#### Abstract

With the growth in requirement for a high reliability of power supply, stability of the power system and the minimum requirement for control systems becomes more and more significant. The most popular way to solve the problem of stability is to install power system stabilizers (PSSs) on synchronous generators in related power systems. The conventional methods for designing PSS are generally based on the compensation approach for the phase and eigenvalue of the generator model. In recent decades, H-norm based robust PSS has been developed because of the system uncertainty of power grids. In another aspect, wind power has evolved into a significant renewable energy source and increased at an outstanding rate. Stability problems of power system with large wind farms became more and more challenging. Some wind plant modelling methods, for which PSSs are not taken into consideration, have been developed and widely used in practical applications.

The present study is concerned with a comprehensive power system stability analysis based on an improved H-norm robust controller design method and a novel modelling approach for doubly fed induction generator (DFIG) wind turbines. Initially, one improved lemma, enhanced with LMI regional pole placement, is developed for linear matrix inequality (LMI) based  $H_2/H_{\infty}$  robust output feedback controller design. Robust PSSs are designed based on the approach and they are tested in both single and multimachine systems. A novel DFIG wind turbine model is then built up and tested with the robust PSS in both single and multi-machine systems to see the oscillations damping ability. Finally, based on the robust PSS, a large multi-machine power system with wind parks is selected for a comprehensive stability analysis.

Simulated examples and case studies are employed in this study to demonstrate the effect of new PSSs. The simulation results clearly suggest that the proposed PSS can solve the stability problem of damping oscillations in power systems with large wind parks.

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### List of publications based on this study

#### **Conference** papers

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Peng, Y., Zhu, Q. M., and Nouri, H., 2011(b), Robust H<sub>2</sub> power system stabilizer design using LMI techniques, *The Proceeding of 2011 International Conference on Modelling, Identification and Control (ICMIC)*, 21--24, June, 2011, Shanghai, China.

Peng, Y., Zhu, Q. M., and Nouri, H., 2012(a), LMI based  $H_2/H_{\infty}$  power system stabilizers fir large disturbances in power systems with wind plant, *The Proceedings of 2012 International Conference on Modelling Identification and Control (ICMIC)*, 24--26, June, 2012, Wuhan, China.

Peng, Y., Nouri, H., and Zhu, Q. M., 2012(b), Robust power system stabilizers for multimachine systems with large wind parks, *The 47th International Universities' Power Engineering Conference*, September 4--7, 2012, London, UK.

Peng, Y., Zhu, Q. M., and Nouri, H., 2013(a), LMI based robust PSS for grid-connected DFIG wind turbines, *The Proceedings of 2013 International Conference on Modelling Identification and Control (ICMIC)*, September, 2013, Cairo, Egypt.

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#### **Journal papers**

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# Abbreviations

Abbreviations	Descriptions
AC	Alternating Current
ARE	Algebraic Riccati Equation
AVR	Auto-Voltage Regulator
CIGRE	International Council on Large Electric Systems
CPSS	Conventional Power System Stabilizer
DC	Direct Current
DFIG	Doubly Fed Induction Generator
EE	Energy to Energy
EMF	Electromotive Force
EP	Energy to Peak
FACTS	Flexible Alternating Current Transmission System
FMAC	Flux Magnitude and Angular Control
FRS	Feasibility Radius Saturation
FSIG	Fixed Speed Induction Generator
GEVP	Generalized Eigenvalue Problem
GWEC	Global Wind Energy Council
HVDC	High Voltage Direct Current

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Abbreviations	Descriptions
IE	Impulse to Energy
IEEE	Institute of Electrical and Electronics Engineers
IGBT	Insulated Gate Bipolar Transistor
IMOFC	Improved Mixed $H_2/H_\infty$ Output Feedback Controller
LFO	Low Frequency Oscillation
LMI	Linear Matrix Inequality
LOEC	Linear Optimal Excitation Controller
NEC	Nonlinear Excitation Controller
PID	Proportional Integral Derivative controller
PP	Peak to Peak
PSS	Power System Stabilizer
PSS/E	Power System Simulation for Engineering
PTI	Power Technology International
PWM	Pulse Width Modulation
SAVNW	Name of the New England Power System
SDRE	State-dependent Riccati Equation
SMIB	Single Machine Infinite Bus
STATCOM	Static Synchronous Compensator
SVC	Static Var Compensator

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VSC

Voltage Source Converter

# Symbols

Symbols	Descriptions
Δ	Deviation of the parameter (can be put before any symbol)
C <sub>dc</sub>	DC capacity of the DFIG wind turbine
$D_{pg}$	Damping torque factor for synchronous generators
$E_d$	Internal electromotive force on $d$ axis
$E_q$	Internal electromotive force on $q$ axis
$E'_{d}$	Internal transient electromotive force on <i>d</i> axis
$E'_{q}$	Internal transient electromotive force on $q$ axis
$E^{\prime\prime}_{q}$	Post-transient electromotive
$E_{fd}$	Electromotive force of exciter winding
i <sub>d</sub>	Synchronous generator stator current on <i>d</i> axis
i <sub>L</sub>	DFIG inductance current
$i_q$	Synchronous generator stator current on $q$ axis
<i>i</i> ,	DFIG rotor current
I <sub>ds</sub>	DFIG stator current on <i>d</i> axis
$I_{qs}$	DFIG stator current on $q$ axis

Symbols	Descriptions
I <sub>dr</sub>	DFIG rotor current on <i>d</i> axis
I <sub>qr</sub>	DFIG rotor current on $q$ axis
K <sub>A</sub>	Gain of exciter
$K_E$	Self-excitation factor of exciters
$K_{F}$	Rotor feedback factor
$K_{P1}, K_{I1}$	Controller parameter of the outer PID controller of DFIG
$K_{P2}, K_{I2}$	Controller parameter of the inner PID controller of DFIG
L	DFIG converter inductance
$L_s$	DFIG stator inductance
L <sub>r</sub>	DFIG rotor inductance
$L_m$	DFIG mutual inductance
M <sub>e</sub>	Electrical torque of synchronous generator
<i>M</i> <sub><i>m</i></sub>	Mechanical torque of synchronous generator
Q <sub>ref</sub>	DFIG reference input of reactive power
R <sub>s</sub>	DFIG stator resistance
R <sub>r</sub>	DFIG rotor resistance

Symbols	Descriptions
S	Operator for Laplace transform
S <sub>s</sub>	Slip of DFIG
$S_E$	Saturation factor of exciters
$T_0$	Transient time constant of DFIG
$T_b$	Time constant of DFIG pitch angle control system
$T'_{d0}$	Open circuit time constant on <i>d</i> axis
	Special time constant used in five-winding generator model
	Open circuit time constant on $q$ axis
	Time constant of regulators
$T_E$	Exciter time constant
$T_F$	Time constant of rotor feedback section
$T_{j}$	Time constant of the one-mass drive train of DFIG
T	Inertia coefficient of synchronous generator
	DFIG rotor side mechanical torque
	Blade input mechanical torque
u <sub>a</sub>	Voltage from the grid side controller of DFIG

Symbols	Descriptions
u <sub>r</sub>	Reference voltage input to the exciter
u <sub>rw</sub>	Voltage from the rotor side controller of DFIG
u <sub>s</sub>	Output voltage from power system stabiliser
u <sub>sw</sub>	DFIG stator voltage
u <sub>td</sub>	Terminal voltage of synchronous generator on d axis
u <sub>tq</sub>	Terminal voltage of synchronous generator on $q$ axis
U <sub>dc</sub>	DFIG DC capacitor voltage
U <sub>dcref</sub>	Reference input of DFIG DC capacitor voltage
U <sub>ds</sub>	DFIG stator voltage on d axis
$U_{qs}$	DFIG stator voltage on $q$ axis
U <sub>dr</sub>	DFIG rotor voltage on <i>d</i> axis
U <sub>qr</sub>	DFIG rotor voltage on $q$ axis
U <sub>t</sub>	Terminal voltage of the generator
U <sub>REF</sub>	Reference voltage input
	Leakage reactance
x <sub>d</sub>	Stator reactance on <i>d</i> axis

Symbols	Descriptions
$X_q$	Stator reactance on $q$ axis
x' <sub>d</sub>	Stator transient reactance on <i>d</i> axis
x'' <sub>d</sub>	Post-transient reactance on <i>d</i> axis
x' <sub>q</sub>	Stator transient reactance on $q$ axis
X',	DFIG transient reactance
	Impedance of transformer
Z <sub>L</sub>	Impedance of transmission line
β	Pitch angle of DFIG
ω	Angular speed
$\omega_0$	Synchronous speed of synchronous generator
$\omega_{\scriptscriptstyle ref}$	Reference input of the DFIG speed
ω <sub>s</sub>	Synchronous speed of the DFIG
δ	Power angle
$\psi_{ds}$	DFIG stator flux on <i>d</i> axis
$\psi_{qs}$	DFIG stator voltage on $q$ axis
$\psi_{dr}$	DFIG rotor flux on <i>d</i> axis

Symbols	Descriptions
$\psi_{qr}$	DFIG rotor flux on $q$ axis
$\Psi_d$	Synchronous generator flux linkage on d axis
$\Psi_q$	Synchronous generator flux linkage on $q$ axis
8	Kronecker Product