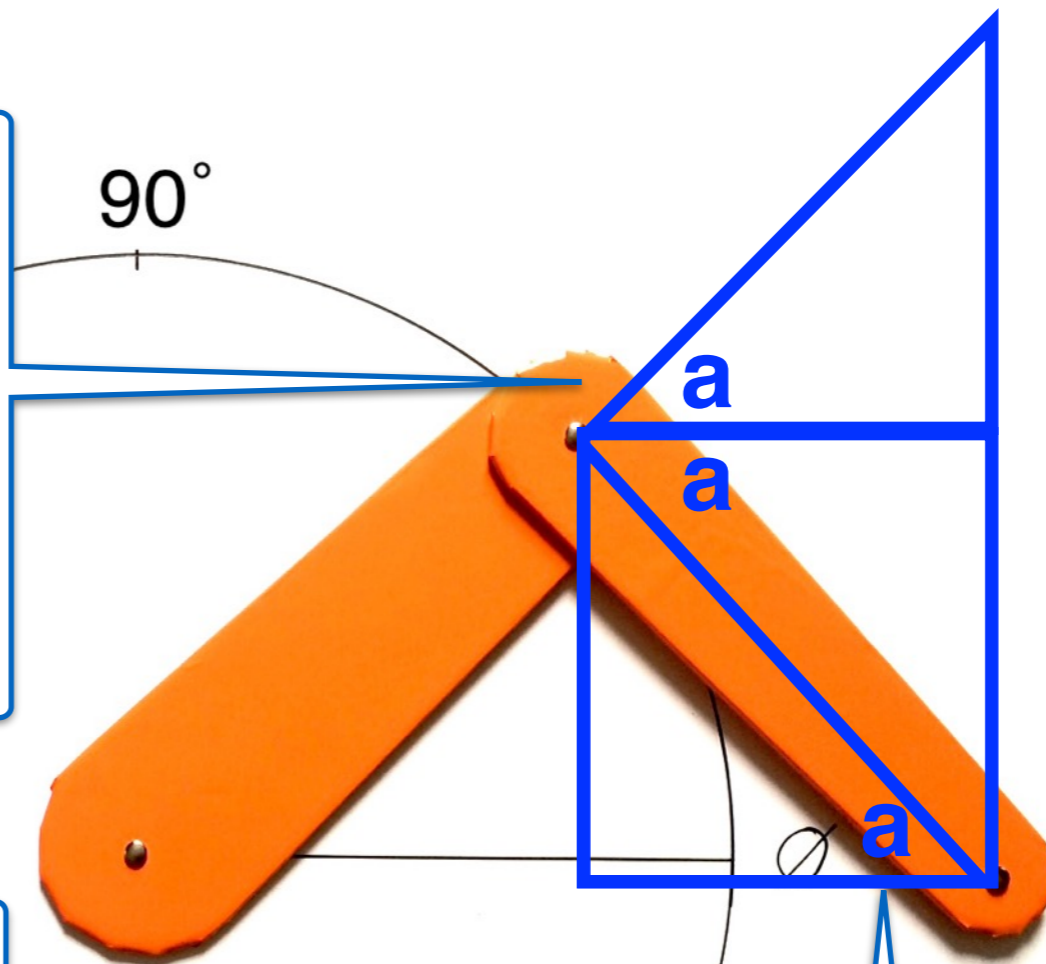
# Adding the forearm



# Give it some elbow

The turtle must turn through the exterior angle  $-2*a$

$-2*a$  is negative because the elbow bends in the opposite way to the shoulder



This is an interior angle.

# Test the results

```
arm.py - /Users/Steve/Documents/Python/arm.py (3.4.3)
Python Turtle Graphics

a = 45
b = -2*a

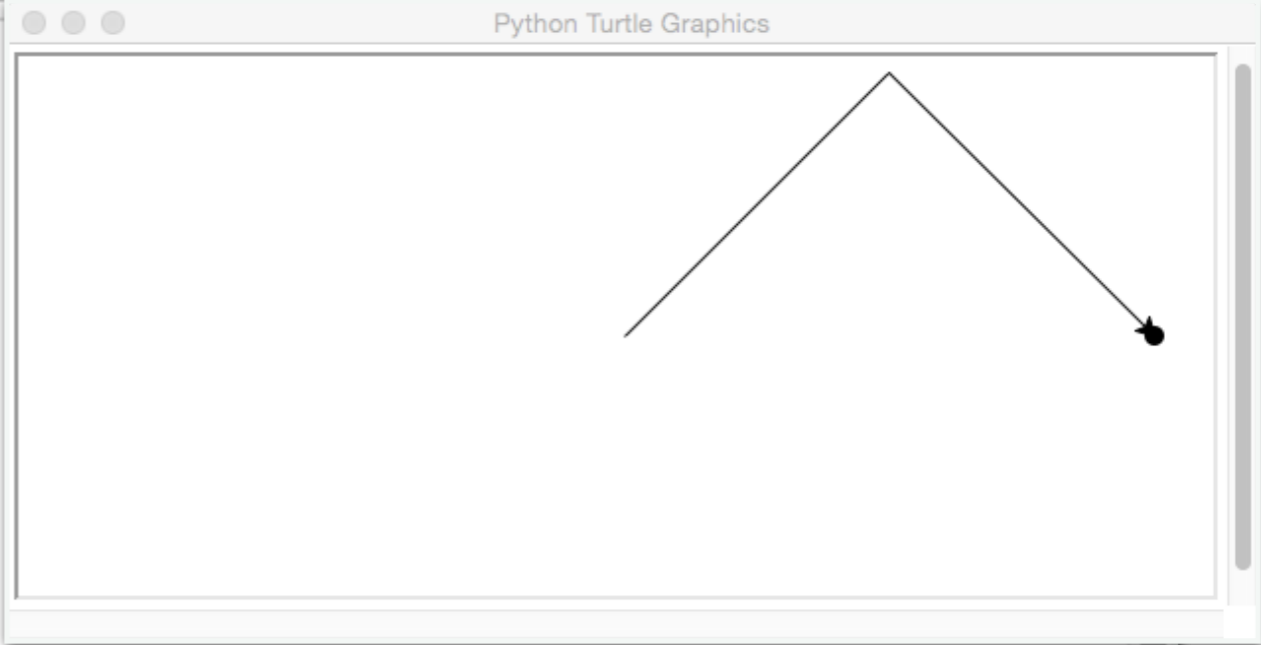
arm(a)
arm(b)

from math import *

w = cos(radians(a))*length
reach = 2*w
print(reach)

penup()
goto(reach,0)
pendown()
dot(10)

done()
```



Check the results by placing a dot at the predicted position.

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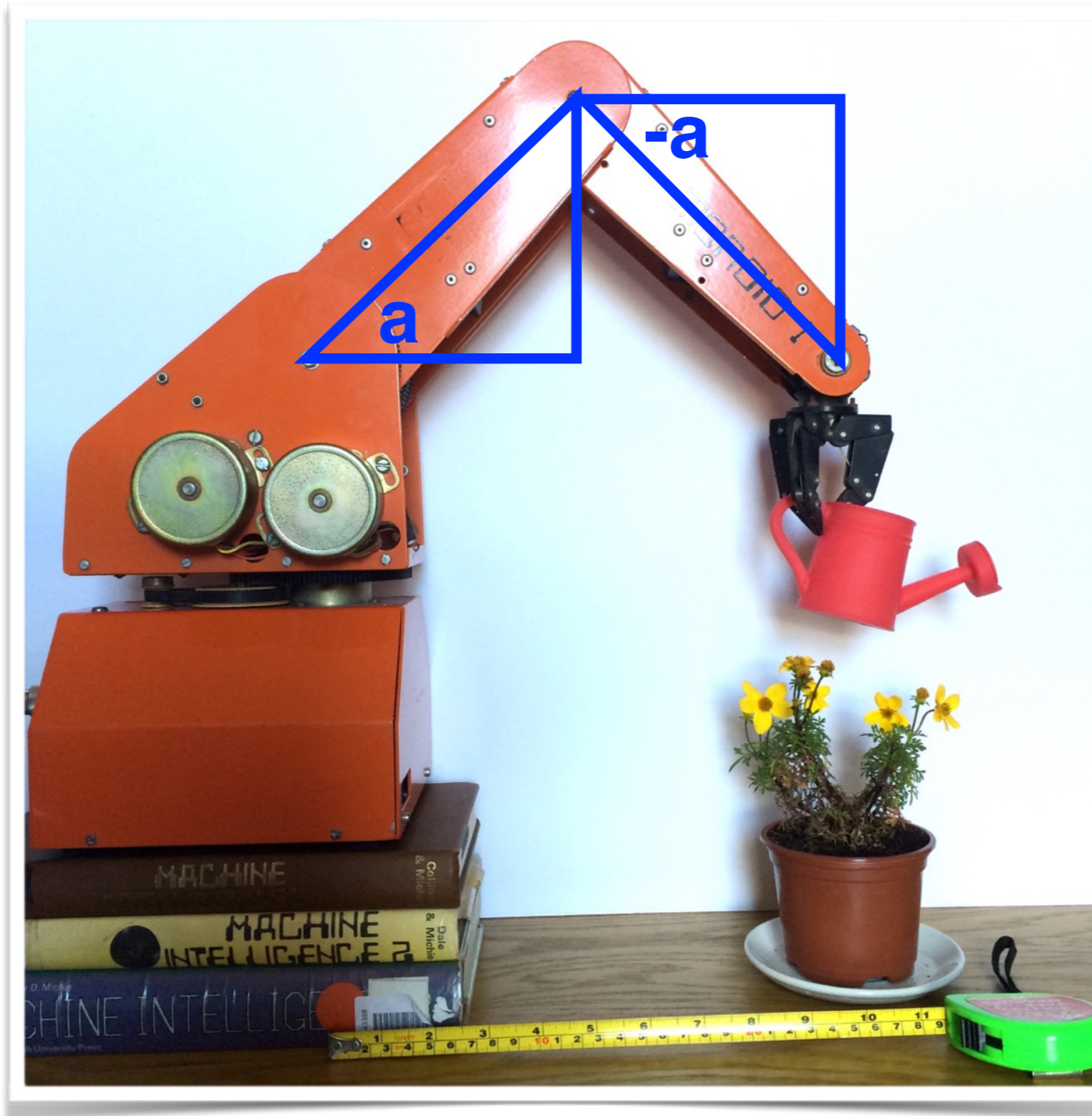
# Parallelograms



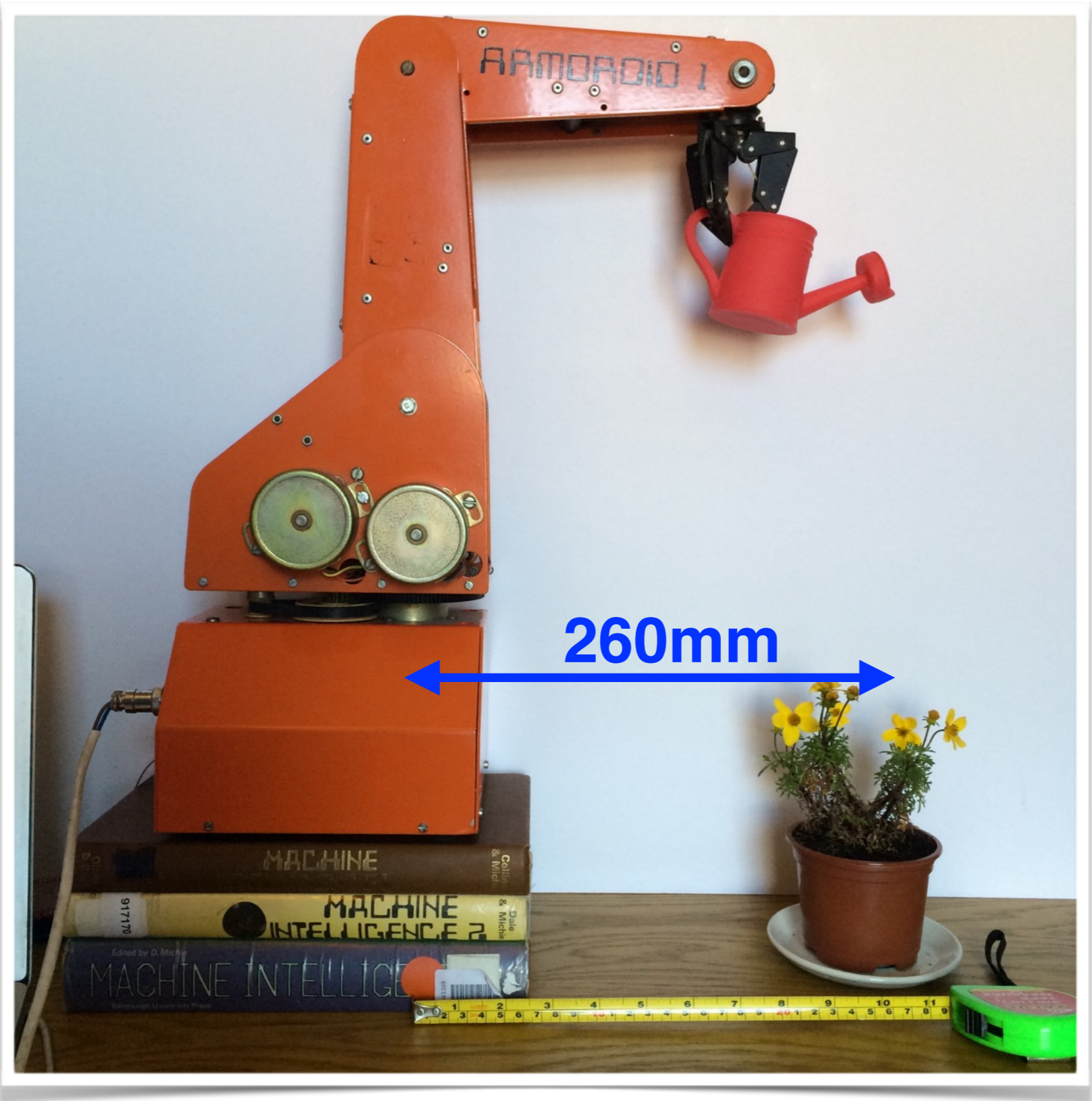
- The **Armdroid** has pulleys so that the forearm maintains its angle.

# Inverse Kinematics

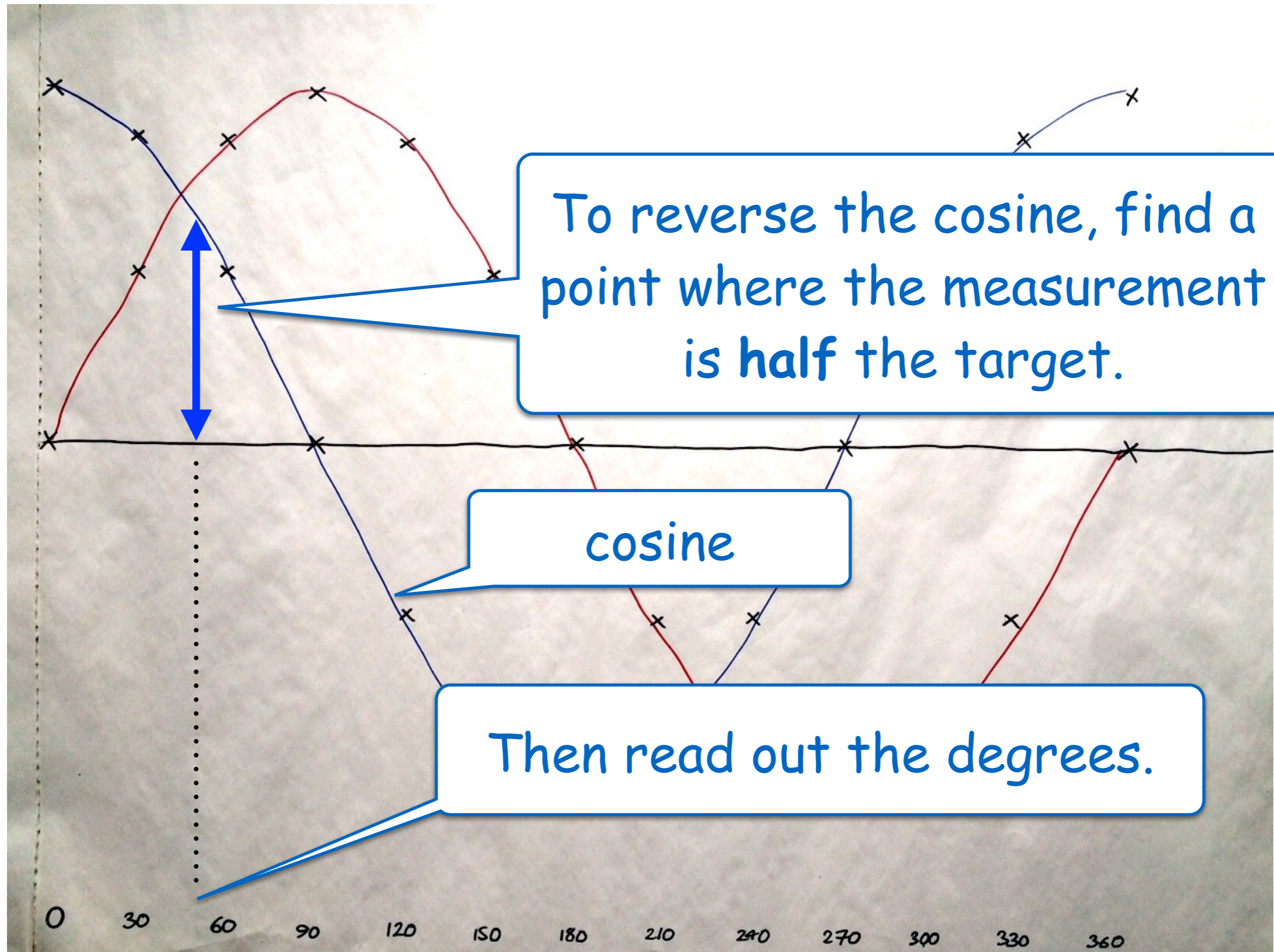
- If we know where the flower is, how do we work out the angle  $a$ ?







# Analogue computer



# Going Digital

```
from turtle import *  
from math import *
```

```
length = 190  
target = 260
```

The flower is 260mm away

```
def arm(angle):  
    left(angle)  
    forward(length)
```

Use the inverse  
(arc) cosine to  
calculate a

```
speed('slow')
```

```
a = degrees(acos(0.5*target/length))  
b = -2*a  
print(a)
```

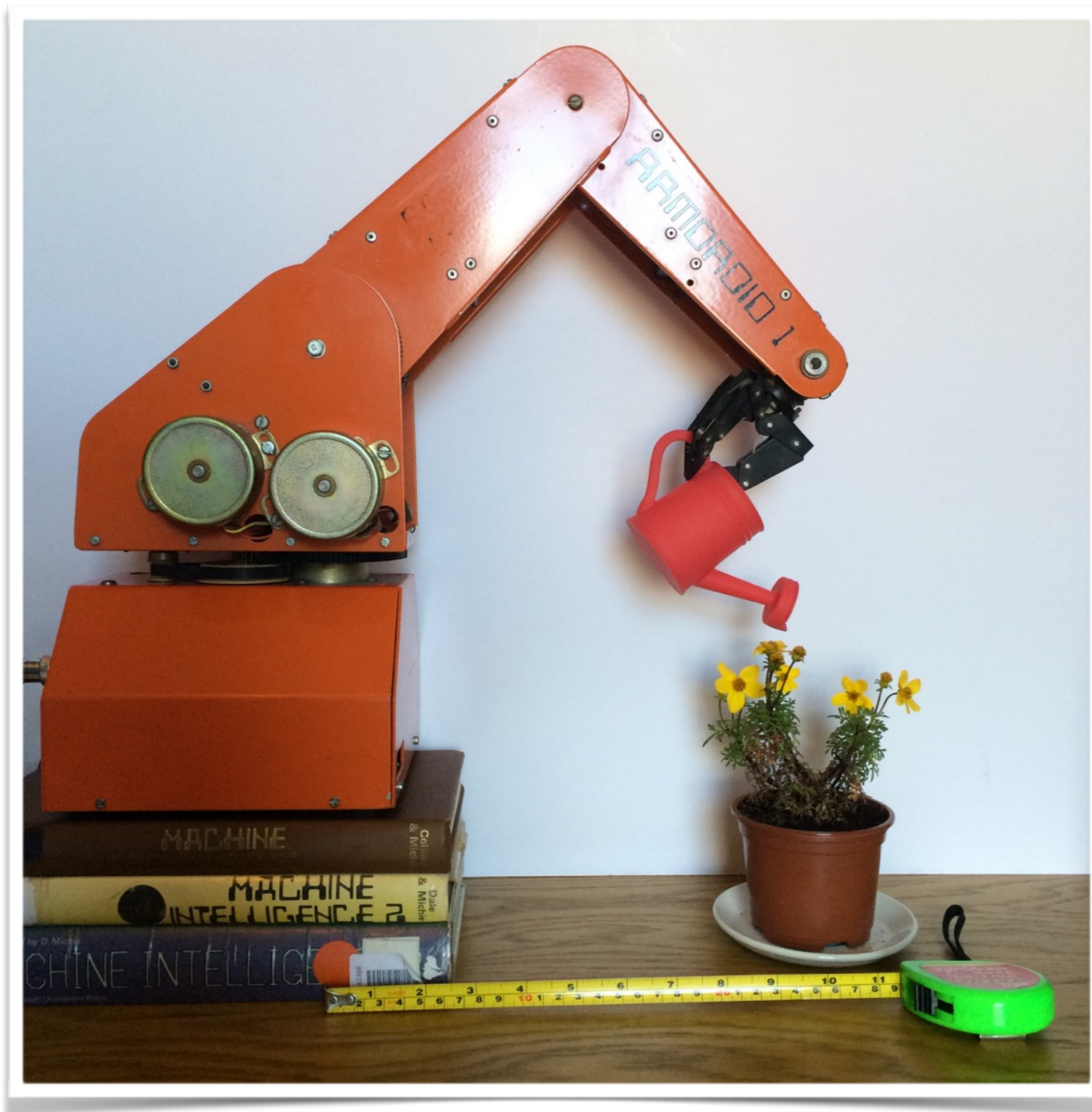
Convert back from radians to degrees

```
arm(a)  
arm(b)
```

```
penup()  
goto(target,0)  
pendown()  
dot(10)
```

Place a dot at the target

```
done()
```



Maintenance Drones are eco-friendly.