Enhanced Thermoelectric Performance of *p*-type BiSbTe Through Incorporation of Magnetic CrSb

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There is evidence that magnetism can potentially increase the thermopower of materials, most likely due to magnon scattering, suggesting the incorporation of intrinsic magnetic semiconductors in non-magnetic thermoelectric materials. Here, samples of *p*-type $Bi_{0.5}Sb_{1.5}Te_3$ with 10 at.% excess Te are ball-milled with varying ratios of the antiferromagnetic semiconductor CrSb (0, 0.125, 0.5, and 1 wt.%) to prepare bulk samples by spark plasma sintering technique. The thermopower of samples containing CrSb is increased due to an increase in the effective mass of the charge carriers, indicating that there is a drag effect originating from the magnetic particles. However, this was at the expense of reduced electrical conductivity caused by reduced charge carrier mobility. While overall only marginal improvements in power factors were observed, these samples exhibited significantly lower thermal conductivity compared to the single-phase material. As a result, a peak *zT* value of ~1.4 was achieved at 325 K for the sample with 0.125 wt.% CrSb. These results highlight the potential of incorporating magnetic secondary phases to enhance the

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thermoelectric performance of materials.

To create a high-performance thermoelectric ing in increased thermopower due to interactions material, one must simultaneously achieve a high between charge carriers and local magnetic mopower factor ($PF = \alpha^2 \sigma$) and a low total ther- ments ^{6,15–18}; and (3) introducing magnetic secmal conductivity (κ). However, α , σ , and κ ondary phases, such as nanoparticles or incluexhibit strong correlations¹⁻³, making the task of sions, into non-magnetic thermoelectric matrioptimizing one parameter independently while ces¹⁹⁻²². keeping the others constant extremely challenging.

tronic band structure to improve the figure of merit $zT = PF/\kappa T^{4,5}$. However, the thermoelectric performance of these alloys is limited by their relatively low thermopower.

Studies on Ba_{0.3}In_{0.3}Co₄Sb₁₂^{19,23} and Ti_{0.25}Zr_{0.25}Hf_{0.5}NiSnSb²⁰ materials have shown Bismuth telluride alloys are among the most that the inclusion of coherent magnetic particles efficient thermoelectric materials for near-room- can simultaneously enhance thermopower and temperature applications. Alloying Bi₂Te₃ with carrier mobility. Magnetic secondary phases Sb₂Te₃ optimizes parameters such as carrier con- may allow the tuning of properties through the centration, lattice thermal conductivity, and elec- composition, size, and microstructure of the materials²⁴⁻²⁸.

In this study, ball-milled stoichiometric Bi_{0.5}Sb_{1.5}Te₃ 10 at.% Te-rich and CrSb (0, 0.125, 0.5, and 1 wt.%) samples were fabricated by The use of magnetism has emerged as a spark plasma sintering (SPS). Excess Te was promising strategy to increase thermopower added to the system as Te-rich bismuth telluride through mechanisms such as paramagnon drag and bismuth antimony telluride alloys showed and spin-dependent effects⁶⁻⁹. The concept that high thermoelectric performance²⁹⁻³². The inclumagnetism can possibly enhance thermoelectric sion of excess Te suppresses the defects caused properties dates back decades, with early work by its easy volatilization during the SPS proproposing that magnon scattering could be the cess³³ and this strategy has been shown to reorigin of an increase in the thermopower of some sult in more efficient thermoelectric materials³². magnetic elements at low temperatures¹⁰. These CrSb is an antiferromagnetic semiconductor with include (1) using intrinsically magnetic semi- a Néel temperature of approximately 680 K³⁴, conductors, such as MnTe¹¹, CuFeS₂^{12,13}, and which makes it a promising magnetic secondary $Cr_2Ge_2Te_6^{14}$; (2) doping non-magnetic thermo- phase candidate for improving the thermoelectric electric materials with magnetic elements result- performance for room temperature applications.

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By incorporating varying concentrations of mag- 900 °C³⁵.

netic CrSb particles, it was possible to increase the thermopower through the indicated drag effect while maintaining a relatively high electrical conductivity. The addition of a secondary phase introduces additional phonon scattering mechanisms that reduce thermal conductivity. This enabled a high peak of $zT \approx 1.4$ at 325 K.

1000 °C, quenched in cold water, and annealed at 400 °C for 72 h.

A pristine CrSb sample was synthesized by loading stoichiometric amounts of Cr (99.95%, Alfa Aesar) and Sb (99.999%, Alfa Aesar) into a vacuum-sealed quartz ampule. The ampule sintered samples were characterized by Powder was heated to 850 °C for 24 h, mixed every 4 h, X-ray Diffraction (PXRD) using a PANalytical homogenized at 1160 °C for 1 h, and allowed to X'Pert Pro diffractometer with CuKa1 radiation cool naturally. The resulting ingot was hand- ($\lambda = 0.15406$ nm, 40 kV, 40 mA). ground using an agate mortar and pestle in a Rauenstein, Germany) at 50 MPa for 20 min at LSR-3 apparatus.

Samples of Bi0.5Sb1.5Te3 with x wt.% CrSb (x = 0, 0.125, 0.5, and 1) were fabricated by wet ball milling powdered ingots of Bi_{0.5}Sb_{1.5}Te_{3+0.3} and CrSb. The cast ingots were pre-milled using an agate mortar and pestle in a glovebox. The powders were weighed and placed in a reduction, combined with a higher thermopower, 250 mL agate jar with 20 mm agate balls and ethanol (99.97%, VWR). The ball-to-powder ra-Polycrystalline Bi_{0.5}Sb_{1.5}Te_{3+0.3} samples tio was 15:1, and the solvent-to-powder ratio was were synthesized by direct reaction of stoichio- 100 mL to 10 g^{36} . Milling was performed using metric amounts of Bi (99.999%, Alfa Aesar), a Retsch Planetary Ball Mill PM 100 at 300 rpm Te (99.999%, Alfa Aesar), and Sb (99.999%, for 4 h at 15 min intervals with 5 min breaks and Alfa Aesar) in vacuum-sealed quartz ampules a change in direction halfway through. The jar in an inert atmosphere glovebox. The ampules was then placed in a desiccator for at least 15 h. were heated to 850 °C for 12 h, homogenized at The dried powders were sintered in a graphite die under vacuum to make Ø11 mm rods using SPS at 50 MPa for 5 min at 400 °C^{37,38}. The densities of all samples were approximately 95% of their nominal density.

The phase purity and crystal structure of the

Electrical conductivity (σ) and thermopower glovebox, loaded into a vacuum-sealed quartz (α) were measured perpendicular to the sintering ampule, and annealed at 900 °C for 24 h. The an-direction of the samples by cutting $\approx 2 \times 2 \times 8$ nealed powder was then sintered in a graphite die mm³ bar specimens from the rods. Measureunder vacuum to make Ø11 mm rods using SPS ments were conducted from room temperature to (KCE FCT-H HP D-25 SD, FCT Systeme GmbH, 523 K under a helium atmosphere using a Linseis

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ples was measured by the LFA method using a thermopower (Fig. 2(a)), indicating p-type semi-NETZSCH LFA 467 HyperFlash® instrument. conductor behavior. The electrical conductivity Slab-shaped samples were also cut to measure exhibited metallic behavior with decreasing valthe room-temperature Hall coefficient $(R_{\rm H})$ un- ues, as seen in Fig. 2(b). For the sample with der a ± 0.55 T magnetic field using an ECOPIA x = 0.5, a significant bipolar contribution is ob-3000 Hall Effect Measurement System. The served, as indicated by the sharp increase in elec-Hall carrier concentration $(n_{\rm H})$ was calculated trical conductivity at higher temperatures^{39,40}. as $n_{\rm H} = 1/(e \cdot R_{\rm H})$, where *e* is the elementary charge.

The PXRD patterns of all samples in Fig. 1 match the rhombohedral Bi_{0.5}Sb_{1.5}Te₃ phase. The inset shows that the diffraction pattern of the pristine CrSb sample corresponds to a singlephase CrSb hexagonal structure.



FIG. 1. Powder X-ray diffraction patterns of $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.% CrSb (x = 0, 0.125, 0.5, and 1) samples. The inset shows the diffraction pattern for pristine CrSb.

The thermal diffusivity (D) of all the sam- tion of sintering. All samples showed positive

The room-temperature values of the thermopower increase with the concentration of the CrSb, rising from $\sim 238 \,\mu V.K^{-1}$ for the singlephase sample to $\sim 280 \,\mu V.K^{-1}$ for the 1 wt.% CrSb. With the opposite effect on electrical conductivity, the electrical conductivity of the singlephase sample decreased from $\sim 2.7 \times 10^4 \text{ S}.\text{m}^{-1}$ for the single-phase sample to $\sim 1.8 \times 10^4 \text{ S}.\text{m}^{-1}$ for the sample with 1 wt.% CrSb.

Fig. 2(d) shows the temperature-dependent electrical transport properties of pristine CrSb samples measured perpendicularly to the sintering direction. The electrical conductivity and thermopower are comparable to the one seen in the literature³⁵. Table I lists the Hall carrier concentrations and mobilities of the samples. The carrier concentration of these samples is lower than those observed in the literature $(\sim 1 \times 10^{19} \text{ cm}^{-3})^{32}$ which results in an overall Figs. 2(a) to (c) show the thermopower, lower electrical conductivity. The mobility of electrical conductivity, and power factor of 232 cm².V⁻¹.s⁻¹ for the single-phase samples $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.% CrSb (x = 0, 0.125, is similar to those reported in the literature (e.g., 0.5, and 1), measured perpendicular to the direc- $248 \text{ cm}^2 \cdot \text{V}^{-1} \cdot \text{s}^{-1})^{29}$. The values of n_{H} ranged



FIG. 2. Temperature dependence of the (a) thermopower, (b) electrical conductivity, and (c) power factor of $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.% CrSb (x = 0, 0.125, 0.5, and 1) samples, and (d) thermopower and electrical conductivity of pristine CrSb.

from 7.1 to 7.7×10^{18} cm⁻³, therefore showing be attributed to changes in the values of $n_{\rm H}$. The similar results. However, the mobility decreases with the inclusion of the secondary phase, which is consistent with the behavior of multiphase materials^{41,42}.

Since the carrier concentration of all samples has similar values, these changes cannot simply behavior of the band structure with CrSb inclusion was analyzed by modeling the thermopower and Hall carrier concentration using the single parabolic band (SPB) model⁴³. The SPB model used here may not fully and accurately describe the behavior of multiphase samples due to the

5



FIG. 3. Temperature dependence of the (a) thermal conductivity, (b) electronic thermal conductivity, (c) lattice thermal conductivity, (d) figure of merit zT of Bi_{0.5}Sb_{1.5}Te_{3+0.3} with x wt.% CrSb (x = 0, 0.125, 0.5, 0.5, 0.5) and 1) samples.

presence of bipolar conduction, complex scatter- the presence of CrSb, as seen in Table II. Since ing processes, and the non-parabolic nature of the thermopower for a degenerate semiconductor, the valence band. Nevertheless, this approach with a parabolic band and energy-independent provides useful insights into the trends of the scattering approximation, can be written as⁴³ carriers' effective mass, m^* , across all samples⁴⁴.

$$\alpha = \frac{8\pi^2 k_{\rm B}}{3qh^2} m^* T\left(\frac{\pi}{3n}\right)^{2/3},\tag{1}$$

The effective mass of samples is increased in where m^* is the effective mass. Eq. (1) suggests

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TABLE I. Room temperature Hall carrier concentra
tion and mobility of $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.?

CrSb (x = 0, 0.125, 0.5, and 1) samples

$x \qquad n_{\rm H}(\times 1)$	$0^{18} \mathrm{cm}^{-3}) \mu_{\mathrm{H}} (\mathrm{cr}$	$m^2.V^{-1}.s^{-1})$
0	7.7	232.0
0.125	7.7	203.9
0.5	7.3	185.5
1	7.1	161.6

TABLE II. Calculated effective of mass $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.% CrSb (x = 0, 0.125, 0.5, and 1) samples using the single parabolic band model

x	$m^*(m_0)$
0	0.90
0.125	1.16
0.5	1.06
1	1.21

terial can lead to an increase in the effective mass of the sample and, consequently, an increase in

ments6,16,46

The results show that despite the presence of a magnetic secondary phase with poor thermoelectric performance and low thermopower of approximately $12.5 \,\mu V.K^{-1}$ at room temperature and $4.38 \,\mu V.K^{-1}$ at 550 K, the electronic performance of the samples can be improved rather than degraded (see Fig. 2(d)).

The combined decrease in carrier mobility due to the presence of an additional phase and the possible dragging effect caused by the magnetic phase degrades the electrical conductivity of multiphase samples¹⁵. However, the overall effect was an increase in the power factor PF was detected (as shown in Fig. 2(c)).

The thermal conductivity (κ) of the samples is shown in Fig. 3(a). The electronic contribution to the thermal conductivity (κ_e) is shown in Fig. 3(b) and it was estimated using the Wiedemann-Franz law⁴⁷ ($\kappa_e = L\sigma T$) where L that the presence of a magnetic phase in the ma- is the Lorenz number, and it was calculated using the SPB model^{48,49}.

The lattice (κ_l) contribution to the thermal the thermopower. In magnetic materials, an ad- conductivity was calculated as $\kappa_l = \kappa - \kappa_e$, as ditional contribution to the thermopower is ob- shown in Fig. 3(c). The measured values for served when the materials are subjected to a tem- the lattice thermal conductivity are optimally perature gradient due to the flux of magnons⁴⁵. low, reaching values slightly below the glass-The interaction between magnons and carriers like thermal conductivity for Bi₂Te₃ ($\kappa_{\text{plass}} \approx$ results in an overall increase in the effective mass 0.31 W.m⁻¹.K⁻¹)³⁰ but higher than Cl-doped and, consequently, in the thermopower¹³. Simi- Bi₂Te₃ alloys (0.15 W.m⁻¹.K⁻¹)⁵⁰, namely the lar enhancement effects have been observed for sample containing the 0.125 wt.% of CrSb nonmagnetic materials doped with magnetic ele- reached the lowest value of $\sim 0.24 \,\mathrm{W.m^{-1}.K^{-1}}$.

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phase.

systematic decrease with increasing secondary phase fraction, which may be attributed to two competing mechanisms: the introduction of additional phonon scattering due to the secondary phase and the presence of a secondary phase with higher thermal conductivity⁵¹. In particular, the intrinsic thermal conductivity of CrSb is as high as 7.24 W.m^{-1} .K⁻¹,³⁵ which is much higher than that of the matrix $(1.25 \text{ W}.\text{m}^{-1}.\text{K}^{-1})$ at 300 K).

The figure of merit (zT) of the samples is shown in Fig. 3(d). The combination of significantly reduced thermal conductivity, aligned with an increase in thermal power due to the incorporation of the magnetic secondary phase, contributed to the high zT values for the multiphase samples compared to the single-phase Bi_{0.5}Sb_{1.5}Te_{3+0.3} material. It should be noted that the single-phase sample has a relatively low zT value of around 0.36, similar to what was observed for⁵², and indicates that the maximum zTfor this sample was below room temperature⁵³.

The 0.125 wt.% CrSb sample exhibited the

The low values for all samples indicate a high next highest zT of ~ 0.92 at 525 K, followed degree of scattering of the phonons due to addi- by the 1 wt.% CrSb at ~ 0.68 . The high zT valtional boundaries introduced by the secondary use result from the synergistic effects of magnetically induced thermopower enhancement and The thermal conductivity does not show a thermal conductivity reduction due to interfacial and magnetic scattering in the multiphase samples.

> In Fig. 4, the results obtained in this work are compared with other compositions seen in the literature^{54–59}, as well as with a commercial BiSbTe ingot. The introduction of the CrSb phase in the Bi_{0.5}Sb_{1.5}Te_{3+0.3} material shows a performance that surpasses the one seen for the commercial ingot and is comparable to the best results reported in the literature for composite BiSbTe materials.

A series of Bi0.5Sb1.5Te3+0.3 samples with varying concentrations of CrSb magnetic secondary phase (0, 0.125, 0.5, and 1 wt.%) were synthesized by a combination of ball milling and spark plasma sintering techniques. The results showed that the incorporation of small amounts of the CrSb magnetic phase significantly enhanced the thermopower of the samples by increasing the carriers' effective mass, which is consistent with previous findings for magnetic dopants. However, the electrical conductivity is adversely affected by the reduced carrier mohighest zT, reaching a peak value of ~ 1.4 at bility caused by the presence of the secondary 325 K. The other multiphase compositions also phase. The increase in the power factor, comshowed promising zT improvements, albeit to bined with the significantly lower thermal cona lesser extent. The 0.5 wt.% CrSb had the ductivity, resulted in a high figure of merit (zT)

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FIG. 4. ues of $Bi_{0.5}Sb_{1.5}Te_{3+0.3} + 0.125$ wt.%, commercial corresponding author upon reasonable request. BiSbTe, and other typical p-type BiSbTe composites: Bi_{0.5}Sb_{1.5}Te₃ + Fe₃O₄⁵⁴, Bi_{0.5}Sb_{1.5}Te₃ + carbon fiber⁵⁵, Bi_{0.46}Sb_{1.54}Te₃ + CdTe⁵⁶, Bi_{0.46}Sb_{1.54}Te₃ + SnTe⁵⁷, Bi_{0.46}Sb_{1.54}Te₃ + SiC⁵⁸, and Bi_{0.4}Sb_{1.6}Te₃ + CuGaTe₂⁵⁹.

values for CrSb added samples. These results confirm the potential benefits of incorporating magnetic secondary phases into thermoelectric materials to modulate their electronic and thermal transport properties favorably.

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AUTHOR DECLARATIONS

Data availability

The authors declare that the data supporting Temperature dependence of zT of the findings of this study are available within $Bi_{0.5}Sb_{1.5}Te_{3+0.3}$ with x wt.% CrSb (x = 0, 0.125, the paper. Should any raw data files be needed 0.5, and 1) samples. Comparisons of zT val- in another format, they are available from the

Declaration of competing interest

The authors have no conflicts to disclose.

REFERENCES

- ¹M. Zhang, W. Liu, C. Zhang, S. Xie, Z. Li, F. Hua, J. Luo,
- Z. Wang, W. Wang, F. Yan, Y. Cao, Y. Liu, Z. Wang,
- C. Uher, and X. Tang, ACS Nano 15, 5706 (2021).
- ²G. Yang, R. Niu, L. Sang, X. Liao, D. R. G. Mitchell, N. Ye, J. Pei, J.-F. Li, and X. Wang, Adv. Energy Mater. 10, 2000757 (2020).
- ³T. Hendricks, T. Caillat, and T. Mori, Energies 15, 7307 (2022).

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0235499

⁴I. T. Witting, T. C. Chasapis, F. Ricci, M. Peters, N. A. ¹⁷S. Das, S. M. Valiyaveettil, K.-H. Chen, S. Suwas, and Heinz, G. Hautier, and G. J. Snyder, Adv. Electron. Mater. 5, 10.1002/aelm.201800904 (2019). G. J. Snyder, Research 2020, 1 (2020). 7545 (2017). ⁷W. Koshibae, K. Tsutsui, and S. Maekawa, Phys. Rev. B 62, 6869 (2000). Adv. 5, eaat5935 (2019). 9Y. Zheng, T. Lu, M. M. H. Polash, M. Rasoulianborou-Chen, R. P. Hermann, D. Vashaee, J. P. Heremans, and H. Zhao, Sci. Adv. 5, eaat9461 (2019). ¹⁰M. Bailyn, Phys. Rev. **126**, 2040 (1962). ¹¹J. D. Wasscher and C. Haas, Phys. Lett. B 8, 302 (1964). ¹²N. Tsujii and T. Mori, Appl. Phys. Express 6, 043001 (2013). 13R. Ang, A. U. Khan, N. Tsujii, K. Takai, R. Nakamura, (2015), pubmed:26332260. 14C. Peng, G. Zhang, C. Wang, Y. Yan, H. Zheng, Y. Wang, Letters 12, 1800172 (2018). N. Kobayashi, and T. Mori, Mater. Today Phys. 9, 100090 (2019). ¹⁶S. Acharya, S. Anwar, T. Mori, and A. Soni, J. Mater. Chem. C 6, 6489 (2018).

R. C. Mallik, Mater. Res. Express 6, 10.1088/2053-1591/aaf710 (2019).

- ⁵I. T. Witting, F. Ricci, T. C. Chasapis, G. Hautier, and ¹⁸H. Matsuura, M. Ogata, T. Mori, and E. Bauer, Phys. Rev. B 104, 214421 (2021).
- ⁶F. Ahmed, N. Tsujii, and T. Mori, J. Mater. Chem.A 5, ¹⁹W. Zhao, Z. Liu, P. Wei, Q. Zhang, W. Zhu, X. Su, X. Tang, J. Yang, Y. Liu, J. Shi, Y. Chao, S. Lin, and Y. Pei, Nat. Nanotechnol. 12, 55 (2017), pubmed:27723733.
- ⁸N. Tsujii, A. Nishide, J. Hayakawa, and T. Mori, Sci. ²⁰R. Lu, J. S. Lopez, Y. Liu, T. P. Bailey, A. A. Page, S. Wang, C. Uher, and P. F. P. Poudeu, J. Mater. Chem.A 7, 11095 (2019).
- jeni, N. Liu, M. E. Manley, Y. Deng, P. J. Sun, X. L. ²¹K. G. Liu and J. Li, Frontiers of Green Building, Materials and Civil Engineering, Pts 1-8 71-78, 3741 (2011).
 - ²²C. Bourgès, W. Zhang, K. K. Raut, Y. Owada, N. Kawamoto, M. Mitome, K. Kobayashi, J.-F. c. Halet, D. Berthebaud, and T. Mori, ACS Appl. Energy Mater. 6,9646 (2023).
 - 23Y.-H. Gao, H. Chen, N. Liu, and R.-Z. Zhang, Results Phys. 11, 915 (2018).
- and T. Mori, Angew. Chem. Int. Ed. Engl. 54, 12909 ²⁴Z. Liu, J. Zhu, P. Wei, W. Zhu, W. Zhao, A. Xia, D. Xu, Y. Lei, and J. Yu, ACS Appl. Mater. Interfaces 11, 45875 (2019).
- and M. Hu, physica status solidi (RRL) Rapid Research ²⁵V. Marghussian, in *Nano-Glass Ceramics* (Elsevier, 2015) pp. 181-223.
- ¹⁵J. B. Vaney, S. A. Yamini, H. Takaki, K. Kobayashi, ²⁶G. Tan, F. Shi, S. Hao, H. Chi, T. P. Bailey, L. D. Zhao, C. Uher, C. Wolverton, V. P. Dravid, and M. G. Kanatzidis, J. Am. Chem. Soc. 137, 11507 (2015), pubmed:26308902.
 - ²⁷S. Vandendriessche, W. Brullot, D. Slavov, V. K. Valev, and T. Verbiest, Appl. Phys. Lett. 102, 161903 (2013).

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0235499

- ²⁸W. Zhao, Z. Liu, Z. Sun, Q. Zhang, P. Wei, X. Mu, ³⁸X. Huang, X. Feng, Q. An, B. Huang, X. Zhang, Z. Lu, H. Zhou, C. Li, S. Ma, D. He, P. Ji, W. Zhu, X. Nie, X. Su, X. Tang, B. Shen, X. Dong, J. Yang, Y. Liu, and J. Shi, Nature 549, 247 (2017), pubmed:28905895. ²⁹H.-L. Zhuang, J. Pei, B. Cai, J. Dong, H. Hu, F.-H. Sun,
- Y. Pan, G. J. Snyder, and J.-F. Li, Adv. Funct. Mater. 31, 2009681 (2021).
- ³⁰Y. Liu, Y. Zhang, S. Ortega, M. Ibáñez, K. H. Lim, A. Grau-Carbonell, S. Martí-Sánchez, K. M. Ng, J. Ar-⁴¹D. K. Ko, Y. Kang, and C. B. Murray, Nano Lett. 11, biol, M. V. Kovalenko, D. Cadavid, and A. Cabot, Nano Lett. 18, 2557 (2018).
- ³¹R. Deng, X. Su, Z. Zheng, W. Liu, Y. Yan, Q. Zhang, V. P. Dravid, C. Uher, M. G. Kanatzidis, and X. Tang, ⁴³G. J. Snyder and E. S. Toberer, Nat. Mater. 7, 105 (2008). Sci. Adv. 4, eaar5606 (2018).
- ³²N. S. Chauhan, S. V. Pyrlin, O. I. Lebedev, L. S. A. Marques, M. M. D. Ramos, T. Maiti, K. Kovnir, B. A. Korgel, and Y. V. Kolen'ko, The Journal of Physical ⁴⁵S. J. Watzman, R. A. Duine, Y. Tserkovnyak, S. R. Chemistry C 125, 20184 (2021).
- ³³H.-S. Kim, N. A. Heinz, Z. M. Gibbs, Y. Tang, S. D. Kang, and G. J. Snyder, Mater. Today 20, 452 (2017).
- 34H. Dohnomae, K. Shintaku, N. Nakayama, and T. Shinjo, Journal of Magnetism and Magnetic Materials 126, 346 (1993).
- ³⁵M. M. H. Polash, F. Mohaddes, M. Rasoulianboroujeni, and D. Vashaee, J. Mater. Chem. C 8, 4049 (2020).
- ³⁶A. Kanatzia, C. Papageorgiou, C. Lioutas, and T. Kyratsi, J. Electronic Mater. 42, 1652 (2012).
- ³⁷V. M. Prokhorov, G. I. Pivivarov, V. M. Levin, and E. S. Morokov, IOP Conference Series: Materials Science and Engineering 42, 012003 (2012).

G. Li, P. Zhai, B. Duan, G. J. Snyder, W. A. Goddard, and Q. Zhang, Matter 6, 3087 (2023).

- ³⁹Y. Zhong, S. Chen, J. Cai, Z. Zhang, F. Gao, S. Huo, J. Wu, C. Cui, X. Tan, G. Liu, and J. Jiang, ACS Applied Electronic Materials 6, 2552 (2024).
- 40H.-S. Kim, K. H. Lee, and S.-i. Kim, Journal of Materials Research and Technology 14, 639 (2021).
- 2841 (2011), pubmed:21630679.
- 42Y.-X. Zhang, Y.-K. Zhu, D.-S. Song, J. Feng, and Z.-H. Ge, Chem. Commun. 57, 2555 (2021).
- 44Y. Zheng, Q. Zhang, X. Su, H. Xie, S. Shu, T. Chen, G. Tan, Y. Yan, X. Tang, C. Uher, and G. J. Snyder, Adv. Energy Mater. 5, 1401391 (2015).
- Boona, H. Jin, A. Prakash, Y. H. Zheng, and J. P. Heremans, Physical Review B 94, 144407 (2016).
- ⁴⁶R. Fortulan, S. A. Yamini, C. Nwanebu, S. Li, T. Baba, M. J. Reece, and T. Mori, ACS Applied Energy Materials 5, 3845 (2022).
- ⁴⁷M. Jonson and G. D. Mahan, Phys. Rev. B 21, 4223 (1980).
- ⁴⁸A. F. May, E. S. Toberer, A. Saramat, and G. J. Snyder, Physical Review B 80, 125205 (2009).
- 49T. Fang, X. Li, C. Hu, Q. Zhang, J. Yang, W. Zhang, X. Zhao, D. J. Singh, and T. Zhu, Advanced Functional Materials 29, 1900677 (2019).
- ⁵⁰T. Parashchuk, R. Knura, O. Cherniushok, and K. T. Wojciechowski, ACS Appl. Mater. Interfaces 14, 33567

PLEASE CITE THIS ARTICLE AS DOI: 10.1063/5.0235499

(2022).

- ⁵¹G. Yang, L. Sang, D. R. Mitchell, F. Fei Yun, K. Wai See, A. Jumlat Ahmed, S. Sayyar, A. Bake, P. Liu, L. Chen, Z. Yue, D. Cortie, and X. Wang, Chemical Engineering Journal 428, 131205 (2022).
- ⁵²Z. Wei, C. Wang, L. You, S. Zhao, K. Yang, H. Chen, J. Luo, and X. Chen, RSC Adv. 7, 41111 (2017).
- ⁵³S. Bano, D. K. Misra, J. S. Tawale, and S. Auluck, Journal of Materiomics 7, 1264 (2021).
- Q. Zhang, and W. Zhao, Energ. Environ. Sci. 13, 535 (2020).

- 55G. Yang, L. Sang, F. F. Yun, D. R. G. Mitchell, G. Casillas, N. Ye, K. See, J. Pei, X. Wang, J.-F. Li, G. J. Snyder, and X. Wang, Adv. Funct. Mater. 31, 2008851 (2021).
- ⁵⁶Q. Tao, R. Deng, J. Li, Y. Yan, X. Su, P. F. P. Poudeu, and X. Tang, ACS Appl. Mater. Interfaces 12, 26330 (2020).
- ⁵⁷D. Zhang, J. Wang, L. Zhang, J. Lei, Z. Ma, C. Wang, W. Guan, Z. Cheng, and Y. Wang, ACS Appl. Mater. Interfaces 11, 36658 (2019).
- ⁵⁴C. Li, S. Ma, P. Wei, W. Zhu, X. Nie, X. Sang, Z. Sun, ⁵⁸D. Zhang, J. Lei, W. Guan, Z. Ma, C. Wang, L. Zhang, Z. Cheng, and Y. Wang, J. Alloys Compd. 784, 1276 (2019).
 - ⁵⁹Y. Li, X. Wang, G. Liu, B. Shin, and F. Shan, Scr. Mater. 172, 88 (2019).